# INFLUENCE OF LININGS ON STRESS AND DEFORMATION IN ROCK AROUND ELLIPTICAL TUNNELS 

## A THESIS SUBMITTED IN PARTIAL FULFILMENT OF THE DEGREE OF MASTER OF ENGINEERING



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## DECLARATION

The work included in the thesis in part or whole, has not been submitted for any other academic qualification at any institution.

Signature of the Candidate

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#### Abstract

Stress and deformation behavior in rock surrounding elliptical tunnels with concrete liners is investigated by finite element analysis. The loading condition is limited to hydrostatic pressure applied inside the tunnel and it is assumed that the constitutive behaviors of both rock and concrete are according to isotropic linear elasticity. Plain strain conditions are assumed to prevail for the tunnels, which is the case when tunnels with straight axis in uniform rock media are considered.

Three elliptical tunnel geometries with major to minor axis ratios of $1.156,1.358$ and 1.500 are considered for the study. Each problem geometry was analysed for liner thickness varying from 0.0 m (unlined case) to 1.0 m in steps of 0.2 m , assuming that the Young's Modulus for rock is $1 / 10^{\text {th }}$ of that of concrete. The result for stress and deformation are presented for the rock domain, both in tabular and graphical forms. These numerical results illustrate the effect of concrete liner thickness and tunnel geometry on stress and deformation in rock.


A limited parametric study is conducted by varying the Young's Modulus of rock for a selected tunnel geometry with a concrete liner thickness of 0.2 m .

The present research makes a significant contribution to tunnel engineers, providing numerical tools to arrive at an optimum tunnel geometry and liner thickness, by striking a balance between cost and efficiency.

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## ABBREVIATIONS

| eg | - exempli gratia ( example) |
| :---: | :---: |
| etc | - et ceteri or cetera ( and the others) |
| hr | - hour |
| i.e. | - id est (that is) |
| kN | - kilo Newton |
| m | - metre |
| $\mathrm{m}^{2}$ | - square metre |
| mm | - millimetre |
| N | - Newton |
| $\mathrm{N} / \mathrm{m}^{2}$ | - Newton per square metre |
| $\mathrm{N} / \mathrm{mm}^{2}$ | ${ }^{2}$ - Newton per square millimetre |
| No |  |
| Pa | - Pascal |
| \% | - Percentage |
| $<$ | - Less than |
| > | - Greater than |
| 0 | - Degree |
| $v$ | - Poisson's ratio |
| $\rho$ | - Density of soil |
| $\tau$ | - Stress in tangential direction |
| $\sigma_{H}$ | . Stress in horizontal direction |
| $\sigma_{v}$ | . Stress in vertical direction |

## CHAPTER 01

## INTRODUCTION

Tunnel construction was first introduced for mining operations in late $16^{\text {th }}$ and early $17^{\text {th }}$ centuries in Europe and United States of America. These tunnels were mainly used to reach mineral deposits and coal deposits. Most of these tunnels consisted of a vertical part and a horizontal part or an angle part depending on the ground condition. In the early designs in tunneling operations, people had to face problems of roof collapse on the working areas. This was overcome by making the tunnel roof as an arch which is a structural form that can take high compressive load. The exception was coal mines; roof of the coal mine was flat. In some cases temporary roof support was achieved by using steel or timber structures. But with the advancement of science and technology, people started to construct underground road systems (highways and railways) to minimize the traffic congestion. These tunnels had to be protected from collapses of roof. For this purpose, tunnel linings were introduced as a protective measure for highway tunnels. Tunnels have many more uses other than highways and railways, as discussed in chapter2. Tunnels may be constructed through rock or soils.

Tunnels in rock constitute an important area in civil and mining engineering. Tunnels can be classified according to many aspects, e.g. based on the shape, utility, location, media, etc. A comprehensive documentation on tunnels and tunnelling has been compiled by Szechy (1973).

Stress and deformation fields in rock surrounding funnel excavations are of considerable importance in tumnel engineering. The stress fields set up due to different load systems that are imposed on the tunnel walls can be used to identify potential failure regions in the surrounding rock. Many instances arise where stresses transmitted to the surrounding rock need to be reduced by some appropriate means. An example for this is the tensile normal tangential stress set up in rock surrounding a circular or elliptical tunnel conveying water under pressure, which causes hydraulic fracturing of the rock at high magnitudes. A concrete lining is often introduced to tunnels to prevent generation of high stresses in the surrounding rock mass, in addition to other potential purposes such as protecting the exposed rock surface from weathering/erosion, controlling seepage of water, and preventing rock falls.

The calculation of the stress distribution around a circular hole in an infinite plate was first solved with the aid of mathematical theory of linear elasticity by Kirsch in 1898 (Herget, 1988). Herget (1988) gives a summary of the typical stress distribution patterns around a circular opening. According to the Kirsch equations, Jaeger (1979) gives the analytical solutions for unlined and lined circular openings in rock. More complex shapes of underground openings have also been considered in the literature, which are useful in mining and civil engineering (e.g. Obert et al. 1960). Finite element analysis has been proposed/used by many authors (e.g. Goodman 1976). The boundary integral equation method has been used to calculate stresses by
superimposing two stress systems, which are the original stress state, and the stresses induced by superimposing negative surface stresses which result from the removal of material which originally existed in the excavation (Hocking 1976). Boundary element method has been used to analyse tabular ore bodies, under the concept of displacement discontinuity models (Crouch and Starfield, 1983).

This work illustrates the effect of tunnel lining on the stress distribution and deformation behaviour in the surrounding rock mass for elliptical tunnels (Szechy 1973), through the use of finite element analysis. Three elliptical tunnels with different ratios of major radius/minor radius are considered. Concrete linings of different thickness are introduced to investigate the stress and deformation behaviour in the rock mass numerically. It is assumed that material behaviour for both the rock-mass and concrete is isotopic linear elastic, and that conditions of plane strain prevail in all cases considered.

Stress and deformation behaviour in rock surrounding lined elliptical tunnels subjected to hydrostatic pressure is investigated here. The influence of different elliptical shapes of the tunnel, thickness of the concrete liner, and the variation of rock stiffness, on the stress and deformation behaviour of the rock surrounding the tunnel is derived through a parametric finite element study. Elliptical tunnels having three different ratios of major to minor radii (ratios of $1.156,1.358$, and 1.500 ) are considered. The different tunnel geometries are analysed assuming plane strain conditions, for different concrete liner thicknesses (thickness changing from 0.0 m to 1.0 m , in steps of 0.2 m ). A limited parametric study is conducted by varying the Young's modulus of the rock while keeping the other variables constant. The results show the effect of tunnel shape, liner thickness and rock stiffness on the stress and deformation distribution in rock surrounding elliptical tunnels

This analysis is useful in identifying the effect of liner thickness on critically stressed areas, the optimum liner thickness for a tunnel in a particular rock type, and a convenient geometrical shape as far as stress and deformation in rock are concerned.


## CHAPTER 02

## 2. TUNNELS IN ROCK AND SOIL

### 2.1. Tunnel Classifications

### 2.1.1. Classifications Based on Service

Tunnels can be classified according to their service as follows (Szechy 1973; Jeager 1979).

## (a). Highway Tunnels

Highway tunnels accommodate all types of vehicles permitted on public highways, except that their use by bicycles and horse drawn vehicles may be limited or prohibited.

## (b). Railroad Tunnels

Railroad tunnels service standard railroad trains and may need special clearances for electrical traction from catenaries.

## (c). Rapid Transit Tunnels



These tumnels service urban and metropolitan rapid transit trains, and are designed to meet the requirements of particular systems.

## (d). Aqueducts and Sewer Tunnels

Used to convey fresh water or sanitary wastes and storm water, the sizes and construction of these tunnels vary according to local conditions.

## (e). Underground Caverns

These are tunnels built to house underground hydroelectric power plants, hardened defense facilities, and special waste storage (e.g. nuclear waste).

## (f). Shafts

There are vertical or inclined excavations that serve as access to mines or tunnel construction or for tunnel ventilations. They are built according to the particular requirements.

## (g). Special Tunnels

Tunnels are also used to carry water pipes, electrical cables or other utilities specially in urban centers.

### 2.1.2. Classification Based on Tunnel Locations

Tunnel may be classified according to location as follows

## (a). Underwater Tunnels

These are built by various methods under rivers, harbours or other waterways to serve any one of the purpose listed above. These tunnels are used when clearance requirements, land use, and sometimes the environment prevent construction of bridges (e.g. Channel Tunnel, built from London to Paris, underneath the English channel).

## (b). Mountain Tunnels

Tunnels through mountains are used to carry transportation facilities or water (e.g. Canyon tunnel in Sri Lanka). These are frequent in some mountainous areas of the world (e.g. Switzerland, Austria, etc).

## (c). Tunnels at Shallow Depths and Beneath City Streets

These are primarily used for rapid transit and other transportation in urban areas. Large metropolitan areas in the world are usually serviced by these system (e.g. London, New York, Vancouver, etc.)

## (d). Bored vs Cut-and-Cover Tunnels

Bored by whatever means, these tunnels require a minimum overburden depending upon soil conditions. Shallow tunnels are most economical by cut-and-cover construction unless other conditions preclude this method.

### 2.1.3. Classification Based on Tunnel Media

Geological conditions greatly affect the cost of tumel construction as indicated below:

## (a). Rock Tunnels

Rock tunnels are excavated in a firm, cohesive medium which may vary from relatively soft marl and sandstone to the very hard igneous rocks such as granite. Bedding and fissuring of rock layers and the presence of water are major factors that control construction methods and pose difficulties.
(b). Soft Ground Tunnels

This category indicates all tunnels built in soft, plastic or non-cohesive soils where water may or may not be a problem.

## (c). Mixed Phase Tunnels

These tunnels have part of their cross-sections in rock and part in soft ground, with rock interface often weathered. There are frequent construction difficulties.

### 2.1.4. Some Aspects in Tunnel Construction

The methods for tunnel constructions vary according to geological conditions, hydrological conditions, length of tunnels, size and shape of tunnel section, type of equipment to be used for excavations and its intended purpose. Out of these, sub surface (geological) conditions, and size and shape of tunnel cross-section are the main factors governing the construction process of tunnel.


### 2.2. Factors Influencing the Tunneling Operation

Owing to the number of factors influencing the design, loading, location and construction of tunnels, various tunneling systems have been developed.

The major influencing factors are as follows:
(1). Geological conditions.
(2). Shape and cross-sectional dimension of the tunnel.
(3). Intended purpose.

The construction of tunnels involves carrying out of the following operations.
(1). Excavations.
(2). Support.
(3). Transportation of excavated materials.
(4). Lining or coating, sealing, draining and ventilation.

The tunneling operations vary according to the conditions discussed earlier. While excavation and the transport of the excavated material is always an indispensable necessity, the type of working conditions and the means of transportation used may differ widely, and the importance and extent of both the support of the excavated cavities and
the process mentioned at (4) above can vary likewise, within a wide range. Thus required operations can be carried out by various methods which can be grouped into the following categories.
(1). Full -face tunneling without temporary support
(2). Full-face tunneling with support .
(3). Combined underground and open surface(cut-and-cover method).
(4). Pre-cast element and caisson sinking method.
(5). Pre-cast element method.
(6). Shield driving method.
(7). New Austrian Tunneling Method (NATM).

The first method can only be applied in solid rocks having RQD(Rock Quality Designation) $90 \%$ or more whereas the methods belonging to group (2) which afford supports of variable extent and strength can be applied in other rocks. In loose and weak rocks and in cohesive and granular soil all the other methods except at (1) and (2) can be applied. Methods mentioned at (5) and (6) afford good results in exceptionally soft and loose ground. The NATM is a flexible tunnel construction method which is adoptable in varying ground conditions from hard rock to soil.

### 2.3. Methods of Tunnel Linning

Most tunnels require temporary support during the boring operation prior to the introduction of permanent support. It is the usual practice to place permanent lining after excavation of the entire tunnel is complete (even in large tumels).

A shallow masonry construction was used for lining in early highway tunnels. Until recently, railroad tunnels relied on timber supports. Many early sewer tunnels were lined with brick (e.g. sewer tunnel under Darley Road, Colombo). Presently concrete lining, usually cast in place, has largely replaced all other materials in all types of tunnels. Concrete lining is frequently placed without reinforcement, but where bending effects are serious, reinforcement may be required. Low-pressure grout is usually used to fill the voids that would otherwise always occur in the tunnel roofs. If the tunnel design relies on the rock to resist internal pressures of a water conveying tunnel, high-pressure grout is usually used to fill shrinkage cracks between the concrete and rock. Shotcrete, used for temporary support, is receiving more favour as permanent lining where smooth surfaces are not required. Rock bolts are sometimes used for permanent support. In this case, they must be grouted for protection against corrosion and are usually used with wire mesh, covered with a thin layer of shotcrete. Highway tunnels sometimes have a tile lining on the walls, attached to the main concrete lining.

## Example:

Canyon Tunnel Details:
Canyon hydro-electricity project consist of a reservoir with concrete gravity dam, conveying tunnel, steel penstock and power house.

The geological condition of this area was fairly good. But in some locations there were weak zones. Hence the geotechnical investigation report emphasised to line the entire tunnel. (The rock encountered mainly consists of Charnokitic rock and Gneisses).

This tunnel was a horseshoe shape tunnel with internal diameter of 3.40 m (see figure 2.1 ) and the tunnel discharge capacity of 19.8 cumecs ( 700 cusecs). To prevent erosion of tunnel wall and seepage of water through tunnel wall, the tunnel was lined with a reinforced concrete liner, whose thickness varied from 0.1 m onwards.


COKCRETE LMAO


Figure 2.1 Tunnel Section After Introduction of Concrete Liner

### 2.4. Stress and Strain in Rock

### 2.4.1. Stresses in Rock

Stresses in rock masses are a fundamental concern in the design of underground excavations in Civil and Mining Engineering projects (Herget 1988; Jaeger 1979). Only an assessment of stresses in rock will allow the application of strength determination and failure theories to a rational design for excavation in rock.

Rock masses in nature are usually under the influence of a stress field. This is known as the natural stress field of the rock, according to its origin. The stress distribution in a rock-mass at a given point of time in his history depends on the history of its constitutive behaviour. Rock-mass may deform according to various constitutive models like elasticity, plasticity, creep, etc, depending on the magnitude and duration of the loading, material properties and boundary conditions. Often, materials display a combination of these various constitutive models. The actual constitutive behaviour of a material is referred to as the rheology of the material.

When man-made excavations or structures are imposed on rock, the naturally occurring stress fields are affected and changed. Such changes are of great concern to rock mechanists. Stress changes induced due to activity of man are known as induced stresses.

### 2.4.2 Natural Stresses

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### 2.4.2.1. Gravitational Stress

Gravity stresses result from the weight of the column of rock per unit area above in the earth's crust. The vertical component of this stress $\sigma_{v}$ can be calculated from.

$$
\sigma_{v}=\int \rho \mathrm{g} \mathrm{dz}-\cdots---\cdots---(2.1)
$$

where $\rho$ is the density of rock, $g$ is the acceleration of gravity and $z$ denotes depth.
While the vertical component can be easily defined, the horizontal component is more difficult to define because of the effect of different boundary conditions and rock mass properties. The stress distribution at a point depends on the constitutive behaviour (stress-strain relationship) of the material through its history of existence.

If the rock mass is assumed to be homogeneous, isotropic and elastic with the boundary conditions not allowing horizontal displacement, the horizontal stress $\sigma_{H}$ is given by

$$
\begin{equation*}
\sigma_{H}=v \sigma_{v} /(1+v) \tag{2.2}
\end{equation*}
$$

where $v$ is the Poisson's ratio.

If the rock material is not elastic and allowance need to be made for creep because of viscosity, it will not sustain shear stresses in the long term, i.e., the rock will flow. In such cases,

$$
\begin{equation*}
\sigma_{H}=\sigma_{v} \tag{2.3}
\end{equation*}
$$

Thus in general it can be written as;

$$
\begin{equation*}
\sigma_{H}=K \sigma_{v} \tag{2.4}
\end{equation*}
$$

where K is a parameter in the range, $0<\mathrm{K}<1$.

Equation (2.3) describes a hydrostatic stress field, but in relation to rocks, it is preferable to use the term 'lithostatic'. In the case of a lithostaic stress field, the weight of the overburden acts in all directions; such situations can be found in areas where sedimentation is ongoing, and the sediments have a high water content. A lithostatic stress field is also expected to exist at great depth in the earth's crust:'

In the general case defined by equation (2.4), K can vary from 0 , with no lateral support, to $\mathrm{K}=1$ for a lithostatic stress field.

### 2.4.2.2. Tectonic Stresses

The earth is not an inert body; movements in the earthis crust occur continuously and seismic events related to these deformations are recorded often. Tectonic plates in the crust move upon the relatively plastic mantle below it due to the driving force provided by the heat differences between the hot core of the earth and the cooler crust.

Teconic stresses are stresses induced in rock crust by the movement of tectonic plates. Some of these stresses may have been locked up in the crust for very long periods of time. Some stresses are subsequently relieved through rock deformation. Regional differences in stress result from the different thicknesses of crustal material which restrict mantle flow in certain regions. Horizontal stresses are generally larger than the vertical stresses. These are difficult to quantity or measure with respect to magnitude and direction, unless there are recent tectonic movements and seismic activity.

One can conceptually distinguish between current or active tectonic stresses and remnant or previous tectonic stress (Herget, 1988). Remnant tectonic stresses are left-over stresses which were not fully relieved by rock deformation. However, due to lack of data, it is difficult to generally distinguish between the current and remnant stress fields. There is some evidence to suggest that current tectonic stresses lead to relatively consistent stress fields over large areas, and seismic events and current deformation suggest a current tectonic stress regime (Herget, 1988).

### 2.4.2.3. Residual Stresses

Residual stresses are self- equilibrating stresses. These stresses are locked-in by the rock fabric while the outer surface of the rock sample is free of stress.

### 2.4.2.4. Thermal Stresses

Thermal Stresses are set up due to heating or cooling of rock (Heating may be due to sunlight close to the earth's surface, or by radioactivity or other geological processes deep inside the crust). As an example, a typical liner coefficient of thermal expansion for sandstone would be $10.8 \times 10^{-8}$ per $1^{0} \mathrm{C}$ of temperature.

### 2.4.3. Induced Stresses

Induced stresses are the result of excavation activity and therefore are of great concern in underground excavation design. Stress distribution in the back and wall of an excavation are different from those existing in the unmined rock because material had been removed.

### 2.5. Stress Distributions in the Earth's Crust

The stress distribution inside the earth's crust has much relevance in the field of Geotechnical and Rock Engineering today. There are many theories developed by researchers during the last two to three decades(Hast 1969, Artyushkove 1971, Herget 1980)

### 2.5.1. Horizontal Stresses for Canadian Shield

Equations $2.5,2.6 \& 2.7$ show horizontal stress components from stress determinations in the Canadian Shield. The relationship of the average horizontal stress component with depth being greater than $\sigma_{v}$ is not constant. Three relationships have been identified for $\sigma_{H}>\sigma_{\mathrm{v}}$ by Herget (1980) and updated in 1988:

$$
\begin{align*}
& \text { 1. } 0-800 \mathrm{~m}, \sigma_{\mathrm{H}}=0.0581 \mathrm{MPa} / \mathrm{m} \text {, }  \tag{2.5}\\
& \text { 2. } 800-2200 \mathrm{~m}, \sigma_{\mathrm{H}}=35.79 \mathrm{MPa}+0.0111 \mathrm{MPa} / \mathrm{m} \text {, }  \tag{2.6}\\
& \text { 3. Extreme values } \sigma_{\mathrm{H}}=14.45 \mathrm{MPa}+0.0563 \mathrm{MPa} / \mathrm{m} . \tag{2.7}
\end{align*}
$$

Relationship 3 in Figure 2.2(Herget 1988) relates to determinations where the vertical stress components were also found to be high. Although areas with extremely high horizontal stresses appear to be of limited extent, they could produce their own stability problems as the areas are approached underground.


Figure 2.2. Variation of horizontal stress components with depth for Canadian Shield(after Herget, 1988)

### 2.5.2. Vertical Stress for Canadian Shield

Figure 2.3(after Herget, 1988) shows the vertical stress with the depth for Canadian Shield. However, the simple gravity relationship does not explain all the observations which have been made. A second relationship is shown in figure 2.3 also which gives a gradient of $0.0603 \mathrm{MPa} / \mathrm{m}$. These values may be found in the vicinity of faults or shear zones.


Figure 2.3. Variation of vertical stress components with depth for Canadian Shield(after Herget, 1988)


Figure 2.4 The influence of a geological fault on the stress distribution in the vicinity of the underground opening(after Herget, 1988)

Figure 2.4 shows the influence of a geological fault on the stress distribution in the vicinity of the underground opening for the Canadian shield (after Herget, 1988)

A useful way of summarizing the above results is given by plotting the ratio (k) of horizontal to vertical stress components with depths.

Figure 2.5 presents the ratio of maximum $\sigma_{H} / \sigma_{v}$ to depth for the Canadian Shield of Northern Ontario based on an inverse relationship (Herget 1988).


Figure 2.5. Change of maximum horizontal stress to vertical stress ratio with depth(after Herget, 1988)

The separation of the horizontal stress components into maximum, average and minimum values is given in figure 2.6(Herget 1988). These Graphs show the tendency of the ratio of the horizontal to vertical stress components to approach 1 to 1.5 at a depth 3000 metres.


Figure 2.6 Change of maximum and minimum horizontal stress to vertical stress ratio with depth(after Herget, 1988)

### 2.5.3. Vertical Stress Based on World Data

Figure 2.7(after Herget, 1988) shows a plot of vertical stress components with depth which were determined over a range of depth from surface to a depth of 2400 m . Over this depth the magnitude changes between zero to 100 MPa .

According to the range of density for the rocks close to the surface of the earth, the gravity stress gradient will vary between $0.025 \mathrm{MPa} / \mathrm{m}$ for acidic rock and $0.035 \mathrm{MPa} / \mathrm{m}$ for basic rock with an average of $0.026 \mathrm{MPa} / \mathrm{m}$ (after Hergte, 1988).


Figure 2.7 Increase of Vertical Stress with depth(after Herget, 1988)

### 2.5.4. Horizontal Stress

From figure 2.8(after Hergte, 1988) it can be seen that the case where stress in a horizontal direction are lower or equalute vertical stress are rather rare, and that frequently horizontal stresses are higher than fettical stresses. Horizontal stresses close to the surface are rather high at approximately 10 mpa


Figure 2.8 Increase of Horizontal Stress with depth(after Herget, 1988)

### 2.6. Stresses Around Underground Openings

All rock in the ground are subjected to compressive stresses, and if an excavation is made, the rock left standing has to take more load because the original support made by the rock within the excavation has been removed.

The changes in stress around the circular opening in elastic material is shown in the figure 2.9 by the trajectories of the maximum principal compressive stress. Trajectories identify the direction of principal stress by the tangent at each point of the trajectory. The relative magnitude of stresses may be judged by the number of the lines per unit width.

Figure 2.9 shows a crowding of the maximum principal stress trajectories on the side of the opening and a widening at the top and bottom. Crowding indicates an increase in compression and a wider spacing indicates a reduction in stress. It can also be seen that the direction of the maximum principal compressive stress is vertical at the top and bottom but deviates considerably from vertical in the vicinity of the opening.

The closest analogy to this behavior is the stream line analogy for laminar flow. If a round object similar in shape as the cross section of this opening is placed as an obstruction in the flow line, a crowding of stream lines (acceleration of flow) at the sides and a spreading (slowing of flow) in front and behind the obstacle is observed. Calculation of stresses around the opening can be carried out by mathematical theory, numerical modeling, photo elasticity and by using analog models( Herget, 1988).


Figure2.9 Principal Stress Trajectories (after Herget, 1988)

### 2.6.1. Circular and Elliptical Openings in Media

The calculation of the stress distribution around the circular opening in an infinite plate was first solved by with aid of mathematical theory of linear elasticity by Kirsch in 1898 (Herget, 1988). The plate is considered to be under a stress field designated by $\sigma_{x}$ and $\sigma_{y}$ as shown in the figure 2.10

In general, mathematical difficulties are reduced if the boundary of an opening can be made to coincide with the coordinates that are used for circular opening. The relationships between rectangular coordinates and polar coordinates are:

$$
\begin{align*}
& X=r \cos \theta  \tag{2.8}\\
& Y=r \sin \theta \tag{2.9}
\end{align*}
$$

The Kirsch equations give the radial stresses, tangential stresses and shear stresses at any point in an infinite plate with polar coordinates with $\theta$ defined from the direction of the normal stress component noted first. These are as given below by equations.

$$
\begin{align*}
& \sigma_{r}=0.5\left(\sigma_{x}+\sigma_{y}\right)\left(1-\mathrm{a}^{2} / r^{2}\right)+0.5\left(1+3 a^{4} / r^{4}-4 a^{2} / r^{2}\right) \cos 2 \theta  \tag{2.10}\\
& \sigma_{t}=0.5\left(\sigma_{x}+\sigma_{y}\right)\left(1+a^{2} / r^{2}\right)-0.5\left(\sigma_{x}+\sigma_{y}\right)\left(1+3 a^{4} / r^{4}\right) \cos 2 \theta  \tag{2.11}\\
& \tau_{r t}=0.5\left(\sigma_{x}+\sigma_{y}\right)\left(1-3 a^{4} / r^{4}+2 a^{2} / r^{2}\right) \sin 2 \theta
\end{align*}
$$



Figure 2.10 Stress field on a plate
In a biaxial stress field, the tangential boundary stresses at the end of the axes of an elliptical opening (with height $=\mathrm{H}$, width $=\mathrm{W}$ ) are given from elastic theory by the following equations.


Figure (2.11)Elliptical Excavation in a Plate

$$
\begin{align*}
\sigma_{\Lambda} & =\sigma_{v}+\sigma_{v} 2 \mathrm{~W} / \mathrm{H}-\sigma_{H}  \tag{2.13}\\
\sigma_{\mathrm{C}} & =\sigma_{H}+\sigma_{H} 2 \mathrm{~W} / \mathrm{H}-\sigma_{H} \tag{2.14}
\end{align*}
$$

### 2.6.2. Solution for Lined Tunnels Under Internal Pressure

Jeager (1979) considered (concrete) lined tunnels, and expressed analytical solution for a uniform pressure loading imposed internally (see figure2.12 for configuration). For concrete lined circular tunnels Jaeger (1979) gives the following solutions

For $\mathrm{c}<\mathrm{R}<\infty$, the stress $\sigma_{\mathrm{r}}$ is given by

$$
\begin{align*}
& \sigma_{\mathrm{r}}=\frac{m_{2} E_{2}}{m_{2}-1} B_{2}-\frac{m_{2} E_{2}}{m_{2}+1} \frac{C_{2}}{R^{2}}, \cdots  \tag{2.15}\\
& \sigma_{\mathrm{r}}=-\sigma_{1} \quad B_{2}=0 \quad m_{2}=1 / V_{2}
\end{align*}
$$

For $\mathrm{R}=\mathrm{c}$ on the rock side;

$$
\begin{aligned}
& \sigma_{\mathrm{r}}=\frac{m_{2} E_{2}}{m^{2}+1} C_{2}=p_{\mathrm{c}}=1 \lambda_{\mathrm{P}} \text {, } \\
& \mathrm{C}_{2}=-\frac{p_{c} c^{2}\left(m_{2}+1\right)}{E_{2} m_{2}}, \text { with } \mathrm{B}_{2}=0
\end{aligned}
$$

The radial displacement u for $\mathrm{R}=\mathrm{c}$ in the rock is

$$
\mathrm{u}_{\mathrm{R}=\mathrm{C}}=\mathrm{B}_{2} \mathrm{R}+\frac{C_{2}}{R}=\frac{p_{c} c}{E_{2}} \frac{m_{2}+1}{m_{2}},
$$

The stresses in the concrete lining are
For $R=b:$

$$
\begin{aligned}
& \sigma_{\mathrm{rb}}=p, \\
& \sigma_{\mathrm{tb}}=-\frac{c^{2}+b^{2}-2 \lambda c^{2}}{c^{2}-b^{2}} p ;
\end{aligned}
$$

For $\mathrm{R}=\mathrm{c}$ :

$$
\sigma_{\mathrm{rc}}=\lambda \mathrm{p},
$$



$$
\sigma_{\mathrm{tc}}=-\frac{2 b^{2}-\lambda\left(c^{2}+b^{2}\right)}{c^{2}-b^{2}} p
$$

In the concrete
For $\mathrm{R}=\mathrm{b}$

$$
\begin{equation*}
\sigma_{\mathrm{R}=\mathrm{b}}=\frac{m_{1} E_{1}}{\left(m_{1}-1\right)} \mathrm{B}_{1}-\frac{m_{1} E_{1}}{\left(m_{1}+1\right)} \frac{C_{1}}{b^{2}}=\mathrm{p} \tag{2.18}
\end{equation*}
$$

For $\mathrm{R}=\mathrm{c}$

$$
\begin{align*}
& \mathrm{\sigma}_{\mathrm{R}=\mathrm{c}}=\frac{m_{1} E_{1}}{\left(m_{1}-1\right)} \mathrm{B}_{1}-\frac{m_{1} E_{1}}{\left(m_{1}+1\right)} \frac{C_{1}}{c^{2}}=\lambda_{\mathrm{p}}  \tag{2.19}\\
& \mathrm{C}_{1}=-\frac{m_{1}+1}{m_{1} E_{1}} \frac{c^{2} b^{2}}{\left(c^{2}-b^{2}\right)}(1-\lambda) p \\
& \mathrm{~B}_{1}=-\frac{m_{1}-1}{m_{1} E_{1}} \frac{\left(b^{2}-\lambda c^{2}\right)}{c^{2}-b^{2}} \mathrm{p}
\end{align*}
$$

Equating the elastic displacement
For $\mathrm{R}=\mathrm{c}$

$$
\begin{align*}
& \mathrm{u}_{\mathrm{R}=\mathrm{c}}=\mathrm{B}_{1} \mathrm{c}+\frac{C_{1}}{c}=\mathrm{B}_{2} \mathrm{c}+\frac{C_{2}}{c} \cdots \cdots(2.20)  \tag{2.20}\\
& \frac{m_{1}-1}{m_{1} E_{1}} \frac{\left(b^{2}-\lambda c^{2}\right)}{c^{2}-b^{2}} \mathrm{cp}+\frac{m_{1}+1}{m_{1} E_{1}} \frac{c^{2} b^{2}}{\left(c^{2}-b^{2}\right)}(1-\lambda) p=\frac{m_{2}+1}{m_{2}} \frac{c}{E_{2}} \lambda_{\mathrm{p}}
\end{align*}
$$

$$
\begin{equation*}
\lambda=\frac{p_{c}}{p}=\frac{\frac{2 b^{2}}{E_{1}\left(c^{2}-b^{2}\right)}}{\frac{m_{2}+1}{m_{2} E_{2}}+\frac{\left(m_{1}-1\right) c^{2}+\left(m_{1}+1\right) b^{2}}{m_{1} E_{1}\left(c^{2}-b^{2}\right)}} . \tag{2.21}
\end{equation*}
$$



Figure 2.12 Tunnel Section With Concrete Liner

### 2.6.3. Stress Distribution due to Gravity Around Circular Tunnels

Herget (1988) gives the solution for stress distribution due to gravity around circular tunnels. There are depicted in figure 2.13 and 2.14.


Figure 2.13 Radial and Tangential Stress for a Circular Opening Subjected to Uniaxial stress(after Herget, 1988)


Figure 2.14 Tangential Stress For $k=0,0.33 \& 1$ (after Herget, 1988)

## CHAPTER 03

## PROBLEM GEOMETRY AND FINITE ELEMENT IDEALASATION

### 3.1 Tunnel Shapes and Geometry

As discussed in chapter two there are various types of tunnel shapes used in the world depending on their practical usage, geotechnical conditions, technology available and the financial resources.

For this research, three elliptical tunnel with different $a / b$ values have been considered, where $\mathrm{a}=$ major radius and $\mathrm{b}=$ minor radius of the elliptical tunnel opening, as depicted in figure 3.1. These three tunnel geometries are as follows.

1. Elliptical tunnel $-\mathrm{a} / \mathrm{b}=1.156$
2. Elliptical tunnel $-\mathrm{a} / \mathrm{b}=1.358$
3. Elliptical tunnel $-\mathrm{a} / \mathrm{b}=1.500$


Figure 3.1 Elliptical tunnel geometry

The above values are based on actual tunnel dimensions used in practice in Sri Lanka for hydro-electric power projects. The three different tunnel shapes and the rock domain surrounding them considered for the finite element analysis here are as shown in figures 3.2, 3.3 and 3.4 .

$a / b=1.156$
No. of Nodes $=253$
No. of Elements $=230$

Figure 3.2. Elliptical Tunnel With $\mathrm{a} / \mathrm{b}=1.156$

$a / b=1.358$
No. of Nodes - 200
No. of Elements - 190

Figure 3.3. Elliptical Tunnel With $\mathrm{a} / \mathrm{b}=1.358$


Figure 3.4. Elliptical Tunnel With $a / b=1.500$

### 3.2. Concrete Lining

As discussed in Chapter 2, there are various types of linings used in tunnel construction (locally and in other countries)

In this research only concrete linings are considered. The discretized finite element domain for one of the tunnels, after the introduction of concrete liners, is shown in figure 3.5. The liner thickness is varied from 0.0 m (unlined case) to 1.0 m , in steps of 0.2 m .


Figure 3.5 Finite element discretisation of the rock domain, after the introduction of the concrete liner.

### 3.3. Material Properties

In this research, only two types of materials were assumed, these being rock and concrete.

The constitutive behavior of rock domain and concrete in liners are assumed to be according to isotropic linear elasticity. Thus the Young's Modulii of concrete and rock are denoted by $\mathrm{E}_{\mathrm{c}}$ and $\mathrm{E}_{\mathrm{r}}$, respectively, and Poisson's ratio of concrete and rock are denoted by $\nu_{c}$ and $\nu_{r}$, respectively.

The effect of liner thickness on the stress and deformation behavior inside the rock surrounding the three elliptical tunnel geometries was first investigated for a fixed moduli ratio $\mathrm{E}_{\mathrm{c}} / \mathrm{E}_{\mathrm{r}}$ of 10.0 . The material properties selected to represent the assumed behavior of rock and concrete for the above analyses are as given in table 3.1(Rock properties after Selvadurai, 1979):

Table 3.1

| Material | Young's Modulus E (kN/m | Poisson's Ratio $\boldsymbol{v}$ |
| :---: | :---: | :---: |
| Rock | $0.21 \times 10^{7}$ | 0.30 |
| Concrete | $0.21 \times 10^{8}$ | 0.20 |

In order to investigate the effect of varying rock stiffness on the stress and deformation inside rock material, the Young's Modulus of rock material was then varied such that a realistic range of $E_{c} / E_{r}$ ratios (varying from 5 to 100) was obtained.

### 3.4. Finite Element Programme

The analysis for this work is carried out by using the finite element analysis program (FEAP) originally developed by Professor R.L. Traylor, University of Berkely, California (Zienkiewiz,1977). The program was later expanded at the Asian Institute of Technology by Professor Worsak Kanok Nukulchai (1984). This program was modified and installed in a pentium micro-computer with 16 MB of RAM (Random Access Memory ) at University of Moratuwa by Dr. U.G.A. Puswewala.

The program FEAP can be utilized to solve one, two and three dimentional finite element analysis problems which may be linear or non-liner. With appropriate modification it can be upgraded to solve transient problems.

The program is written in FORTRAN computer language; it follows a modular concept, by which flexibility to change or modify various modules of the program without affecting the rest of the program is allowed. This enables users to incorporate various additional features in the program in the form of new algorithms or element subroutines. Another feature of the program is the Macro programming language; under this, the various stages of a finite element analysis are performed by specifying a series of Macro commands. Each Macro command instructs the program to access a certain set of subroutines in order to perform a certain task.

The program can be basically divided into three parts as main program, system sub-routines and the element subroutine library. Main program controls the overall memory allocation and the start and end of the analysis. System sub-routine constitute the body of the finite element algorithms, and control the input (data) and the output (results of the program). Element subroutine library contains a number of element subroutines, each subroutine for a specific type of finite element. This arrangement allows the users to write their own element subroutines to solve their specific programs.

### 3.5. Finite Element Discretisation

The typical finite element meshes are shown in figure 3.6(elliptical tunnel with $\mathrm{a} / \mathrm{b}$ $=1.156)$ figure $3.7(\mathrm{a} / \mathrm{b}=1.358)$ and figure $3.8(\mathrm{a} / \mathrm{b}=1.500)$ respectively. Four noded finite elements were used to discretise the material domains. Memory limitations of the personal computer used to analyse these problems meant that meshes could not be made much finer than shown in figures $3.6,3.7$ or 3.8 .


Figure 3.6 Finite element mesh for elliptical tunnel with $a / b=1.156$


Figure 3.7 Finite element mesh for elliptical tunnel with $\mathrm{a} / \mathrm{b}=1.358$


Figure 3.8 Finite element mesh for elliptical tunnel with $a / b=1.500$

### 3.6. Boundary Conditions and Loadings

### 3.6.1. Loading Conditions

The loads in the domain are

1. Gravity Force
2. Fluid Pressure

Gravity force is not considered here. It is assumed that the rock domain has reached equilibrium under gravity, before the application of the hydraulic loading inside the tunnel.

Fluid pressure acts perpendicular to the surface of the openings. Equivalent nodal forces were computed and input into the computer program. Figure 3.9 shows the application of hydraulic pressure at nodal points


Figure 3.6 Tunnel section after introduction of fluid pressure

### 3.6.2. Boundary Conditions

Figure 3.10 shows the boundary conditions used for the analysis.


Figure 3.10 Tunnel Section With Boundary Conditions
AB- " $y$ " Displacement is Fixed (line of symmetry)
BC- " $x$ " and " $y$ " Displacements are Fixed (the far boundary)
CD- "x" Displacement is Fixed (line of symmetry)
DA- " $x$ " and " $y$ " Displacements are Free (loading surface)

### 3.7. Verification of Finite Element Programme Using a Circular Tunnel

Analytical solution for a lined tunnel of a circular cross-section is given by Jaeger(1979). The finite element program FEAP was used to simulate a problem including circular tunnel geometry of selected dimension and parameter, and the comparison of numerical results from FEAP with analytical result of Jaeger(1979) is given in Appendix A.

## CHAPTER 4.0

## RESULTS FOR ELLIPTICAL TUNNEL $\mathbf{a} / \mathrm{b}=1.156$

### 4.1. Influence of Liner Thickness on Stress and Deformation in Rock Around Tunnel

Principal stresses were investigated along three radial lines $\mathrm{AB}, \mathrm{CD}$ and EF , shown in figure 4.1 radiating from the center of the tunnel. For the tunnel with $a / b=1.156$, variation of the major principal stress along the radial line $A B$ for different liner thicknesses is shown in figure 4.2, and the variation of the minor principal stress along the same line for different liner thicknesses is shown in figure 4.5. Corresponding results for the same tunnel along line CD are shown in figures 4.3 and 4.6, respectively. Figures 4.4 and 4.7 respectively, show the corresponding results for the same tunnel along line EF.

Figure 4.8 shows the circumferential line considered for analysis. Figure 4.9 shows the variation of major principal stress along an elliptical (circumferential) line of a shape similar to that of the tunnel opening, but at some distance inside the rock mass from the tunnel face, as the liner thickness is varied, for the tunnel with $a / b=1.156$. The circumferential line along which the stresses shown in figure 4.9 are evaluated is similar to the line GH shown on figure 4.8 . Morman srilank

For the elliptical tunnel with $a / b=1.156$, influence of the concrete liner thickness on displacement at points inside the rock mass are illustrated by figures 4.10 and 4.11 . figures 4.10 and 4.11 show displacements at points inside the rock mass located along an elliptical (circumferential) line GH, which is shown on the scaled diagram of 4.8.

Figure $4.2,4.3 \& 4.4$ show the variation of major principal stress along radical line $\mathrm{AB}, \mathrm{CD} \& E F$ respectively.

In the case of line AB (figure 4.2), for the tunnel $\mathrm{a} / \mathrm{b}=1.156$ major principal stress at a point inside the rock(element number 5 l ) when there is no lining, which is 420.9 kPa decreases by $18.34 \%$ when a liner of thickness of 0.2 m is introduced. The corresponding reductions are $35.64 \%$ for a liner thickness of 0.4 m thickness and $58.97 \%$ for a liner of 1.0 m .

In the case of line $C D$ (figure 4.3 ), for the tunnel $a / b=1.156$ major principal stress at a point inside the rock(element 56 ) reduce by $31.51 \%$ when a liner of thickness of 0.2 m is introduced as compared to the stresses in the case of unlined tunnel. The corresponding reductions are $45.56 \%$ for a liner thickness of 0.4 m thickness and $59.43 \%$ for a liner of 1.0 m .

In the case of line EF (figure 4.4), for the tunnel $a / b=1.156$ major principal stress at a point inside the rock(element number 60) reduce by $40.10 \%$ when a liner of thickness of 0.2 m is introduced as compared to the stresses in the case of unlined tunnel. The corresponding reductions are $54.33 \%$ for a liner thickness of 0.4 m thickness and $73.75 \%$ for a liner of 1.0 m .

The numerical results and the comparison of figures $4.2,4.3 \& 4.4$ show that the line EF is the critical line along which maximum principal tensile stresses occurred.

Figures 4.5, 4.6 and 4.7 show the influence of concrete liner thickness on the compressive principal stress around the tunnel with $a / b=1.156$. According to figure 4.5 , the minor principal stress at a point inside the rock closure to point A reduces by $28.13 \%$ when a 0.2 m thick concrete is introduced to the originally unlined tunnel; this reduction is 39.73 for a 0.4 m thick liner and $52.32 \%$ for a 1.0 m thick liner. Figure 4.6 shows similar behavior of the minor principal stress along the line CD. Figure 4.7 shows that large percentage stress reductions occur in the case of the minor principal stress along line EF. This stress reduces at a point inside the rock closure to point E by $57.70 \%$ when a 0.2 m thick liner is introduced to the unlined tunnel; the corresponding reduction is $79.25 \%$ for a 0.4 m thick liner, and $98.46 \%$ for a 1.0 m thick liner.

Figures $4.9 \& 4.10$ shows the variation of major principal stress and minor principal stress along circumferential line GH respectively, which is in rock.

The major principal stress reduction is $18.34 \%$ when 0.2 m liner is introduced as compared to the stress in the case of unlined tunnel closure to point $A$ (Element number 51 ). Where as reduction is $35.64 \%$ at point closure to $E$ when 0.2 m liner is introduced as compared to the stress in the case of an unlined tunnel.

Figure 4.10 shows the minor principal stress variation along line GH. It also shows the same pattern of reduction as in the major principal stress mentioned above.

According to the results in figures 4.11 and 4.12 the percentage reduction of $x$ displacement and $y$-displacement over the rock domain varies with the location. Figure 4.11 shows relatively large percentage reductions in the $x$-displacement at the $x$-axis as the tunnel liner thickness is increased (this is $40.01 \%$ when a 0.2 m thick liner is introduced on the unlined tunnel; and about $83.86 \%$ for a 1.0 m thick liner).

Figures 4.13.4.14 \& 4.15 are shows the variation of major principal stress with the introduction of concrete liner on three elements close to point $A, C$ \& E respectively.


Figure 4.1 Radial lines (For elliptical tunnel- $1, \mathrm{a} / \mathrm{b}=1.156$ )


Figure 4.2 Variation of major principal stress along radial line "AB"
(For elliptical tunnel-1, $\mathrm{a} / \mathrm{b}=1.156$ )

VARIATION OF MAJOR PRINCIPAL STRESS ALONG RADIAL LINE "AB" (FOR ELLIPTICAL TUNNEL-2, $a / b=1.156$ )

| ELEMENT NUMBER | MAJOR PRINCIPAL STRESS $\times 10^{3}\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  | LINER ELEMENTS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS (m) |  |  |  |  |  |  |
|  | $t=0.0$ | $t=0.2$ | $t=0.4$ | $t=0.6$ | $t=0.8$ | $t=1.0$ |  |
| 1 | 0.4999 | 6.4820 | 4.8740 | 3.1910 | 3.1850 | 2.7730 |  |
| 11 | 0.4914 | 0.4568 | 4.8580 | 3.1370 | 0.3169 | 2.7840 |  |
| 21 | 0.4712 | 0.4169 | 0.3281 | 3.0140 | 3.1270 | 2.7600 |  |
| 31 | 0.3836 | 0.3352 | 0.2639 | 0.1520 | 2.5560 | 2.1630 |  |
| 41 | 0.4457 | 0.3678 | 0.2689 | 0.1946 | 0.2065 | 2.6790 |  |
| 51 | 0.4209 | 0.3437 | 0.2709 | 0.1840 | 0.1910 | 0.1727 |  |
| 61 | 0.3690 | 0.2874 | 0.2256 | 0.1603 | 0.1623 | 0.1496 |  |
| 71 | 0.3099 | 0.2315 | 0.1824 | 0.1335 | 0.1326 | 0.1220 |  |
| 81 | 0.2526 | 0.1835 | 0.1446 | 0.1083 | 0.1059 | 0.0972 |  |
| 91 | 0.2115 | 0.1510 | rMor01191 | mia 0.0907 | 0.0878 | 0.0850 |  |
| 101 | 0.1770 | 0.1250 | hese 0.0987 | - 0.0761 | 0.0731 | 0.0669 |  |
| 111 | 0.1140 | 0.1008 | 0.0798 | 0.0621 | 0.0593 | 0.0543 |  |
| 121 | 0.1107 | 0.0769 | 0.0610 | 0.0480 | 0.0455 | 0.0417 |  |
| 131 | 0.0804 | 0.0555 | 0.0441 | 0.0351 | 0.0331 | 0.0303 |  |
| 141 | 0.0565 | 0.0383 | 0.0310 | 0.0249 | 0.0234 | 0.0214 |  |
| 151 | 0.0387 | 0.0265 | 0.0212 | 0.0712 | 0.0161 | 0.0148 |  |
| 161 | 0.0253 | 0.0173 | 0.0139 | 0.0114 | 0.0107 | 0.0098 |  |
| 171 | 0.0159 | 0.0109 | 0.0088 | 0.0073 | 0.0068 | 0.0062 |  |
| 181 | 0.0092 | 0.0063 | 0.0051 | 0.0043 | 0.0040 | 0.0037 |  |
| 191 | 0.0039 | 0.0027 | 0.0022 | 0.0018 | 0.0017 | 0.0016 |  |
| 201 | 0.0010 | 0.0007 | 0.0005 | 0.0003 | 0.0002 | 0.0002 |  |
| 211 | 0.0020 | -0.0139 | -0.0011 | -0.0008 | -0.0007 | -0.0007 |  |

Table 4.1


## VARIATION OF MAJOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" (FOR ELLIPTICAL TUNNEL-2, $a / b=1.156$ )

| ELEMENT NUMBER | MAJOR PRINCIPAL STRESS $\times 10^{3}\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS (m) |  |  |  |  |  |
|  | $t=0.0$ | $t=0.2$ | $t=0.4$ | $t=0.6$ | $t=0.8$ | $\mathrm{t}=1.0$ |
| 6 | 0.8419 | 7.8140 | 5.5030 | 4.0300 | 3.6300 | 3.1300 |
| 16 | 0.8378 | 0.5621 | 5.0482 | 4.2230 | 3.7690 | 3.2830 |
| 26 | 0.7772 | 0.5275 | 0.3975 | 4.3780 | 3.8920 | 3.4350 |
| 36 | 0.7279 | 0.4909 | 0.3830 | 0.3350 | 3.9210 | 3.5120 |
| 46 | 0.7105 | 0.4805 | 0.3802 | 0.3296 | 0.2938 | 3.7070 |
| 56 | 0.6402 | 0.4385 | 0.3485 | 0.2936 | 0.2678 | 0.2597 |
| 66 | 0.5236 | 0.3593 | 0.2893 | 0.2390 | 0.2219 | 0.2079 |
| 76 | 0.4089 | 0.2818 | 0.2273 | 0.1687 | 0.1741 | 0.1610 |
| 86 | 0.3174 | 02191 | 0.1767 | 0.1447 | 0.1349 | 0.1243 |
| 96 | 0.2519 | U0.1740 | Mor 0.1401 | 0.1146 | 0.1067 | 0.0981 |
| 106 | 0.2004 | E01381 | - $\cos ^{2} 0.1110$ | 0.0906 | 0.0843 | 0.0773 |
| 116 | 0.1677 | 0.1158 | 0.0931 | 0.0760 | 0.0707 | 0.0659 |
| 126 | 0.1169 | 0.0802 | 0.0644 | 0.0527 | 0.0489 | 0.0448 |
| 136 | 0.0830 | 0.0570 | 0.0457 | 0.0372 | 0.0345 | 0.0316 |
| 146 | 0.0055 | 0.0377 | 0.0302 | 0.0245 | 0.0227 | 0.0208 |
| 156 | 0.0359 | 0.0246 | 0.0169 | 0.0159 | 0.0147 | 0.0134 |
| 166 | 0.0218 | 0.0149 | 0.0118 | 0.0095 | 0.0088 | 0.0080 |
| 176 | 0.0128 | 0.0088 | 0.0069 | 0.0055 | 0.0051 | 0.0046 |
| 186 | 0.0070 | 0.0048 | 0.0037 | 0.0029 | 0.0027 | 0.0024 |
| 196 | 0.0021 | 0.0015 | 0.0011 | 0.0008 | 0.0008 | 0.0006 |
| 206 | -0.0013 | -0.0009 | -0.0007 | -0.0006 | 0.0005 | -0.0005 |
| 216 | -0.0033 | -0.0022 | -0.0017 | -0.0132 | -0.0120 | -0.0011 |

Table 4.2


Figure 4.4 Variation of major principal stress along radial line "EF"
(For elliptical tunnel- $1, \mathrm{a} / \mathrm{b}=1.156$ )

VARIATION OF MAJOR PRINCIPAL STRESS ALONG RADIAL LINE "EF" (FOR ELLIPTICAL TUNNEL-2, $a / b=1.156$ )

| ELEMENT NUMBER | MAJOR PRINCIPAL STRESS $\times 10^{3}\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS (m) |  |  |  |  |  |
|  | $t=0.0$ | $t=0.2$ | $t=0.4$ | $t=0.6$ | $t=0.8$ | $t=1.0$ |
| 10 | 1.6050 | 10.9200 | 8.7150 | 7.6750 | 6.8050 | 6.2020 |
| 20 | 1.3960 | 0.8186 | 6.7370 | 6.0250 | 5.4390 | 5.0240 |
| 30 | 1.2270 | 0.7210 | 0.5380 | 4.5710 | 4.2910 | 4.0600 |
| 40 | 1.0890 | 0.6421 | 0.4820 | 0.3916 | 3.1970 | 3.1770 |
| 50 | 0.9618 | 0.5747 | 0.4374 | 0.3611 | 0.2994 | 2.3540 |
| 60 | 0.8195 | 0.4909 | 0.3743 | 0.3095 | 0.2584 | 0.2151 |
| 70 | 0.6184 | 0.3766 | 0.2905 | 0.2416 | 0.2071 | 0.1786 |
| 80 | 0.4464 | 0.2768 | 0.2151 | 0.1786 | 0.1563 | 0.1378 |
| 90 | 0.3275 | 0.2067 | Mor 011615 | 0.1334 | 0.1184 | 0.1056 |
| 100 | 0.2530 | 0.1619 | cill 0.1268 | 0.1043 | 0.0933 | 0.0837 |
| 110 | 0.1992 | 0.1289 | 0.1011 | 0.0828 | 0.0746 | 0.0671 |
| 120 | 0.1535 | 0.1002 | 0.0786 | 0.0640 | 0.0579 | 0.0522 |
| 130 | 0.1104 | 0.0727 | 0.0571 | 0.0462 | 0.0420 | 0.0379 |
| 140 | 0.0761 | 0.0505 | 0.0396 | 0.0318 | 0.0290 | 0.0262 |
| 150 | 0.0502 | 0.0335 | 0.0262 | 0.0208 | 0.0191 | 0.0172 |
| 160 | 0.0319 | 0.0213 | 0.0166 | 0.0131 | 0.0120 | 0.0101 |
| 170 | 0.0191 | 0.0128 | 0.0099 | 0.0077 | 0.0070 | 0.0063 |
| 180 | 0.0108 | 0.0073 | 0.0055 | 0.0042 | 0.0038 | 0.0034 |
| 190 | 0.0056 | 0.0038 | 0.0028 | 0.0021 | 0.0019 | 0.0016 |
| 200 | 0.0011 | 0.0077 | 0.0005 | 0.0003 | 0.0002 | 0.0002 |
| 210 | -0.0020 | -0.0014 | -0.0012 | -0.0008 | -0.0008 | -0.0007 |
| 220 | -0.0027 | -0.0013 | -0.0013 | -0.0010 | -0.0009 | -0.0008 |

Table 4.3


Figure 4.5 Variation of minor principal stress along radial line " $A B$ " (For elliptical tunnel-1, $\mathrm{a} / \mathrm{b}=1.156$ )

VARIATION OF MINOR PRINCIPAL STRESS ALONG RADIAL LINE "AB" (FOR ELLIPTICAL TUNNEL-2, $\mathrm{a} / \mathrm{b}=1.156$ )

| ELEMENT NUMBER | MINOR PRINCIPALSTRESS $\times\left(-1 \times 10^{3}\right)\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 1 | 0.8843 | 0.8716 | 0.8697 | 0.8689 | 0.8707 | 0.8814 |
| 11 | 0.8352 | 0.6426 | 0.5798 | 0.6831 | 0.6743 | 0.7003 |
| 21 | 0.7821 | 0.5850 | 0.4900 | 0.4866 | 0.4657 | 0.5221 |
| 31 | 1.0440 | 0.7785 | 0.6427 | 0.5610 | 0.1633 | 1.7720 |
| 41 | 0.7503 | 0.5492 | 0.4606 | 0.3721 | 0.3744 | 0.4381 |
| 51 | 0.6872 | 0.4939 | 0.4142 | 0.3404 | 0.3388 | 0.3276 |
| 61 | 0.5891 | 0.4206 | 0.3530 | 0.2957 | 0.2909 | 0.2790 |
| 71 | 0.4951 | 0.3415 | 0.2896 | 0.2442 | 0.2375 | 0.2263 |
| 81 | 0.4086 | 0.2788 | 0.2346 | 0.2021 | 0.1948 | 0.1850 |
| 91 | 0.3426 | 0.2327 | 0.1960 | 0.1701 | 0.1629 | 0.1544 |
| 101 | 0.2923 | 0.1981 | 0.1671 | 0.1457 | 0.1389 | 0.1314 |
| 111 | 0.2423 | 0.1639 | 0.1384 | 0.1212 | 0.1150 | 0.1087 |
| 121 | 0.1907 | 0.1296 | 0.1096 | 0.0963 | 0.0909 | 0.0858 |
| 131 | 0.1480 | 0.1001 | 0.0847 | 0.0746 | 0.0702 | 0.0661 |
| 141 | 0.1134 | 0.0767 | 0.0649 | 0.0572 | 0.0537 | 0.0505 |
| 151 | 0.0881 | 0.0596 | 0.0504 | 0.0444 | 0.0416 | 0.0391 |
| 161 | 0.0697 | 0.0472 | 0.0399 | 0.0351 | 0.0329 | 0.0308 |
| 171 | 0.0573 | 0.0388 | 0.0328 | 0.0288 | 0.0269 | 0.0253 |
| 181 | 0.0492 | 0.0334 | 0.0281 | 0.0247 | 0.0231 | 0.0216 |
| 191 | 0.0435 | 0.0295 | 0.0249 | 0.0281 | 0.0204 | 0.0192 |
| 200 | 0.0171 | 0.0117 | 0.0082 | 0.0526 | 0.0048 | 0.0396 |
| 210 | 0.0143 | 0.0098 | 0.0070 | 0.0046 | 0.0042 | 0.0035 |

Table 4.4


No. of Nodes $=253$
No. of Elements $=230$

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SCAL $1 \mathrm{~cm}: 143 \mathrm{kN} / \mathrm{m}^{\wedge} 2$

Figure 4.6 Variation of minor principal stress along radial line "CD" (For elliptical tunnel-1, $\mathrm{a} / \mathrm{b}=1.156$ )

VARIATION OF MINOR PRINCIPAL STRESS ALONG RADIAL LINE "CD"
(FOR ELLIPTICAL TUNNEL-2, $a / b=1.156$ )

| ELEMENT NUMBER | MINOR PRINCIPAL STRESS $\times\left(-1 \times 10^{3}\right)\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS (m) |  |  |  |  |  |
|  | $t=0.0$ | $t=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $t=0.8$ | $t=1.0$ |
| 6 | 1.0850 | 0.7854 | 0.8850 | 0.9362 | 0.9583 | 0.9813 |
| 16 | 0.9754 | 0.7463 | 0.7886 | 0.8078 | 0.8300 | 0.8445 |
| 26 | 0.8958 | 0.6783 | 0.5752 | 0.5255 | 0.5930 | 0.6218 |
| 36 | 0.8535 | 0.6600 | 0.5525 | 0.4731 | 0.5859 | 0.5866 |
| 46 | 0.7975 | 0.6058 | 0.5114 | 0.4286 | 0.3897 | 0.3768 |
| 56 | 0.7122 | 0.5381 | 0.4502 | 0.3748 | 0.3426 | 0.3126 |
| 66 | 0.5767 | 0.4319 | 0.3581 | 0.2949 | 0.2715 | 0.2461 |
| 76 | 0.4425 | 0.3268 | 0.2683 | 0.2191 | 0.2024 | 0.1836 |
| 86 | 0.3437 | 0.2506 | 0.2041 | 0.1657 | 0.1531 | 0.1388 |
| 96 | 0.2738 | 0.1973 | Mor 0.1597 | 0.1290 | 0.1192 | 0.1081 |
| 106 | 0.2246 | 0.1604 | cse 0.1292 | 0.1041 | 0.0962 | 0.0872 |
| 116 | 0.1746 | 0.1234 | 0.0983 | 0.0784 | 0.0723 | 0.0653 |
| 126 | 0.1440 | 0.1013 | 0.0810 | 0.0656 | 0.0601 | 0.0545 |
| 136 | 0.1033 | 0.0719 | 0.0571 | 0.0456 | 0.0421 | 0.0381 |
| 146 | 0.0780 | 0.0540 | 0.0428 | 0.0341 | 0.0316 | 0.0386 |
| 156 | 0.0591 | 0.0407 | 0.0322 | 0.0256 | 0.0237 | 0.0214 |
| 166 | 0.0460 | 0.0316 | 0.0249 | 0.0197 | 0.0183 | 0.0165 |
| 176 | 0.0372 | 0.0255 | 0.0200 | 0.0158 | 0.0146 | 0.0132 |
| 186 | 0.0315 | 0.0215 | 0.0169 | 0.0133 | 0.0123 | 0.0112 |
| 196 | 0.0264 | 0.0181 | 0.0141 | 0.0122 | 0.0103 | 0.0931 |
| 206 | 0.0225 | 0.0154 | 0.0121 | 0.0951 | 0.0088 | -0.0080 |
| 216 | 0.0204 | 0.0139 | 0.0109 | 0.0864 | 0.0080 | -0.0072 |

Table 4.5


Figure 4.7 Variation of minor principal stress along radial line "EF" (For elliptical tunnel-1, $a / b=1.156$ )

VARIATION OF MINOR PRINCIPAL STRESS ALONG RADIAL LINE "EF" (FOR ELLIPTICAL TUNNEL-2, $a / b=1.156$ )

| ELEMENT NUMBER | MINOR PRINCIPAL STRESS $\times\left(-1 \times 10^{3}\right)\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 10 | 1.0210 | 0.4374 | 0.5375 | 0.6097 | 0.6674 | 0.7094 |
| 20 | 0.8463 | 0.2934 | 0.2371 | 0.3445 | 0.4156 | 0.4606 |
| 30 | 0.7394 | 0.2694 | 0.1086 | 0.1534 | 0.2413 | 0.2936 |
| 40 | 0.6619 | 0.2518 | 0.1086 | 0.0417 | 0.1270 | 0.1858 |
| 50 | 0.6055 | 0.2359 | 0.1040 | 0.0405 | 0.0177 | 0.0136 |
| 60 | 0.4984 | 0.2108 | 0.1034 | 0.0456 | 0.0241 | 0.0077 |
| 70 | 0.3824 | 0.1761 | 0.0927 | 0.0437 | 0.0279 | 0.0116 |
| 80 | 0.2787 | 0.1424 | 0.0810 | 0.0412 | 0.0304 | 0.0182 |
| 90 | 0.2092 | 0.1151 | 0.0684 | 0.0358 | 0.0282 | 0.0188 |
| 100 | 0.1653 | 0.0955 | 0.0582 | 0.0309 | 0.0252 | 0.0176 |
| 110 | 0.1339 | 0.0802 | 0.0498 | 0.0267 | 0.0223 | 0.0159 |
| 120 | 0.1071 | 0.0662 | 0.0419 | 0.0227 | 0.0193 | 0.0141 |
| 130 | 0.0819 | 0.0521 | 0.0334 | 0.0183 | 0.0158 | 0.0117 |
| 140 | 0.0621 | 0.0405 | 0.0264 | 0.0147 | 0.0129 | 0.0097 |
| 150 | 0.0470 | 0.0312 | 0.0206 | 0.0116 | 0.0103 | 0.0079 |
| 160 | 0.0363 | 0.0244 | 0.0163 | 0.0094 | 0.0084 | 0.0065 |
| 170 | 0.0288 | 0.0195 | 0.0132 | 0.0078 | 0.0067 | 0.0055 |
| 180 | 0.0238 | 0.0262 | 0.0111 | 0.0067 | 0.0061 | 0.0049 |
| 190 | 0.0205 | 0.0140 | 0.0097 | 0.0060 | 0.0054 | 0.0044 |
| 200 | 0.0171 | 0.0117 | 0.0082 | 0.0053 | 0.0048 | 0.0040 |
| 210 | 0.0143 | 0.0098 | 0.0070 | 0.0046 | 0.0042 | 0.0035 |
| 220 | 0.0122 | 0.0083 | 0.0060 | 0.0040 | 0.0037 | 0.0031 |

Table 4.6


Figure 4.8 Circumferential lines (For elliptical tunnel- $1, \mathrm{a} / \mathrm{b}=1.156$ )


Figure 4.9 Variation of major principal stress along circumferential line " GH "
(For elliptical tunnel- $1, \mathrm{a} / \mathrm{b}=1.156$ )

VARIATION OF MAJOR PRINCIPAL STRESS ALONG CIRCUMFERENTIAL LINE "GH" (FOR ELLIPTICAL TUNNEL-2, $a / b=1.156$ )

| ELEMENT NUMBER | MAJOR PRINCIPAL STRESS $\times 10^{3}\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 51 | 0.4209 | 0.3437 | 0.2709 | 0.1840 | 0.1910 | 0.1727 |
| 52 | 0.4359 | 0.3443 | 0.2718 | 0.1929 | 0.1948 | 0.1867 |
| 53 | 0.4718 | 0.3517 | 0.2729 | 0.2027 | 0.2068 | 0.1916 |
| 54 | 0.5152 | 0.3681 | 0.2886 | 0.2128 | 0.2161 | 0.1876 |
| 55 | 0.5652 | 0.3945 | 0.3087 | 0.2409 | 0.2290 | 0.2060 |
| 56 | 0.6402 | 0.4358 | 0.3485 | 0.2936 | 0.2678 | 0.2597 |
| 57 | 0.7318 | 0.4730 | 0.3908 | 0.3385 | 0.3091 | 0.2980 |
| 58 | 0.7764 | 0.5081 | 0.4217 | 0.3684 | 0.3376 | 0.3072 |
| 59 | 0.8105 | 0.5115 | 0.4103 | 0.3557 | 0.3188 | 0.3065 |
| 60 | 0.8195 | 0.4909 | 0.3743 | 0.3095 | 0.2584 | 0.2151 |

"Table 4.7


Figure 4.10 Variation of minor principal stress along circumferential line "GH" (For elliptical tunnel-1, $\mathrm{a} / \mathrm{b}=1.156$ )

| ELEMENT NUMBER | MINOR PRINCIPAL STRESS $\left(-1 \times 10^{3}\right)\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 51 | 0.6872 | 0.4939 | 0.4142 | 0.3404 | 0.3388 | 0.3276 |
| 52 | 0.6945 | 0.4925 | 0.4123 | 0.3412 | 0.3379 | 0.3174 |
| 53 | 0.6922 | 0.4835 | 0.4019 | 0.3313 | 0.3298 | 0.3134 |
| 54 | 0.6779 | 0.4897 | 0.4060 | 0.3421 | 0.3355 | 0.3162 |
| 55 | 0.7084 | 0.5081 | 0.4272 | 0.3603 | 0.3427 | 0.3174 |
| 56 | 0.7122 | 0.5381 | 0.4504 | 0.3748 | 0.3426 | 0.3126 |
| 57 | 0.7030 | 0.5350 | 0.4368 | 0.3598 | 0.3187 | 0.2899 |
| 58 | 0.6452 | 0.4558 | 0.3568 | 0.2835 | 0.2454 | 0.2244 |
| 59 | 0.5732 | 0.3336 | 0.2311 | 0.1663 | 0.1399 | 0.1139 |
| 60 | 0.4984 | 0.2108 | 0.1034 | 0.0456 | 0.0241 | 0.0077 |

Table 4.8


Figure 4.11 Variation of " $x$ " displacement along circumferential line " GH " (For elliptical tunnel-1, $\mathrm{a} / \mathrm{b}=1.156$ )

VARIATION OF "X' DISPLACEMENT ALONG CIRCUMFERENTIAL LINE "GH" (FOR ELLIPTICAL TUNNEL-2, $\mathrm{a} / \mathrm{b}=1.156$ )

| NODE NUMBER | "X' DISPLACEMENT $\times 10^{-3}(\mathrm{~m})$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $t=0.0$ | $t=0.2$ | $t=0.4$ | $t=0.6$ | $t=0.8$ | $t=1.0$ |
| 67 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 68 | 0.2452 | 0.1895 | 0.1518 | 0.1111 | 0.1124 | 0.1047 |
| 69 | 0.4907 | 0.3751 | 0.2996 | 0.2202 | 0.2216 | 0.2052 |
| 70 | 0.7205 | 0.5434 | 0.4316 | 0.3184 | 0.3182 | 0.2935 |
| 71 | 0.9324 | 0.6986 | 0.5518 | 0.4082 | 0.4026 | 0.3660 |
| 72 | 1.1340 | 0.8465 | 0.6036 | 0.4889 | 0.4712 | 0.4221 |
| 73 | 1.3180 | 0.9735 | 0.7500 | 0.5482 | 0.5124 | 0.4525 |
| 74 | 1.4360 | 1.0220 | 0.7646 | 0.5472 | 0.4964 | 0.4324 |
| 75 | 1.4690 | 0.9851 | 0.7061 | 0.4838 | 0.4290 | 0.3606 |
| 76 | 1.4560 | 0.9032 | 0.6101 | 0.3897 | 0.3376 | 0.2702 |
| 77 | 1.4240 | 0.8542 | 0.5615 | 0.3446 | 0.2951 | 0.2299 |

Table 4.9


Figure 4.12 Variation of " y " displacement along circumferential line " GH " (For elliptical tunnel-1, $\mathrm{a} / \mathrm{b}=1.156$ )

VARIATION OF "Y' DISPLACEMENT ALONG CIRCUMFERENTIAL LINE "GH" (FOR ELLIPTICAL TUNNEL-2, $a / b=1.156$ )

| NODE NUMBER | "Y" DISPLACEMENT $\times 10^{-3}(\mathrm{~m})$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $t=0.0$ | $t=0.2$ | $t=0.4$ | $t=0.6$ | $t=0.8$ | $t=1.0$ |
| 67 | 2.5480 | 1.7460 | 1.4630 | 1.2560 | 1.1970 | 1.1300 |
| 68 | 2.5330 | 1.7330 | 1.4510 | 1.2480 | 1.1860 | 1.1160 |
| 69 | 2.4210 | 1.6730 | 1.3980 | 1.2030 | 1.1390 | 1.0670 |
| 70 | 2.3100 | 1.5790 | 1.3120 | 1.1320 | 1.0630 | 0.9944 |
| 71 | 2.1370 | 1.4570 | 2130 | 1.0490 | 0.9730 | 0.9041 |
| 72 | 1.9110 | 1.3040 | 1.0810 | 0.9321 | 0.8498 | 0.7823 |
| 73 | 1.6230 | 1.0980 | 0.8987 | 0.7705 | 0.9880 | 0.9238 |
| 74 | 1.2450 | 0.8178 | 0.6533 | 0.5525 | 0.4821 | 0.4293 |
| 75 | 0.8410 | 0.5256 | 0.4060 | 0.3358 | 0.2863 | 0.2464 |
| 76 | 0.3936 | 0.2303 | 0.1706 | 0.1370 | 0.1136 | 0.9314 |
| 77 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |

Table 4.10


Figure 4.13 Variation of major principal stress with liner thickness (For element number 51)

| LINER THICKNESS $(\mathrm{m})$ | STRESS $\times 10^{3} \mathrm{kN} / \mathrm{m}^{2}$ |
| :---: | :---: |
| 0.00 | 0.4209 |
| 0.20 | 0.3437 |
| 0.40 | 0.2709 |
| 0.60 | 0.1840 |
| 0.80 | 0.1910 |
| 1.00 | 0.1727 |

Table 4.11


Figure 4.14 Variation of major principal stress with liner thickness (For element number 56)

| LINER THICKNESS $(\mathrm{m})$ | STRESS $\times 10^{3} \mathrm{kN} / \mathrm{m}^{2}$ |
| :---: | :---: |
| 0.00 | 0.6402 |
| 0.20 | 0.4385 |
| 0.40 | 0.3485 |
| 0.60 | 0.2936 |
| 0.80 | 0.2678 |
| 1.00 | 0.2597 |

Table 4.12


Figure 4.15 Variation of major principal stress with liner thickness (For element number 60)

| LINER THICKNESS $(\mathrm{m})$ | STRESS $\times 10^{3} \mathrm{kN} / \mathrm{m}^{2}$ |
| :---: | :---: |
| 0.00 | 0.8195 |
| 0.20 | 0.4909 |
| 0.40 | 0.3743 |
| 0.60 | 0.3095 |
| 0.80 | 0.2584 |
| 1.00 | 0.2151 |

Table 4.13


# RESULTS FOR ELLIPTICAL TUNNEL $\mathbf{a} / \mathbf{b}=1.358$ 

### 5.1. Influence of Liner Thickness on Stress and Deformation in Rock Around Tunnel

Principal stresses were investigated along three radial lines $\mathrm{AB}, \mathrm{CD}$ and EF , shown in figure 5.1 radiating from the center of the tunnel. For the tunnel with $a / b=1.358$, variation of the major principal stress along the radial line $A B$ for different liner thicknesses is shown in figure 5.2, and the variation of the minor principal stress along the same line for different liner thicknesses is shown in figure 5.5. Corresponding results for the same tunnel along line CD are shown in figures 5.3 and 5.6, respectively. Figures 5.4 and 5.7 , respectively, show the corresponding results for the same tunnel along line EF.

Figure 5.8 shows the circumferential line considered for analysis Figure 5.9 shows the variation of principal tensile stress along an elliptical (circumferential) line of a shape similar to that of the tunnel opening, but at some distance inside the rock mass from the tunnel face, as the liner thickness is varied, for the tunnel with $a / b=1.358$. The circumferential line along which the stresses shown in figure 5.9 are evaluated is similar to the line GH shown on figure 5.8. of Montuma Sri Lanka

For the elliptical tunnel with $a / b=1.358$, influence of the concrete liner thickness on displacement at points inside the rock mass are illustrated by figures 5.10 and 5.11 . Figures 5.10 and 5.11 show displacements at points inside the rock mass located along an elliptical (circumferential) line GH, which is shown on the scaled diagram of 5.8.

Figure $5.2,5.3 \& 5.4$ are shows the variation of major principal stress along radical line $A B, C D \& E F$ respectively.

In the case of line AB (figure 5.2), for the tunnel $\mathrm{a} / \mathrm{b}=1.358$ principal tensile stress at a point inside the rock(element number 21) when there is no lining, which is 547.8 kPa decreases by $20.44 \%$ when a liner of thickness of 0.2 m is introduced. The corresponding reductions are $38.9 \%$ for a liner thickness of 0.4 m thickness and $65.5 \%$ for a liner of 1.0 m .

In the case of line $C D$ (figure 5.3 ), for the tunnel $\mathrm{a} / \mathrm{b}=1.358$ principal stress at a point inside the rock(element number 26) reduce by $28.3 \%$ when a liner of thickness of 0.2 m is introduced as compared to the stresses in the case of unlined tunnel. The corresponding reductions are $40.0 \%$ for a liner thickness of 0.4 m thickness and $55.5 \%$ for a liner of 1.0 m .

In the case of line EF (figure 5.4 , for the tunnel $\mathrm{a} / \mathrm{b}=1.358$ major principal stress at a point inside the rock(element number 26) reduce by $28.3 \%$ when a liner of thickness of 0.2 m is introduced as compared to the stresses in the case of unlined tunnel. The corresponding reductions are $40.0 \%$ for a liner thickness of 0.4 m thickness and $55.5 \%$ for a liner of 1.0 m .

The numerical results and the comparison of figures $5.2,5.3 \& 5.4$ show that the line EF is the critical line along which maximum principal tensile stresses occurred.

Figures 5.5, 5.6 and 5.7 show the influence of concrete liner thickness on the compressive principal stress around the tunnel with $a / b=1.358$. According to figure 5.5 , the minor principal stress at a point inside the rock closure to point A reduces by $16.5 \%$ when a 0.2 m thick concrete is introduced to the originally unlined tunnel; this reduction is $26.53 \%$ for a 0.4 m thick liner and $40.8 \%$ for a 1.0 m thick liner. Figure 5.6 shows similar behavior of the minor principal stress along the line CD. Figure 5.7 shows that large percentage stress reductions occur in the case of the minor principal stress along line EF. This stress reduces at a point inside the rock closure to point E by $52.5 \%$ when a 0.2 m thick liner is introduced to the unlined tunnel; the corresponding reduction is $79.2 \%$ for a 0.4 m thick liner, and $91.1 \%$ for a 1.0 m thick liner.

Figures $5.9 \& 5.10$ show the variation of major principal stress and minor principal stress along circumferential line GH respectively, which is in rock.

The major principal stress reduction is $19.18 \%$ when 0.2 m liner is introduced as compared to the stress in the case of unlined tunnel closure to point A . Where as reduction is $27.6 \%$ at point $E$ when 0.2 m liner is introduced as compared to the stress in the case of an unlined tunnel.

Figure 5.10 shows the minor principal stress variation along line GH. It also shows the same pattern of reduction as in the major principal stress mentioned above.

According to these results in figures 5.11 and 5.12, the percentage reduction of x displacement and $y$-displacement over the rock domain varies with the location. Figure 5.11 shows relatively large percentage reductions in the $x$-displacement at the $x$-axis as the tunnel liner thickness is increased (this is $42.92 \%$ when a 0.2 m thick liner is introduced on the unlined tunnel; and about $94.57 \%$ for a 1.0 m thick liner).

Figures $4.13 .4 .14 \& 4.15$ are shows the variation of major principal stress with the introduction of concrete liner on three elements close to point $A, C$ \& E respectively.


Figure 5.1 Radial lines (For elliptical tunnel-2, $\mathrm{a} / \mathrm{b}=1.358$ )


Figure 5.2 Variation of major principal stress along radial line "AB" (For elliptical tunnel $-2, \mathrm{a} / \mathrm{b}=1.358$ )

VARIATION OF MAJOR PRINCIPAL STRESS ALONG RADIAL LINE "AB" (FOR ELLIPTICAL TUNNEL $-2, a / b=1.356$ )

| ELEMENT NUMBER | MAJOR PRINCIPAL STRESS * $10^{3}\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 1 | 0.7122 | 7.2430 | 5.6360 | 4.7630 | 3.8850 | 3.1840 |
| 11 | 0.6343 | 0.4818 | 0.3591 | 4.5450 | 3.8260 | 3.1370 |
| 21 | 0.5478 | 0.4358 | 0.3345 | 0.2848 | 0.2379 | 0.1891 |
| 31 | 0.4672 | 0.3776 | 0.2944 | 0.2574 | 0.2210 | 0.1814 |
| 41 | 0.3978 | 0.3191 | 0.2518 | 0.1274 | 0.1918 | 0.1660 |
| 51 | 0.3346 | 0.2643 | 0.2109 | 0.1806 | 0.1616 | 0.1450 |
| 61 | 0.2758 | 0.2145 | 0.1725 | 0.1477 | 0.1331 | 0.1215 |
| 71 | 0.2247 | 0.1730 | 0.1398 | 0.1200 | 0.1086 | 0.0998 |
| 81 | 0.1803 | 0.1378 | 0.1170 | 0.0963 | 0.0874 | 0.0806 |
| 91 | 0.1418 | 0.1079 | 0.0877 | 0.0759 | 0.0690 | 0.0637 |
| 101 | 0.1110 | 0.0844 | 0.0687 | 0.0597 | 0.0543 | 0.0503 |
| 111 | 0.0860 | 0.0653 | 0.0533 | 0.0464 | 0.0423 | 0.0392 |
| 121 | 0.0651 | 0.0495 | 0.0404 | 0.0354 | 0.0323 | 0.0299 |
| 131 | 0.0475 | 0.0361 | 0.0296 | 0.0260 | 0.0237 | 0.0220 |
| 141 | 0.0324 | 0.0246 | 0.0202 | 0.0177 | 0.0162 | 0.0151 |
| 151 | 0.0192 | 0.0146 | 0.0119 | 0.0105 | 0.0095 | 0.0088 |
| 161 | 0.0081 | 0.0060 | 0.0049 | 0.0041 | 0.0037 | 0.0034 |
| 171 | 0.0033 | 0.0024 | 0.0019 | 0.0017 | 0.0016 | 0.0015 |
| 181 | 0.0197 | 0.0159 | 0.0139 | 0.0131 | 0.0124 | 0.0118 |
|  |  |  |  |  |  |  |

Table 5.1


Figure 5.3 Variation of major principal stress along radial line "CD" (For elliptical tunnel-2, $\mathrm{a} / \mathrm{b}=1.358$ )

VARIATION OF MAJOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" (FOR ELLIPTICAL TUNNEL $-2, a / b=1.356$ )

| ELEMENT NUMBER | MAJOR PRINCIPAL STRESS* $10^{3}\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 6 | 0.9991 | 7.7680 | 5.3120 | 4.4850 | 3.9790 | 3.5370 |
|  | LINER ELEMENTS |  |  |  |  |  |
| 26 | 0.7849 | 0.5535 | 0.3944 | 4.1330 | 3.7910 | 3.2930 |
| 36 | 0.6593 | 0.4726 | 0.3947 | 0.3288 | 0.3220 | 0.2964 |
| 46 | 0.5088 | 0.3684 | 0.3231 | 0.2764 | 0.2650 | 0.2560 |
| 56 | 0.4056 | 0.2998 | 0.2524 | 0.2211 | 0.2072 | 0.1986 |
| 66 | 0.3075 | 0.2303 | 0.1901 | 0.1677 | 0.1551 | 0.1465 |
| 76 | 0.2323 | 0.1752 | 0.1428 | 0.1260 | 0.1159 | 0.0904 |
| 86 | 0.1704 | 0.1288 | 0.1041 | 0.0917 | 0.0840 | 0.0783 |
| 96 | 0.1169 | 0.0882 | 0.0708 | 0.0621 | 0.0567 | 0.0526 |
| 106 | 0.0756 | 0.0567 | 0.0450 | 0.0393 | 0.0356 | 0.0329 |
| 116 | 0.0490 | 0.0365 | 0.0288 | 0.0249 | 0.0225 | 0.0207 |
| 126 | 0.0322 | 0.0237 | 0.0185 | 0.0158 | 0.0141 | 0.0129 |
| 136 | 0.0203 | 0.0148 | 0.0112 | 0.0094 | 0.0083 | 0.0075 |
| 146 | 0.0109 | 0.0077 | 0.0057 | 0.0046 | 0.0040 | 0.0036 |
| 156 | 0.0035 | 0.0023 | 0.0014 | 0.0009 | 0.0007 | 0.0005 |
| 166 | -0.0006 | -0.0007 | -0.0007 | -0.0008 | -0.0008 | -0.0007 |
| 176 | -0.0032 | -0.0024 | -0.0019 | -0.0017 | -0.0015 | -0.0013 |
| 186 | -0.0036 | -0.0025 | -0.0019 | -0.0015 | -0.0012 | -0.0010 |
|  | -0.0056 | -0.0004 | -0.0011 | -0.0007 | -0.0005 | -0.0004 |

Table 5.2


Figure 5.4 Variation of major principal stress along radial line "EF" (For elliptical tunnel-2, $\mathrm{a} / \mathrm{b}=1.358$ )

VARIATION OF MAJOR PRINCIPAL STRESS ALONG RADIAL LINE "EF" (FOR ELLIPTICAL TUNNEL $-2, \mathrm{a} / \mathrm{b}=1.356$ )

| ELEMENT NUMBER | MAJOR PRINCIPAL STRESS * $10^{3}\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  | LINER ELEMENTS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS (m) |  |  |  |  |  |  |
|  | t $=0.0$ | $\mathrm{t}=0.2$ | t $=0.4$ | $\mathrm{t}=0.6$ | t $=0.8$ | $\mathrm{t}=1.0$ |  |
| 10 | 1.3670 | 11.3203 | 7.4210 | 6.2540 | 5.7130 | 5.2690 |  |
| 20 | 1.0950 | 0.9083 | 0.5184 | 4.6120 | 4.0780 | 3.4660 |  |
| 30 | 0.8015 | 0.6006 | 0.4074 | 0.3313 | 0.2942 | 0.2447 |  |
| 40 | 0.5815 | 0.4209 | 0.3016 | 0.2527 | 0.2218 | 0.1936 |  |
| 50 | 0.4075 | 0.2907 | 0.2163 | 0.1846 | 0.1616 | 0.1425 |  |
| 60 | 0.2887 | 0.2053 | 0.1560 | 0.1336 | 0.1175 | 0.0904 |  |
| 70 | 0.2065 | 0.1470 | 0.1127 | 0.0964 | 0.0850 | 0.0759 |  |
| 80 | 0.1458 | 0.1037 | 0.0797 | 0.0679 | 0.0598 | 0.0535 |  |
| 90 | 0.1024 | 0.0728 | 0.0559 | 0.0473 | 0.0416 | 0.0372 |  |
| 100 | 0.0717 | 0.0504 | 0.0384 | 0.0323 | 0.0283 | 0.0254 |  |
| 110 | 0.0482 | 0.0340 | 0.0257 | 0.0213 | 0.0186 | 0.0164 |  |
| 120 | 0.0316 | 0.0221 | 0.0164 | 0.0134 | 0.0115 | 0.0101 |  |
| 130 | 0.0198 | 0.0135 | 0.0098 | 0.0078 | 0.0066 | 0.0057 |  |
| 140 | 0.0112 | 0.0074 | 0.0051 | 0.0039 | 0.0031 | 0.0026 |  |
| 150 | 0.0050 | 0.0030 | 0.0018 | 0.0017 | 0.0008 | 0.0005 |  |
| 160 | 0.0005 | -0.0067 | -0.0004 | -0.0006 | 0.0007 | -0.0008 |  |
| 170 | -0.0025 | -0.0021 | -0.0018 | -0.0017 | -0.0001 | -0.0015 |  |
| 180 | -0.0026 | -0.0021 | -0.0075 | -0.0016 | -0.0001 | -0.0014 |  |
| 190 | 0.0054 | 0.0013 | 0.0019 | 0.0013 | 0.0007 | 0.0004 |  |

Table 5.3


SCALE $1 \mathrm{~cm}=108 \mathrm{kN} / \mathrm{m}^{-2}$

Figure 5.5 Variation of minor principal stress along radial line "AB" (For elliptical unnel-2, $\mathrm{a} / \mathrm{b}=1.358$ )

VARIATION OF MINOR PRINCIPAL STRESS ALONG RADIAL LINE "AB"
(FOR ELLIPTICAL TUNNEL $-2, a / b=1.356$ )

| ELEMENT NUMBER | MINOR PRINCIPAL STRESS $\left(\mathrm{kN} / \mathrm{m}^{2}\right)^{\star} 10^{3}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 1 | -1.0320 | -0.9726 | -0.8671 | -0.9171 | -0.9288 | -0.9387 |
|  | LINER ELEMENTS |  |  |  |  |  |
| 11 | -0.9541 | -0.7891 | -0.6717 | -0.7394 | -0.7157 | -0.6605 |
| 21 | -0.8603 | -0.7181 | -0.6321 | -0.6169 | -0.5697 | -0.5089 |
| 31 | -0.7609 | -0.6343 | -0.5640 | -0.5439 | -0.5195 | -0.4865 |
| 41 | -0.6642 | -0.5496 | -0.4924 | -0.4686 | -0.4497 | -0.4289 |
| 51 | -0.5643 | -0.4631 | -0.4161 | -0.3938 | -0.3782 | -0.3631 |
| 61 | -0.4750 | -0.3876 | -0.3483 | -0.3290 | -0.3157 | -0.3036 |
| 71 | -0.3961 | -0.3221 | -0.2888 | -0.2726 | -0.2613 | -0.2511 |
| 81 | -0.3288 | -0.2668 | -0.2385 | -0.2250 | -0.2153 | -0.2066 |
| 91 | -0.2733 | -0.2216 | -0.1974 | -0.1862 | -0.1779 | -0.1704 |
| 101 | -0.2285 | -0.1852 | -0.1644 | -0.1550 | -0.1478 | -0.1414 |
| 111 | -0.1931 | -0.1565 | -0.1384 | -0.1304 | -0.1242 | -0.1187 |
| 121 | -0.1638 | -0.1328 | -0.1171 | -0.1102 | -0.1005 | -0.0950 |
| 131 | -0.1405 | -0.1138 | -0.1001 | -0.0942 | -0.0895 | -0.0854 |
| 141 | -0.1208 | -0.0979 | -0.0859 | -0.0808 | -0.0767 | -0.0731 |
| 151 | -0.1041 | -0.0843 | -0.0738 | -0.0694 | -0.0659 | -0.0627 |
| 161 | -0.0898 | -0.0727 | -0.0636 | -0.0598 | -0.0567 | -0.0540 |
| 171 | -0.0791 | -0.0640 | -0.0560 | -0.0526 | -0.0500 | -0.0475 |
| 181 | -0.0769 | -0.0623 | -0.0544 | -0.0511 | -0.0485 | -0.0461 |

Table 5.4


Figure 5.6 Variation of minor principal stress along radial line "CD" (For elliptical tunnel-2, $\mathrm{a} / \mathrm{b}=1.358$ )

VARIATION OF MINOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" (FOR ELLIPTICAL TUNNEL $-2, \mathrm{a} / \mathrm{b}=1.356$ )

| ELEMENT NUMBER | MINOR PRINCIPAL STRESS $\left(\mathrm{kN} / \mathrm{m}^{2}\right)^{\star} 10^{3}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 6 | -0.8335 | -0.4562 | -0.6347 | -0.6632 | -0.6885 | -0.7096 |
| 16 | -0.8354 | -0.7242 | -0.6399 | -0.5000 | -0.4903 | -0.4717 |
| 26 | -0.6888 | -0.5519 | -0.4629 | -0.4246 | -0.3872 | -0.3651 |
| 36 | -0.5920 | -0.4761 | -0.4696 | -0.3479 | -0.3230 | -0.3107 |
| 46 | -0.4716 | -0.3758 | -0.3019 | -0.2667 | -0.2447 | -0.2308 |
| 56 | -0.3661 | -0.2896 | -0.2300 | -0.2024 | -0.1845 | -0.1719 |
| 66 | -0.2875 | -0.2246 | -0.1768 | -0.1548 | -0.1403 | -0.1297 |
| 76 | -0.2218 | -0.1713 | -0.1345 | -0.1172 | -0.1059 | -0.0975 |
| 86 | -0.1674 | -0.1279 | -0.1004 | -0.0871 | -0.0786 | -0.0721 |
| 96 | -0.1272 | -0.0959 | -0.0749 | -0.0645 | -0.0579 | -0.0529 |
| 106 | -0.0987 | -0.0738 | -0.0577 | -0.0495 | -0.0443 | -0.0404 |
| 116 | -0.0843 | -0.0628 | -0.0490 | -0.0420 | -0.0375 | -0.0341 |
| 126 | -0.0716 | -0.0532 | -0.0415 | -0.0355 | -0.0317 | -0.0288 |
| 136 | -0.0607 | -0.0449 | -0.0350 | -0.0298 | -0.0265 | -0.0241 |
| 146 | -0.0528 | -0.0390 | -0.0304 | -0.0259 | -0.0231 | -0.0209 |
| 156 | -0.0453 | -0.0333 | -0.0250 | -0.0220 | -0.0196 | -0.0177 |
| 166 | -0.0396 | -0.0292 | -0.0227 | -0.0193 | -0.0172 | -0.0156 |
| 176 | -0.0337 | -0.0247 | -0.0191 | -0.0161 | -0.0142 | -0.0128 |
| 186 | -0.0240 | -0.0319 | -0.0161 | -0.0134 | -0.0125 | -0.0106 |

Table 5.5


Figure 5.7 Variation of minor principal stress along radial line "EF"
(For elliptical tunnel-2, $\mathrm{a} / \mathrm{b}=1.358$ )

VARIATION OF MINOR PRINCIPAL STRESS ALONG RADIAL LINE "EF"
(FOR ELLIPTICAL TUNNEL $-2, a / b=1.356$ )

| ELEMENT NUMBER | MINOR PRINCIPAL STRESS $\left(\mathrm{kN} / \mathrm{m}^{2}\right)^{*} 10^{3}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 10 | -0.8696 | -0.6431 | -0.4378 | -0.4961 | -0.5459 | -0.5739 |
| 20 | -0.6887 | -0.3898 | -0.1358 | -0.1480 | -0.0640 | -0.8474 |
| 30 | -0.5173 | -0.2458 | -0.1075 | -0.0323 | -0.0128 | 0.0458 |
| 40 | -0.3816 | -0.1784 | -0.0860 | -0.0305 | 0.0048 | 0.0299 |
| 50 | -0.2799 | -0.1322 | -0.0657 | -0.0233 | 0.0023 | 0.0199 |
| 60 | -0.2074 | -0.1028 | -0.0531 | -0.0208 | -0.0022 | 0.0103 |
| 70 | -0.1595 | -0.0820 | -0.0431 | -0.0177 | -0.0035 | 0.0060 |
| 80 | -0.1233 | -0.0657 | -0.0350 | -0.0151 | -0.0042 | 0.0031 |
| 90 | -0.0971 | -0.0534 | -0.0289 | -0.0131 | -0.0046 | 0.0010 |
| 100 | -0.0783 | -0.0442 | -0.0245 | -0.0118 | -0.0050 | -0.0005 |
| 110 | -0.0642 | -0.0371 | -0.0210 | -0.0107 | -0.0051 | -0.0015 |
| 120 | -0.0542 | -0.0321 | -0.0186 | -0.0100 | -0.0054 | -0.0024 |
| 130 | -0.0467 | -0.0281 | -0.0167 | -0.0095 | -0.0056 | -0.0031 |
| 140 | -0.0409 | -0.0251 | -0.0153 | -0.0092 | -0.0059 | -0.0037 |
| 150 | -0.0362 | -0.0226 | -0.0141 | -0.0089 | -0.0060 | -0.0046 |
| 160 | -0.0324 | -0.0205 | -0.0131 | -0.0085 | -0.0060 | -0.0043 |
| 170 | -0.0289 | -0.0186 | -0.0121 | -0.0081 | -0.0006 | -0.0043 |
| 180 | -0.0267 | -0.0173 | -0.0115 | -0.0079 | -0.0006 | -0.0045 |
| 190 | -0.0270 | -0.0177 | -0.0118 | -0.0083 | -0.0006 | -0.0049 |

Table 5.6


Figure 5.8 Circumferential lines (For elliptical tunnel- $2, \mathrm{a} / \mathrm{b}=1.358$ )


Figure 5.9 Variation of major principal stress along circumferential line " GH " (For elliptical tunnel-2, $\mathrm{a} / \mathrm{b}=1.358$ )

VARIATION OF MAJOR PRINCIPAL STRESS ALONG CIRCUMFERENTIAL LINE "GH" (FOR ELLIPTICAL TUNNEL $-2, a / b=1.356$ )

| ELEMENT NUMBER | MAJOR PRINCIPAL STRESS $100^{3}\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 31 | 0.4672 | 0.3776 | 0.2945 | 0.2574 | 0.2210 | 0.1814 |
| 32 | 0.4646 | 0.3190 | 0.3032 | 0.2598 | 0.2309 | 0.1993 |
| 33 | 0.4685 | 0.3873 | 0.3157 | 0.2618 | 0.2383 | 0.2250 |
| 34 | 0.4771 | 0.3835 | 0.3178 | 0.2626 | 0.2427 | 0.2414 |
| 35 | 0.4982 | 0.3834 | 0.3231 | 0.2697 | 0.2545 | 0.2510 |
| 36 | 0.5088 | 0.3684 | 0.3164 | 0.2764 | 0.2650 | 0.2560 |
| 37 | 0.5551 | 0.3871 | 0.3270 | 0.2928 | 0.2774 | 0.2670 |
| 38 | 0.5679 | 0.3978 | 0.3235 | 0.2951 | 0.2674 | 0.2514 |
| 39 | 0.5691 | 0.4074 | 0.3132 | 0.2800 | 0.2470 | 0.2242 |
| 40 | 0.5815 | 0.4209 | 0.3016 | 0.2527 | 0.2218 | 0.1936 |

Table 5.7


No. of Nodes - 200
No of Elements - 190


SCALE $1 \mathrm{~cm}=137 \mathrm{kN} / \mathrm{m}^{-2}$

Figure 5.10 Variation of minor principal stress along circumferential line " GH " (For elliptical tunnel-2, $\mathrm{a} / \mathrm{b}=1.358$ )

VARIATION OF MINOR PRINCIPAL STRESS ALONG CIRCUMFERENTIAL "GH" (FOR ELLIPTICAL TUNNEL $-2, a / b=1.356$ )

| ELEMENT NUMBER | MINOR PRINCIPAL STRESS $\left(\mathrm{kN} / \mathrm{m}^{2}\right)^{\star} 10^{3}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 31 | -0.7609 | -0.6343 | -0.5640 | -0.5439 | -0.5195 | -0.4865 |
| 32 | -0.7703 | -0.6405 | -0.5773 | -0.5384 | -0.5154 | -0.4964 |
| 33 | -0.7488 | -0.6224 | -0.5640 | -0.5244 | -0.4975 | -0.474 |
| 34 | -0.7055 | -0.5889 | -0.5266 | -0.4813 | -0.4579 | -0.4385 |
| 35 | -0.6377 | -0.5348 | -0.4696 | -0.4137 | -0.3954 | -0.3849 |
| 36 | -0.5920 | -0.4761 | -0.3937 | -0.3479 | -0.3230 | -0.3107 |
| 37 | -0.5693 | -0.4287 | -0.3133 | -0.2743 | -0.2460 | -0.2276 |
| 38 | -0.5197 | -0.3595 | -0.2385 | -0.1867 | -0.1568 | -0.1390 |
| 39 | -0.4280 | -0.2404 | -0.1428 | -0.0888 | -0.0591 | -0.0398 |
| 40 | -0.3816 | -0.1784 | -0.0860 | -0.0305 | -0.0248 | -0.0299 |

Table 5.8


Nio ot :xindes - 200

| hatr makkness t" in m |  |  |
| :---: | :---: | :---: |
| 1 | =0.0 | - |
|  | $=02$ | - -- |
| : | $=0.4$ | - - . |
|  | = 0.6 |  |
| , ! | =05 |  |
| 1 | $=1.0$ | --- |

SCAR 10 O: $0.0735 \times 10^{-}-3 \mathrm{~m}$

Figure 5.11 Variation of " $x$ " displacement along circumferential line "GH"
(For elliptical tunnel-2, $\mathrm{a} / \mathrm{b}=1.358$ )

VARIATION OF "X" DISPLACEMENTS CIRCUMFERENTIAL LINE "GH" (FOR ELLIPTICAL TUNNEL $-2, \mathrm{a} / \mathrm{b}=1.356$ )

| NODE NUMBER | "X" DISPLACEMENT * $10^{-3}(\mathrm{~m})$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 34 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 35 | 0.2909 | 0.2374 | 0.1915 | 0.1734 | 0.1524 | 0.1294 |
| 36 | 0.5913 | 0.4867 | 0.3958 | 0.3505 | 0.3135 | 0.2710 |
| 37 | 0.8622 | 0.7100 | 0.5775 | 0.4984 | 0.4459 | 0.3987 |
| 38 | 1.1070 | 0.9001 | 0.7199 | 0.5985 | 0.5377 | 0.4953 |
| 39 | 1.2910 | 1.0160 | 0.7919 | 0.6397 | 0.5651 | 0.5204 |
| 40 | 1.4640 | 1.0870 | 0.8018 | 0.6379 | 0.5492 | 0.4889 |
| 41 | 1.6120 | 1.1210 | 0.7735 | 0.5794 | 0.4715 | 0.3984 |
| 42 | 1.6310 | 1.0440 | 0.6807 | 0.4673 | 0.3459 | 0.2617 |
| 43 | 1.6100 | 0.9485 | 0.5836 | 0.3600 | 0.2309 | 0.1396 |
| 44 | 1.6240 | 0.9270 | 0.5487 | 0.3180 | 0.1824 | 0.0882 |

Table 5.9


Figure 5.12 Variation of " y " displacement along circumferential line " GH " (For elliptical tunnel-2, $\mathrm{a} / \mathrm{b}=1.358$ )

VARIATION OF "Y' DISPLACEMENT CIRCUMFERENTIAL LINE "GH" (FOR ELLIPTICAL TUNNEL $-2, a / b=1.356$ )

| NODE NUMBER | $" Y$ " DISPLACEMENT $(\mathrm{m}) * 10^{-3}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 34 | 3.2260 | 2.6200 | 2.3060 | 2.1700 | 2.0640 | 1.9550 |
| 35 | 3.2070 | 2.6010 | 2.2900 | 2.1420 | 2.0350 | 1.9420 |
| 36 | 3.1150 | 2.5180 | 2.2160 | 2.0570 | 1.9530 | 1.8650 |
| 37 | 2.9160 | 2.3400 | 2.0430 | 1.8910 | 1.7840 | 1.6970 |
| 38 | 2.6380 | 2.0950 | 1.7960 | 1.6450 | 1.5480 | 1.4660 |
| 39 | 2.2268 | 1.7740 | 1.4830 | 1.3490 | 1.2510 | 1.1710 |
| 40 | 1.8810 | 1.4330 | 1.1400 | 1.0310 | 0.9341 | 0.8553 |
| 41 | 1.4440 | 1.0750 | 0.8068 | 0.7100 | 0.6221 | 0.5520 |
| 42 | 0.9429 | 0.6801 | 0.4863 | 0.1813 | 0.3499 | 0.2993 |
| 43 | 0.4729 | 0.3309 | 0.2268 | 0.1613 | 0.1543 | 0.1291 |
| 44 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |

Table 5.10


Figure 5.13 Variation of major principal stress with liner thickness (For element number 21)

| LINER THICKNESS $(\mathrm{m})$ | STRESS $\times 10^{3} \mathrm{kN} / \mathrm{m}^{2}$ |
| :---: | :---: |
| 0.00 | 0.5478 |
| 0.20 | 0.4358 |
| 0.40 | 0.3345 |
| 0.60 | 0.2848 |
| 0.80 | 0.2379 |
| 1.00 | 0.1891 |

Table 5.11


Figure 5.14 Variation of major principal stress with liner thickness (For element number 26)

| LINER THICKNESS $(\mathrm{m})$ | STRESS $\times 10^{3} \mathrm{kN} / \mathrm{m}^{2}$ |
| :---: | :---: |
| 0.00 | 0.6593 |
| 0.20 | 0.4726 |
| 0.40 | 0.3947 |
| 0.60 | 0.3288 |
| 0.80 | 0.3220 |
| 1.00 | 0.2964 |

Table 5.12


Figure 5.15 Variation of major principal stress with liner thickness (For element number 36)

| LINER THICKNESS $(\mathrm{m})$ | STRESS $\times 10^{3} \mathrm{kN} / \mathrm{m}^{2}$ |
| :---: | :---: |
| 0.00 | 0.8015 |
| 0.20 | 0.6006 |
| 0.40 | 0.4074 |
| 0.60 | 0.3313 |
| 0.80 | 0.2942 |
| 1.00 | 0.2447 |

Table 5.13

## CHPTER 6.0

## RESULTS FOR ELLIPTICAL TUNNEL $\mathbf{a} / \mathrm{b}=1.500$

### 6.1. Influence of Liner Thickness on Stress and Deformation in Rock Around Tunnel

Principal stresses were investigated along three radial lines $\mathrm{AB}, \mathrm{CD}$ and EF , shown in figure 6.1 radiating from the center of the tunnel. For the tunnel with $a / b=1.500$, variation of the major principal stress along the radial line $A B$ for different liner thicknesses is shown in figure 6.2, and the variation of the minor principal stress along the same line for different liner thicknesses is shown in figure 6.5. Corresponding results for the same tunnel along line CD are shown in figures 6.3 and 6.6 , respectively. Figures 6.4 and 6.7 , respectively, show the corresponding results for the same tunnel along line EF.

Figure 6.8 shows the circumferential line considered for analysis. Figure 6.9 shows the variation of major principal stress along an elliptical (circumferential) line of a shape similar to that of the tunnel opening, but at some distance inside the rock mass from the tunnel face, as the liner thickness is varied, for the tunnel with $a / b=1.500$. The circumferential line along which the stresses shown in figure 6.9 are evaluated is similar to the line GH shown on figure 6.8 . ar Mormuma Sri Lanka

For the elliptical tunnel with $a / b=1.500$, influence of the concrete liner thickness on displacement at points inside the rock mass are illustrated by figures 6.10 and 6.11 . Figures 6.10 and 6.11 show displacements at points inside the rock mass located along an elliptical (circumferential) line GH, which is shown on the scaled diagram of 6.8 .

Figure $6.2,6.3 \& 6.4$ show the variation of major principal stress along radical line $\mathrm{AB}, \mathrm{CD} \& \mathrm{EF}$ respectively.

In the case of line $A B$ (figure 6.2), for the tunnel $a / b=1.500$ tensile stress at a point inside the rock(element number 51) when there is no lining, which is 343.4 kPa decreases by $14.78 \%$ when a liner of thickness of 0.2 m is introduced. The corresponding reductions are $29.24 \%$ for a liner thickness of 0.4 m thickness and $47.26 \%$ for a liner of 1.0 m .

In the case of line CD (figure 6.3 ), for the tunnel $\mathrm{a} / \mathrm{b}=1.500$ principal stress at a point inside the rock(element number 56 ) reduce by $24.17 \%$ when a liner of thickness of 0.2 m is introduced as compared to the stresses in the case of unlined tunnel. The corresponding reductions are $38.48 \%$ for a liner thickness of 0.4 m thickness and $51.64 \%$ for a liner of 1.0 m .

In the case of line EF (figure 6.4 ), for the tunnel $\mathrm{a} / \mathrm{b}=1.500$ principal stress at a point inside the rock(element number 60) reduce by $38.17 \%$ when a liner of thickness of 0.2 m is introduced as compared to the stresses in the case of unlined tunnel. The corresponding reductions are $51.69 \%$ for a liner thickness of 0.4 m thickness and $69.58 \%$ for a liner of 1.0 m .

The numerical results and the comparison of figures $6.2,6.3 \& 6.4$ show that the line EF is the critical line along which maximum major principal stresses occurred.

Figures 6.5, 6.6 and 6.7 show the influence of concrete liner thickness on the compressive principal stress around the tunnel with $a / b=1.500$. According to Figure (6.8), the compressive principal stress at a point inside the rock closure to point $A$ reduces by $13.52 \%$ when a 0.2 m thick concrete is introduced to the originally unlined tunnel; this reduction is $19.33 \%$ for a 0.4 m thick liner and $24.66 \%$ for a 1.0 m thick liner. Figure 6.6 shows similar behavior of the compressive principal stress along the line CD. Figure 6.7 shows that large percentage stress reductions occur in the case of the compressive principal stress along line EF. This stress reduces at point $E$ by $67.68 \%$ when a 0.2 m thick liner is introduced to the unlined tunnel; the corresponding reduction is $71.72 \%$ for a 0.4 m thick liner, and $75.26 \%$ for a 1.0 m thick liner.

Figures $6.9 \& 6.10$ shows the variation of major principal stress and minor principal stress along circumferential line GH respectively, which is in rock.

The major principal stress reduction is $14.68 \%$ when 0.2 m liner is introduced as compared to the stress in the case of unlined tunnel closure to point A . Where as reduction is $28.28 \%$ at point E when 0.2 m liner is introduced as compared to the stress in the case of an unlined tunnel.

Figure 6.10 shows the minor principal stress variation along line GH. It also shows the same pattern of reduction as in the major principal stress mentioned above.

According to these results in figures 6.11 and 6.12 the percentage reduction of $x$ displacement and $y$-displacement over the rock domain varies with the location. figure 6.11 shows relatively large percentage reductions in the x -displacement at the x -axis as the tunnel liner thickness is increased (this is $51.8 \%$ when a 0.2 m thick liner is introduced on the unlined tunnel; and about $99 \%$ for a 1.0 m thick liner).

Figures $4.13,4.14 \& 4.15$ are shows the variation of major principal stress with the introduction of concrete liner on three elements close to point A,C \& E respectively.

A further analysis of strain set up in the concrete liner as predicted by the finite element is given in Appendix B.


Figure 6.1 Radial lines (For elliptical tunnel-3, $a / b=1.500$ )


Figure 6.2 Variation of major principal stress along radial line " AB "
(For elliptical tunnel-3, a/b $=1.500$ )

VARIATION OF MAJOR PRINCIPAL STRESS ALONG RADIAL LINE "AB"
(FOR ELLIPTICAL TUNNEL-3, $\mathrm{a} / \mathrm{b}=1.500$ )

| ELEMENT NUMBER | MAJOR PRINCIPAL STRESS $\times 10^{3}\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 1 | 0.3002 | 5.0010 | 3.8490 | 2.8670 | 2.2010 | 1.6880 |
| 11 | 0.3212 | 0.3080 | 4.2840 | 3.3230 | 2.6370 | 2.1850 |
| 21 | 0.3308 | 0.3056 | 0.2540 | 3.9600 | 2.9630 | 2.5640 |
| 31 | 0.3409 | 0.3061 | 0.2570 | 0.2162 | 3.3140 | 2.9570 |
| 41 | 0.3449 | 0.3031 | 0.2536 | 0.2132 | 0.1868 | 3.1780 |
| 51 | 0.3434 | 0.2930 | 0.2436 | 0.2069 | 0.1878 | 0.1811 |
| 61 | 0.3300 | 0.2712 | 0.2231 | 0.1928 | 0.1788 | 0.1769 |
| 71 | 0.2967 | 0.2365 | 0.1929 | 0.1690 | 0.1561 | 0.1509 |
| 81 | 0.2579 | 0.2011 | 0.1634 | 0.1443 | 0.1322 | 0.1258 |
| 91 | 0.2213 | 0.1698 | 0.1379 | 0.1220 | 0.1112 | 0.1051 |
| 101 | 0.1891 | 0.1434 | 0.1165 | 0.1032 | 0.0936 | 0.0882 |
| 111 | 0.1564 | 0.1174 | 0.0956 | 0.0848 | 0.0767 | 0.0721 |
| 121 | 0.1209 | 0.0899 | 0.0734 | 0.0651 | 0.0588 | 0.0552 |
| 131 | 0.0904 | 0.0668 | 0.0547 | 0.0486 | 0.0439 | 0.0411 |
| 141 | 0.0645 | 0.0476 | 0.0392 | 0.0349 | 0.0315 | 0.0295 |
| 151 | 0.0441 | 0.0325 | 0.0269 | 0.0241 | 0.0218 | 0.0204 |
| 161 | 0.0273 | 0.0202 | 0.0168 | 0.0151 | 0.0137 | 0.0129 |
| 171 | 0.0163 | 0.0122 | 0.0103 | 0.0093 | 0.0085 | 0.0080 |
| 181 | 0.0086 | 0.0064 | 0.0055 | 0.0055 | 0.0046 | 0.0043 |
| 191 | 0.0027 | 0.0020 | 0.0017 | 0.0017 | 0.0014 | 0.0014 |
| 200 | 0.0002 | -0.0713 | -0.0006 | -0.0006 | -0.0023 | 0.0004 |
| 210 | -0.0018 | -0.0013 | -0.0009 | -0.0009 | -0.0006 | -0.0003 |

## Table 6.1

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Figure 6.3 Variation of major principal stress along radial line "CD"
(For elliptical tunnel-3, $\mathrm{a} / \mathrm{b}=1.500$ )

VARIATION OF MAJOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" (FOR ELLIPTICAL TUNNEL-3, $\mathrm{a} / \mathrm{b}=1.500$ )

| ELEMENT NUMBER | MAJOR PRINCIPAL STRESS $\times 10^{3}\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 6 | 0.7990 | 9.9410 | 6.2190 | 5.0880 | 4.1000 | 3.5880 |
| 16 | 0.7842 | 0.7144 | 5.8550 | 4.8480 | 3.8690 | 3.4300 |
| 26 | 0.7369 | 0.6181 | 0.4356 | 4.7030 | 3.6670 | 3.2850 |
| 36 | 0.7100 | 0.5635 | 0.4290 | 0.4017 | 3.6440 | 3.2930 |
| 46 | 0.6500 | 0.5134 | 0.4085 | 0.3827 | 0.3137 | 3.2090 |
| 56 | 0.6048 | 0.4586 | 0.3721 | 0.3453 | 0.3064 | 0.2925 |
| 66 | 0.5004 | 0.3737 | 0.3101 | 0.2859 | 0.2646 | 0.2535 |
| 76 | 0.4048 | 0.3012 | 0.2518 | 0.2301 | 0.2128 | 0.2038 |
| 86 | 0.3182 | 0.2353 | 0.1982 | 0.1809 | 0.1674 | 0.1601 |
| 96 | 0.2582 | 0.1902 | 0.1603 | 0.1457 | 0.1343 | 0.1280 |
| 106 | 0.2108 | 0.1550 | 0.1307 | 0.1187 | 0.1093 | 0.1040 |
| 116 | 0.1688 | 0.1241 | 0.1047 | 0.0950 | 0.0873 | 0.0829 |
| 126 | 0.1242 | 0.0921 | 0.0770 | 0.0698 | 0.0641 | 0.0608 |
| 136 | 0.0874 | 0.0630 | 0.0538 | 0.0486 | 0.0445 | 0.0421 |
| 146 | 0.0606 | 0.0443 | 0.0372 | 0.0336 | 0.0307 | 0.0290 |
| 156 | 0.0387 | 0.0282 | 0.0235 | 0.0211 | 0.0193 | 0.0182 |
| 166 | 0.0224 | 0.0161 | 0.0133 | 0.0119 | 0.0108 | 0.0101 |
| 176 | 0.0119 | 0.0085 | 0.0069 | 0.0062 | 0.0055 | 0.0052 |
| 186 | 0.0056 | 0.0039 | 0.0031 | 0.0027 | 0.0024 | 0.0023 |
| 196 | 0.0012 | 0.0008 | 0.0006 | 0.0005 | 0.0004 | 0.0004 |
| 206 | -0.0016 | -0.0011 | -0.0009 | -0.0008 | -0.0007 | -0.0006 |
| 216 | -0.0027 | -0.0018 | -0.0013 | -0.0011 | -0.0009 | -0.0007 |

Table 6.2


Figure 6.4 Variation of major principal stress along radial line "EF" (For elliptical tunnel-3, $\mathrm{a} / \mathrm{b}=1.500$ )

VARIATION OF MAJOR PRINCIPAL STRESS ALONG RADIAL LINE "EF" (FOR ELLIPTICAL TUNNEL-3, $a / b=1.500$ )

| ELEMENT NUMBER | MAJOR PRINCIPAL STRESS $\times 10^{3}\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 10 | 1.4620 | 1.0500 | 7.9680 | 6.9480 | 6.3130 | 5.9540 |
| 20 | 1.3050 | 0.7786 | 6.4570 | 5.5680 | 5.0830 | 4.8010 |
| 30 | 1.1610 | 0.6947 | 0.5317 | 4.3630 | 4.0380 | 3.8260 |
| 40 | 1.0290 | 0.6245 | 0.4843 | 0.3970 | 3.1400 | 2.9980 |
| 50 | 0.9317 | 0.5675 | 0.4404 | 0.3626 | 0.3048 | 2.2000 |
| 60 | 0.7897 | 0.4883 | 0.3815 | 0.3176 | 0.2683 | 0.2402 |
| 70 | 0.6048 | 0.3815 | 0.2999 | 0.2526 | 0.2149 | 0.1918 |
| 80 | 0.4372 | 0.2829 | 0.2240 | 0.1909 | 0.1643 | 0.1481 |
| 90 | 0.3243 | 0.2141 | 0.1701 | 0.1459 | 0.1264 | 0.1147 |
| 100 | 0.2493 | 0.1672 | 0.1333 | 0.1150 | 0.1002 | 0.0915 |
| 110 | 0.1982 | 0.1342 | 0.1071 | 0.0926 | 0.0809 | 0.0741 |
| 120 | 0.1534 | 0.1048 | 0.0837 | 0.0726 | 0.0636 | 0.0584 |
| 130 | 0.1121 | 0.0770 | 0.0614 | 0.0532 | 0.0466 | 0.0428 |
| 140 | 0.0751 | 0.0520 | 0.0458 | 0.0362 | 0.0320 | 0.0296 |
| 150 | 0.0530 | 0.0366 | 0.0290 | 0.0251 | 0.0221 | 0.0204 |
| 160 | 0.0320 | 0.0221 | 0.0173 | 0.0149 | 0.0130 | 0.0120 |
| 170 | 0.0178 | 0.0122 | 0.0093 | 0.0079 | 0.0068 | 0.0063 |
| 180 | 0.0089 | 0.0059 | 0.0043 | 0.0036 | 0.0031 | 0.0030 |
| 190 | 0.0038 | 0.0024 | 0.0016 | 0.0013 | 0.0012 | 0.0014 |
| 200 | 0.0002 | -0.0713 | -0.0002 | -0.0002 | -0.0023 | 0.0004 |
| 210 | -0.0018 | -0.0013 | -0.0001 | -0.0008 | -0.0006 | -0.0003 |
| 220 | -0.0022 | -0.0014 | -0.0009 | -0.0006 | -0.0004 | -0.0003 |



Figure 6.5 Variation of minor principal stress along radial line "AB"
(For elliptical tunnel-3, $\mathrm{a} / \mathrm{b}=1.500$ )

VARIATION OF MINOR PRINCIPAL STRESS ALONG RADIAL LINE "AB" (FOR ELLIPTICAL TUNNEL-3, $\mathrm{a} / \mathrm{b}=1.500$ )

| ELEMENT NUMBER | MINOR PRINCIPAL STRESS $\times\left(-1 \times 10^{3}\right)\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 1 | 1.0020 | 1.0890 | 1.1130 | 1.0970 | 1.1070 | 1.1230 |
| 11 | 0.9551 | 0.8537 | 0.8046 | 0.8160 | 0.8523 | 0.8685 |
| 21 | 0.9380 | 0.8319 | 0.7890 | 0.8180 | 0.8821 | 0.9187 |
| 31 | 0.9046 | 0.7956 | 0.7500 | 0.7132 | 0.7444 | 0.7869 |
| 41 | 0.8850 | 0.7740 | 0.7278 | 0.6921 | 0.6824 | 0.7912 |
| 51 | 0.8310 | 0.7187 | 0.6704 | 0.6369 | 0.6284 | 0.6261 |
| 61 | 0.7307 | 0.6211 | 0.5748 | 0.5498 | 0.5364 | 0.5284 |
| 71 | 0.6190 | 0.5172 | 0.4757 | 0.4551 | 0.4403 | 0.4290 |
| 81 | 0.5181 | 0.4268 | 0.3912 | 0.3738 | 0.3594 | 0.3485 |
| 91 | 0.4364 | 0.3554 | 0.3253 | 0.3102 | 0.2970 | 0.2873 |
| 101 | 0.3711 | 0.2997 | 0.2740 | 0.2609 | 0.2490 | 0.2405 |
| 111 | 0.3059 | 0.2452 | 0.2240 | 0.2129 | 0.2027 | 0.1955 |
| 121 | 0.2407 | 0.1915 | 0.1748 | 0.1695 | 0.1575 | 0.1517 |
| 131 | 0.1848 | 0.1461 | 0.1333 | 0.1262 | 0.1195 | 0.1150 |
| 141 | 0.1419 | 0.1116 | 0.1017 | 0.0961 | 0.0909 | 0.0873 |
| 151 | 0.1049 | 0.0822 | 0.0748 | 0.0705 | 0.0666 | 0.0639 |
| 161 | 0.0794 | 0.0620 | 0.0563 | 0.0531 | 0.0500 | 0.0479 |
| 171 | 0.0619 | 0.0482 | 0.0437 | 0.0411 | 0.0387 | 0.0371 |
| 181 | 0.0513 | 0.0398 | 0.0361 | 0.0339 | 0.0319 | 0.0305 |
| 191 | 0.0440 | 0.0341 | 0.0309 | 0.0290 | 0.0272 | 0.0260 |
| 200 | 0.0121 | 0.0068 | 0.0033 | 0.0017 | 0.0007 | 0.0005 |
| 210 | 0.0106 | 0.0062 | 0.0034 | 0.0018 | 0.0011 | 0.0008 |

[^0]

Figure 6.6 Variation of minor principal stress along radial line "CD" (For elliptical tunnel-3, $\mathrm{a} / \mathrm{b}=1.500$ )

VARIATION OF MINOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" (FOR ELLIPTICAL TUNNEL-3, $\mathrm{a} / \mathrm{b}=1.500$ )

| ELEMENT NUMBER | MINOR PRINCIPAL STRESS $\times\left(-1 \times 10^{3}\right)\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 6 | 1.0450 | 0.6004 | 0.7902 | 0.8159 | 0.8749 | 0.8976 |
| 16 | 0.9792 | 0.7335 | 0.7847 | 0.7441 | 0.8044 | 0.8139 |
| 26 | 0.9285 | 0.6893 | 0.5849 | 0.6354 | 0.7079 | 0.7237 |
| 36 | 0.8046 | 0.6005 | 0.5231 | 0.4845 | 0.3844 | 0.4132 |
| 46 | 0.7772 | 0.5749 | 0.4922 | 0.4533 | 0.4216 | 0.3934 |
| 56 | 0.6766 | 0.5036 | 0.4345 | 0.4002 | 0.3732 | 0.3538 |
| 66 | 0.5571 | 0.4129 | 0.3529 | 0.3217 | 0.2974 | 0.2824 |
| 76 | 0.4367 | 0.3250 | 0.2780 | 0.2526 | 0.2334 | 0.2221 |
| 86 | 0.3439 | 0.2542 | 0.2150 | 0.1938 | 0.1775 | 0.1638 |
| 96 | 0.2752 | 0.2029 | 0.1710 | 0.1538 | 0.1405 | 0.1329 |
| 106 | 0.2285 | 0.1675 | 0.1403 | 0.1257 | 0.1144 | 0.1079 |
| 116 | 0.1837 | 0.1338 | 0.1113 | 0.0993 | 0.0900 | 0.0847 |
| 126 | 0.1390 | 0.1011 | 0.0840 | 0.0749 | 0.0679 | 0.0638 |
| 136 | 0.1070 | 0.0776 | 0.0632 | 0.0560 | 0.0503 | 0.0471 |
| 146 | 0.0799 | 0.0576 | 0.0473 | 0.0419 | 0.0377 | 0.0352 |
| 156 | 0.0970 | 0.0427 | 0.0347 | 0.0306 | 0.0273 | 0.0255 |
| 166 | 0.0443 | 0.0316 | 0.0255 | 0.0223 | 0.0198 | 0.0184 |
| 176 | 0.0345 | 0.0245 | 0.0196 | 0.0171 | 0.0152 | 0.0140 |
| 186 | 0.0285 | 0.0201 | 0.0161 | 0.0140 | 0.0123 | 0.0114 |
| 196 | 0.0338 | 0.0168 | 0.0133 | 0.0115 | 0.0102 | 0.0094 |
| 206 | 0.0205 | 0.0145 | 0.0115 | 0.0099 | 0.0087 | 0.0080 |
| 216 | 0.0183 | 0.0129 | 0.0102 | 0.0089 | 0.0078 | 0.0071 |

Table 6.5


Figure 6.7 Variation of minor principal stress along radial line "EF" (For elliptical tunnel-3, $\mathrm{a} / \mathrm{b}=1.500$ )

VARIATION OF MINOR PRINCIPAL STRESS ALONG RADIAL LINE "EF"
(FOR ELLIPTICAL TUNNEL-3, $\mathrm{a} / \mathrm{b}=1.500$ )

| ELEMENT NUMBER | MINOR PRINCIPAL STRESS $\left(-1 \times 10^{3}\right)\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | ---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 10 | 0.9234 | 0.4399 | 0.5236 | 0.5765 | 0.6123 | 0.6339 |
| 20 | 0.7544 | 0.2300 | 0.1588 | 0.2711 | 0.3332 | 0.3679 |
| 30 | 0.6593 | 0.2029 | 0.0239 | 0.0370 | 0.1163 | 0.1614 |
| 40 | 0.5925 | 0.1774 | 0.0109 | 0.0653 | 0.1639 | 0.1045 |
| 50 | 0.5103 | 0.1629 | 0.0177 | 0.0524 | 0.0988 | 0.7631 |
| 60 | 0.4243 | 0.1374 | 0.0120 | 0.0483 | 0.0892 | 0.1035 |
| 70 | 0.3129 | 0.1075 | 0.0098 | 0.0369 | 0.0692 | 0.0837 |
| 80 | 0.2184 | 0.0792 | 0.0064 | 0.0278 | 0.0516 | 0.0627 |
| 90 | 0.1584 | 0.0608 | 0.0055 | 0.0202 | 0.0382 | 0.0467 |
| 100 | 0.1215 | 0.0480 | 0.0039 | 0.0165 | 0.0307 | 0.0372 |
| 110 | 0.0972 | 0.0398 | 0.0039 | 0.0126 | 0.0242 | 0.0295 |
| 120 | 0.0770 | 0.0325 | 0.0037 | 0.0096 | 0.0189 | 0.0231 |
| 130 | 0.0584 | 0.0255 | 0.0034 | 0.0068 | 0.0138 | 0.0171 |
| 140 | 0.0436 | 0.0195 | 0.0029 | 0.0047 | 0.0099 | 0.0122 |
| 150 | 0.0339 | 0.0162 | 0.0039 | 0.0018 | 0.0056 | 0.0074 |
| 160 | 0.0254 | 0.0123 | 0.0030 | 0.0013 | 0.0043 | 0.0056 |
| 170 | 0.0197 | 0.0099 | 0.0030 | 0.0002 | 0.0024 | 0.0033 |
| 180 | 0.0161 | 0.0084 | 0.0031 | 0.0006 | 0.0010 | 0.0016 |
| 190 | 0.0140 | 0.0076 | 0.0032 | 0.0012 | 0.0001 | 0.0004 |
| 200 | 0.0121 | 0.0068 | 0.0033 | 0.0016 | 0.0007 | 0.0005 |
| 210 | 0.0106 | 0.0062 | 0.0034 | 0.0020 | 0.0011 | 0.0008 |
| 220 | 0.0095 | 0.0057 | 0.0033 | 0.0021 | 0.0012 | 0.0008 |

Table 6.6


Figure 6.8 Circumferential lines (For elliptical tunnel-3, $\mathrm{a} / \mathrm{b}=1.500$ )

No. of Nodes $=253$
No. of Elements $=230$


Figure 6.9 Variation of major principal stress along circumferential line " GH " (For elliptical tunnel-3, $a / b=1.500$ )

VARIATION OF MAJOR PRINCIPAL STRESS ALONG CIRCUMFERENTIAL LINE "GH" (FOR ELLIPTICAL TUNNEL3, $a / b=1.500$ )

| ELEMENT NUMBER | MAJOR PRINCIPAL STRESS $\times 10^{3}\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 51 | 0.3434 | 0.2930 | 0.2463 | 0.2069 | 0.1878 | 0.1811 |
| 52 | 0.3671 | 0.3110 | 0.2583 | 0.2218 | 0.2110 | 0.2293 |
| 53 | 0.3998 | 0.3317 | 0.2735 | 0.2426 | 0.2353 | 0.2288 |
| 54 | 0.4566 | 0.3711 | 0.3027 | 0.2784 | 0.2667 | 0.2430 |
| 55 | 0.5223 | 0.4133 | 0.3335 | 0.3109 | 0.2880 | 0.2672 |
| 56 | 0.6048 | 0.4586 | 0.3721 | 0.3453 | 0.3064 | 0.2925 |
| 57 | 0.6736 | 0.4881 | 0.4059 | 0.3737 | 0.3534 | 0.3460 |
| 58 | 0.7336 | 0.4978 | 0.4149 | 0.3741 | 0.3467 | 0.3418 |
| 59 | 0.7699 | 0.4972 | 0.4060 | 0.3601 | 0.3262 | 0.3200 |
| 60 | 0.7897 | 0.4883 | 0.3815 | 0.3176 | 0.2683 | 0.2402 |

Table 6.7


Figure 6.10 Variation of minor principal stress along circumferential line " GH " (For elliptical tunnel-3, $\mathrm{a} / \mathrm{b}=1.500$ )

VARIATION OF MINOR PRINCIPAL STRESS ALONG CIRCUMFERENTIAL LINE "GH" (FOR ELLIPTICAL TUNNEL3, $a / b=1.500$ )

| ELEMENT NUMBER | MINOR PRINCIPAL STRESS $\times 10^{3}\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 51 | 0.8310 | 0.7187 | 0.6704 | 0.6396 | 0.6284 | 0.6261 |
| 52 | 0.8176 | 0.7080 | 0.6561 | 0.6294 | 0.6109 | 0.5864 |
| 53 | 0.7951 | 0.6844 | 0.6279 | 0.6002 | 0.5797 | 0.5738 |
| 54 | 0.7501 | 0.6247 | 0.5659 | 0.5391 | 0.5198 | 0.5097 |
| 55 | 0.7358 | 0.5611 | 0.5067 | 0.4814 | 0.4567 | 0.4345 |
| 56 | 0.6766 | 0.5030 | 0.4345 | 0.4002 | 0.3732 | 0.3538 |
| 57 | 0.6148 | 0.4492 | 0.3537 | 0.3116 | 0.2713 | 0.2567 |
| 58 | 0.5132 | 0.3395 | 0.2406 | 0.1956 | 0.1674 | 0.1586 |
| 59 | 0.4562 | 0.2184 | 0.1058 | 0.0541 | 0.0231 | 0.0196 |
| 60 | 0.4243 | 0.1374 | 0.0120 | 0.0483 | 0.0892 | 0.1035 |

Table 6.8


Figure 6.11 Variation of " x " displacement along circumferential line " GH " (For elliptical tunnel-3, $\mathrm{a} / \mathrm{b}=1.500$ )

VARIATION OF "X" DISPLACEMENT ALONG CIRCUMFERENTIAL LINE "GH" (FOR ELLIPTICAL TUNNEL3, $\mathrm{a} / \mathrm{b}=1.500$ )

| NODE NUMBER | DISPLACEMEN $\times 10^{-3}(\mathrm{~m})$ |  |  |  |  |  |
| :---: | :---: | ---: | ---: | ---: | ---: | ---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 67 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 68 | 0.2210 | 0.1862 | 0.1606 | 0.1438 | 0.1361 | 0.1350 |
| 69 | 0.4154 | 0.3476 | 0.2967 | 0.2654 | 0.2497 | 0.2440 |
| 70 | 0.6156 | 0.5027 | 0.4201 | 0.3737 | 0.3484 | 0.3379 |
| 71 | 0.8069 | 0.6352 | 0.5155 | 0.4535 | 0.4145 | 0.3927 |
| 72 | 0.9831 | 0.7326 | 0.5679 | 0.4850 | 0.4262 | 0.3918 |
| 73 | 1.1110 | 0.7872 | 0.5687 | 0.4617 | 0.3806 | 0.3386 |
| 74 | 1.1780 | 0.7694 | 0.4959 | 0.3622 | 0.2614 | 0.2115 |
| 75 | 1.1980 | 0.6995 | 0.3852 | 0.2308 | 0.1171 | 0.0607 |
| 76 | 1.1810 | 0.6084 | 0.2706 | 0.1065 | -0.0135 | -0.0754 |
| 77 | 1.1690 | 0.5635 | 0.2175 | 0.0497 | -0.0723 | -0.0137 |

Table 6.9


Figure 6.12 Variation of " $y$ " displacement along circumferential line " GH " (For elliptical tunnel-3, $\mathrm{a} / \mathrm{b}=1.500$ )

VARIATION OF "Y" DISPLACEMENT CIRCUMFERENTIAL LINE "GH" (FOR ELLIPTICAL TUNNEL3, $\mathrm{a} / \mathrm{b}=1.500$ )

| NODE NUMBER | " $Y$ " DISPLACEMENT X10 ${ }^{-3}(\mathrm{~m})$ |  |  |  |  |  |
| :---: | :---: | ---: | ---: | ---: | ---: | ---: |
|  | LINER THICKNESS $(\mathrm{m})$ |  |  |  |  |  |
|  | $\mathrm{t}=0.0$ | $\mathrm{t}=0.2$ | $\mathrm{t}=0.4$ | $\mathrm{t}=0.6$ | $\mathrm{t}=0.8$ | $\mathrm{t}=1.0$ |
| 67 | 3.2030 | 2.5640 | 2.3230 | 2.1930 | 2.0850 | 2.0170 |
| 68 | 3.1650 | 2.5260 | 2.2850 | 2.1550 | 2.0450 | 1.9670 |
| 69 | 0.3080 | 2.4410 | 2.1980 | 2.0690 | 1.9530 | 1.8740 |
| 70 | 2.8600 | 2.2310 | 1.9930 | 1.8650 | 1.7490 | 1.6750 |
| 71 | 2.6040 | 1.9790 | 1.7500 | 1.6230 | 1.5060 | 1.1438 |
| 72 | 2.2220 | 1.6300 | 1.4170 | 1.2910 | 1.1810 | 1.1120 |
| 73 | 1.8510 | 1.3160 | 1.1110 | 0.9906 | 0.0886 | 0.8241 |
| 74 | 1.3340 | 0.9020 | 0.7312 | 0.6296 | 0.5434 | 0.4980 |
| 75 | 0.8911 | 0.5657 | 0.4381 | 0.3624 | 0.2991 | 0.2572 |
| 76 | 0.4476 | 0.2672 | 0.1980 | 0.1574 | 0.1242 | 0.1001 |
| 77 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |

Table 6.10


Figure 6.13 Variation of major principal stress with liner thickness
(For element number 51 )

| LINER THICKNESS $(\mathrm{m})$ | STRESS $\times 10^{3} \mathrm{kN} / \mathrm{m}^{2}$ |
| :---: | :---: |
| 0.00 | 0.3434 |
| 0.20 | 0.2930 |
| 0.40 | 0.2430 |
| 0.60 | 0.2069 |
| 0.80 | 0.1878 |
| 1.00 | 0.1811 |

Table 6.11


Figure 6.14 Variation of major principal stress with liner thickness (For element number 56)

| LINER THICKNESS $(\mathrm{m})$ | STRESS $\times 10^{3} \mathrm{kN} / \mathrm{m}^{2}$ |
| :---: | :---: |
| 0.00 | 0.6048 |
| 0.20 | 0.4586 |
| 0.40 | 0.3721 |
| 0.60 | 0.3453 |
| 0.80 | 0.3064 |
| 1.00 | 0.2925 |

Table 6.12


Figure 6.15 Variation of major principal stress with liner thickness (For element number 60)

| LINER THICKNESS $(\mathrm{m})$ | STRESS $\times 10^{3} \mathrm{kN} / \mathrm{m}^{2}$ |
| :---: | :---: |
| 0.00 | 0.7897 |
| 0.20 | 0.4883 |
| 0.40 | 0.3815 |
| 0.60 | 0.3176 |
| 0.80 | 0.2683 |
| 1.00 | 0.2402 |

Table 6.13

## CHAPTER 7.0

## INFLUENCE OF TUNNEL GEOMETRY ON STRESS IN ROCK AROUND ELLIPTICAL TUNNELS

Figures 7.1 to 7.12 indicate the influence of the tunnel geometry (the $a / b$ ratio) on the principal stress distribution in the rock mass, for different liner thicknesses. A distinct feature that can be seen from these figures is that the minimum stresses along the line CD are indicated for the tunnel with $a / b=1.156$. In most cases, the maximum stress is indicated for the tunnel with $a / b=1.358$, while tunnel with $a / b=1.500$ indicates intermediate values.

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Figure 7.1 Variation of major principal stress along radial line "CD"
(Without liner)

VARIATION OF MAJOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" (FOR LINER THICKNESS $t=0.0$ )

| ELEMENT NUMBER | MAJOR PRINCIPAL STRESS $\times 10^{3}\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |
| :---: | :---: | :---: | :---: |
|  | RATIO OF $\mathrm{a} / \mathrm{b}$ |  |  |
|  | $\mathrm{a} / \mathrm{b}=1.156$ | $\mathrm{a} / \mathrm{b}=1.358$ | $\mathrm{a} / \mathrm{b}=1.500$ |
| 6 | 0.8419 | 0.9991 | 0.7990 |
| 16 | 0.8378 | 0.7849 | 0.7842 |
| 26 | 0.7772 | 0.6593 | 0.7369 |
| 36 | 0.7279 | 0.5088 | 0.7100 |
| 46 | 0.7105 | 0.4056 | 0.6500 |
| 56 | 0.6402 | 0.3075 | 0.6048 |
| 66 | 0.5236 | 0.2323 | 0.5004 |
| 76 | 0.4089 | 0.1704 | 0.4048 |
| 86 | 0.3174 | 0.1169 | 0.3182 |
| 96 | 0.2519 | 0.0756 | 0.2582 |
| 106 | 0.2004 | 0.0490 | 0.2108 |
| 116 | 0.1677 | 0.0322 | 0.1688 |
| 126 | 0.1169 | 0.0203 | 0.1242 |
| 136 | 0.0830 | 0.0109 | 0.0874 |
| 146 | 0.0055 | 0.0035 | 0.0606 |
| 156 | 0.0359 | -0.0006 | 0.0387 |
| 166 | 0.0218 | -0.0032 | 0.0224 |
| 176 | 0.0128 | -0.0036 | 0.0119 |
| 186 | 0.0070 | -0.0056 | 0.0056 |

Table 7.1


Figure 7.2 Variation of major principal stress along radial line "CD"
(Liner thickness $(\mathrm{t})=0.2 \mathrm{~m})$

VARIATION OF MAJOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" (FOR LINER THICKNESS $\mathrm{t}=0.2 \mathrm{~m}$ )

| ELEMENT NUMBER | MAJOR PRINCIPAL STRESS $\times 10^{3}\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |
| :---: | :---: | :---: | :---: |
|  | RATIO OF $\mathrm{a} / \mathrm{b}$ |  |  |
|  | $\mathrm{a} / \mathrm{b}=1.156$ | $\mathrm{a} / \mathrm{b}=1.358$ | $\mathrm{a} / \mathrm{b}=1.500$ |
| 6 | 7.8140 | 8.2450 | 9.9410 |
|  | 0.5621 | 7.7680 | 0.7144 |
| 16 | 0.5275 | 0.5535 | 0.6181 |
| 26 | 0.4909 | 0.4726 | 0.5635 |
| 36 | 0.4805 | 0.3684 | 0.5134 |
| 46 | 0.4385 | 0.2998 | 0.4586 |
| 56 | 0.3593 | 0.2303 | 0.3737 |
| 66 | 0.2818 | 0.1752 | 0.3012 |
| 76 | 0.2191 | 0.1288 | 0.2353 |
| 86 | 0.1740 | 0.0882 | 0.1902 |
| 96 | 0.1381 | 0.0567 | 0.1550 |
| 106 | 0.1158 | 0.0365 | 0.1241 |
| 116 | 0.0802 | 0.0148 | 0.0921 |
| 126 | 0.0570 | 0.0077 | 0.0630 |
| 136 | 0.0377 | 0.0023 | 0.0443 |
| 146 | 0.0246 | -0.0007 | 0.0282 |
| 156 | 0.0149 | -0.0024 | 0.0161 |
| 166 | 0.0088 | -0.0025 | 0.0085 |
| 176 | 0.0048 | -0.0004 | 0.0039 |
| 186 |  |  |  |

Table 7.2


Figure 7.3 Variation of major principal stress along radial line "CD"
(Liner thickness $(\mathrm{t})=0.4 \mathrm{~m})$

VARIATION OF MAJOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" (FOR LINER THICKNESS $\mathrm{t}=0.4 \mathrm{~m}$ )

| ELEMENT NUMBER | MAJOR PRINCIPAL STRESS $\times 10^{3}\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |
| :---: | :---: | :---: | :---: |
|  | RATIO OF $\mathrm{a} / \mathrm{b}$ |  |  |
|  | $\mathrm{a} / \mathrm{b}=1.156$ | $\mathrm{a} / \mathrm{b}=1.358$ | $\mathrm{a} / \mathrm{b}=1.500$ |
|  | 5.5030 | 5.3120 | 6.2190 |
| 6 | 5.4820 | 0.3944 | 5.8550 |
| 16 | 0.3975 | 0.3947 | 0.4356 |
| 26 | 0.3830 | 0.3231 | 0.4290 |
| 36 | 0.3802 | 0.2524 | 0.4085 |
| 46 | 0.3485 | 0.1901 | 0.3721 |
| 56 | 0.2893 | 0.1428 | 0.3101 |
| 66 | 0.2273 | 0.1041 | 0.2518 |
| 76 | 0.1767 | 0.0708 | 0.1982 |
| 86 | 0.1401 | 0.0405 | 0.1603 |
| 96 | 0.1110 | 0.0288 | 0.1307 |
| 106 | 0.0931 | 0.0185 | 0.1047 |
| 116 | 0.0644 | 0.0112 | 0.0770 |
| 126 | 0.0457 | 0.0057 | 0.0538 |
| 136 | 0.0302 | 0.0014 | 0.0372 |
| 146 | 0.0169 | -0.0007 | 0.0235 |
| 156 | 0.0118 | -0.0002 | 0.0133 |
| 166 | 0.0069 | -0.0019 | 0.0069 |
| 176 | 0.0037 | -0.0011 | 0.0031 |
| 186 |  |  |  |

Table 7.3


Figure 7.4 Variation of major principal stress along radial line "CD"
(Liner thickness $(\mathrm{t})=0.6 \mathrm{~m})$

VARIATION OF MAJOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" (FOR LINER THICKNESS $\mathrm{t}=0.6 \mathrm{~m}$ )

| ELEMENT NUMBER | MAJOR PRINCIPAL STRESS $\times 10^{3}\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |
| :---: | :---: | :---: | :---: |
|  | RATIO OF $\mathrm{a} / \mathrm{b}$ |  |  |
|  | $\mathrm{a} / \mathrm{b}=1.156$ | $\mathrm{a} / \mathrm{b}=1.358$ | $\mathrm{a} / \mathrm{b}=1.500$ |
| 6 | 4.0300 | 4.4850 | 5.0880 |
| 16 | 4.2230 | 4.1330 | 4.8480 |
| 26 | 4.3780 | 0.3288 | 4.7030 |
| 36 | 0.3350 | 0.2764 | 0.4017 |
| 46 | 0.3296 | 0.2211 | 0.3827 |
| 56 | 0.2936 | 0.1677 | 0.3453 |
| 66 | 0.2390 | 0.1260 | 0.2859 |
| 76 | 0.1687 | 0.0917 | 0.2301 |
| 86 | 0.1447 | 0.0621 | 0.1809 |
| 96 | 0.1146 | 0.0393 | 0.1457 |
| 106 | 0.0906 | 0.0249 | 0.1187 |
| 116 | 0.0760 | 0.0158 | 0.0950 |
| 126 | 0.0527 | 0.0094 | 0.0698 |
| 136 | 0.0372 | 0.0046 | 0.0486 |
| 146 | 0.0245 | 0.0009 | 0.0336 |
| 156 | 0.0159 | -0.0008 | 0.0211 |
| 166 | 0.0095 | -0.0017 | 0.0119 |
| 176 | 0.0055 | -0.0015 | 0.0062 |
| 186 | 0.0029 | -0.0007 | 0.0027 |

Table 7.4


Figure 7.5 Variation of major principal stress along radial line "CD"
(Liner thickness $(\mathrm{t})=0.8 \mathrm{~m})$

VARIATION OF MAJOR PRINCIPAL STRESS ALONG RADIAL LINE "CD"
(FOR LINER THICKNESS $\mathrm{t}=0.8 \mathrm{~m}$ )

| ELEMENT NUMBER | MAJOR PRINCIPAL STRESS $\times 10^{3}\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |
| :---: | :---: | :---: | :---: |
|  | RATIO OF $\mathrm{a} / \mathrm{b}$ |  |  |
|  | $\mathrm{a} / \mathrm{b}=1.156$ | $\mathrm{a} / \mathrm{b}=1.358$ | $\mathrm{a} / \mathrm{b}=1.500$ |
| 6 | 3.6300 | 3.9790 | 0.8749 |
| 16 | 3.7690 | 3.7910 | 0.8044 |
|  | 3.8920 | 0.3220 | 0.7079 |
| 36 | 3.9210 | 0.2650 | 0.3844 |
|  | 0.2938 | 0.2072 | 0.4216 |
| 56 | 0.2678 | 0.1552 | 0.3732 |
| 66 | 0.2219 | 0.1159 | 0.2974 |
| 76 | 0.1741 | 0.0840 | 0.2334 |
| 86 | 0.1349 | 0.0567 | 0.1775 |
| 96 | 0.1067 | 0.0356 | 0.1405 |
| 106 | 0.0843 | 0.0225 | 0.1144 |
| 116 | 0.0707 | 0.1410 | 0.0900 |
| 126 | 0.0489 | 0.0083 | 0.0679 |
| 136 | 0.0345 | 0.0040 | 0.0503 |
| 146 | 0.0227 | 0.0007 | 0.0377 |
| 156 | 0.0147 | -0.0008 | 0.0273 |
| 166 | 0.0088 | -0.0015 | 0.0198 |
| 176 | 0.0051 | -0.0012 | 0.0152 |
| 186 | 0.0027 | 0.0005 | 0.0123 |

Table 7.5


Figure 7.6 Variation of major principal stress along radial line "CD" $($ Liner thickness $(t)=1.0 \mathrm{~m})$

VARIATION OF MAJOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" (FOR LINER THICKNESS $\mathrm{t}=1.0 \mathrm{~m}$ )

| ELEMENT NUMBER | MAJOR PRINCIPAL STRESS $\times 10^{3}\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |
| :---: | :---: | :---: | :---: |
|  | RATIO OF $\mathrm{a} / \mathrm{b}$ |  |  |
|  | $\mathrm{a} / \mathrm{b}=1.156$ | $\mathrm{a} / \mathrm{b}=1.358$ | $\mathrm{a} / \mathrm{b}=1.500$ |
| 6 | 3.1300 | 3.5370 | 0.8976 |
| 16 | 3.2830 | 3.2930 | 0.8139 |
| 26 | 3.4350 | 0.2964 | 0.7237 |
| 36 | 3.5120 | 0.2560 | 0.4132 |
| 46 | 3.7070 | 0.1986 | 0.3934 |
|  | 0.2597 | 0.1465 | 0.3538 |
| 66 | 0.2079 | 0.1086 | 0.2824 |
| 76 | 0.1610 | 0.0783 | 0.2221 |
| 86 | 0.1243 | 0.0526 | 0.1638 |
| 96 | 0.09811 | 0.0329 | 0.1329 |
| 106 | 0.0773 | 0.0277 | 0.1079 |
| 116 | 0.0659 | 0.0129 | 0.0847 |
| 126 | 0.0448 | 0.0075 | 0.0638 |
| 136 | 0.0316 | 0.0036 | 0.0471 |
| 146 | 0.0208 | 0.0005 | 0.0352 |
| 156 | 0.0134 | -0.0007 | 0.0255 |
| 166 | 0.0080 | -0.0013 | 0.0184 |
| 176 | 0.0046 | -0.0010 | 0.0140 |
| 186 | 0.0024 | -0.0004 | 0.0114 |

Table 7.6


Figure 7.7 Variation of minor principal stress along radial line "CD"
(Without liner)

VARIATION OF MINOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" (FOR LINER THICKNESS $\mathrm{t}=0.0 \mathrm{~m}$ )

| ELEMENT NUMBER | MINOR PRINCIPAL STRESS $\times\left(-1 \times 10^{3}\right)\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |
| :---: | :---: | :---: | :---: |
|  | RATIO OF $\mathrm{a} / \mathrm{b}$ |  |  |
|  | $\mathrm{a} / \mathrm{b}=1.156$ | $\mathrm{a} / \mathrm{b}=1.358$ | $\mathrm{a} / \mathrm{b}=1.500$ |
| 6 | 1.0850 | 0.8335 | 1.0450 |
| 16 | 0.9754 | 0.8354 | 0.9792 |
| 26 | 0.8958 | 0.6888 | 0.9285 |
| 36 | 0.8535 | 0.5920 | 0.8046 |
| 46 | 0.7975 | 0.4716 | 0.7772 |
| 56 | 0.7122 | 0.3661 | 0.6766 |
| 66 | 0.5767 | 0.2875 | 0.5571 |
| 76 | 0.4425 | 0.2218 | 0.4367 |
| 86 | 0.3437 | 0.1674 | 0.3439 |
| 96 | 0.2738 | 0.1272 | 0.2752 |
| 106 | 0.2246 | 0.0987 | 0.2285 |
| 116 | 0.1746 | 0.0884 | 0.1837 |
| 126 | 0.1440 | 0.0716 | 0.1390 |
| 136 | 0.1033 | 0.0607 | 0.1070 |
| 146 | 0.0780 | 0.0528 | 0.0799 |
| 156 | 0.0591 | 0.0453 | 0.0970 |
| 166 | 0.0460 | 0.0396 | 0.0443 |
| 176 | 0.0372 | 0.0337 | 0.0345 |
| 186 | 0.0315 | 0.0240 | 0.0285 |

Table 7.7


Figure 7.8 Variation of minor principal stress along radial line "CD" $($ Liner thickness $(t)=0.2 \mathrm{~m})$

VARIATION OF MINOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" (FOR LINER THICKNESS $\mathrm{t}=0.2 \mathrm{~m}$ )

| ELEMENT NUMBER | MINOR PRINCIPAL STRESS $\times\left(-1 \times 10^{3}\right)\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |
| :---: | :---: | :---: | :---: |
|  | RATIO OF $\mathrm{a} / \mathrm{b}$ |  |  |
|  | $\mathrm{a} / \mathrm{b}=1.156$ | $\mathrm{a} / \mathrm{b}=1.358$ | $\mathrm{a} / \mathrm{b}=1.500$ |
| 6 | 0.7854 | 0.4562 | 0.6004 |
|  | 0.7463 | 0.7242 | 0.7335 |
| 26 | 0.6783 | 0.5519 | 0.6893 |
| 36 | 0.6600 | 0.4761 | 0.6005 |
| 46 | 0.6058 | 0.3758 | 0.5749 |
| 56 | 0.5381 | 0.2896 | 0.5036 |
| 66 | 0.4319 | 0.2246 | 0.4129 |
| 76 | 0.3268 | 0.1713 | 0.3250 |
| 86 | 0.2506 | 0.1279 | 0.2542 |
| 96 | 0.1973 | 0.0959 | 0.2029 |
| 106 | 0.1604 | 0.0738 | 0.1675 |
| 116 | 0.1234 | 0.0628 | 0.1338 |
| 126 | 0.1013 | 0.0532 | 0.1011 |
| 136 | 0.0719 | 0.0449 | 0.0776 |
| 146 | 0.0540 | 0.0390 | 0.0576 |
| 156 | 0.0407 | 0.0333 | 0.0427 |
| 166 | 0.0316 | 0.0292 | 0.0316 |
| 176 | 0.0255 | 0.0247 | 0.0245 |
| 186 | 0.0215 | 0.0319 | 0.0201 |

Table 7.8


Figure 7.9 Variation of minor principal stress along radial line "CD" $($ Liner thickness $(\mathrm{t})=0.4 \mathrm{~m})$

VARIATION OF MINOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" (FOR LINER THICKNESS $\mathrm{t}=0.4 \mathrm{~m}$ )

| ELEMENT NUMBER | MINOR PRINCIPAL STRESS $\times\left(-1 \times 10^{3}\right)\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |
| :---: | :---: | :---: | :---: |
|  | RATIO OF $\mathrm{a} / \mathrm{b}$ |  |  |
|  | $\mathrm{a} / \mathrm{b}=1.156$ | $\mathrm{a} / \mathrm{b}=1.358$ | $\mathrm{a} / \mathrm{b}=1.500$ |
| 6 | 0.8850 | 0.6347 | 0.7902 |
|  | 0.7886 | 0.6399 | 0.7847 |
| 26 | 0.5752 | 0.4629 | 0.5849 |
| 36 | 0.5525 | 0.4696 | 0.5231 |
| 46 | 0.5114 | 0.3019 | 0.4922 |
| 56 | 0.4502 | 0.2300 | 0.4345 |
| 66 | 0.3581 | 0.1768 | 0.3529 |
| 76 | 0.2683 | 0.1345 | 0.2780 |
| 86 | 0.2041 | 0.1004 | 0.2150 |
| 96 | 0.1597 | 0.0749 | 0.1710 |
| 106 | 0.1292 | 0.5770 | 0.1403 |
| 116 | 0.9830 | 0.0490 | 0.1113 |
| 126 | 0.0810 | 0.0415 | 0.0840 |
| 136 | 0.0571 | 0.0350 | 0.0632 |
| 146 | 0.0428 | 0.0304 | 0.0473 |
| 156 | 0.0322 | 0.0250 | 0.0347 |
| 166 | 0.0249 | 0.0227 | 0.0255 |
| 176 | 0.0200 | 0.0191 | 0.0196 |
| 186 | 0.0169 | 0.0161 | 0.0161 |

Table 7.9


Figure 7.10 Variation of minor principal stress along radial line "CD" $($ Liner thickness $(t)=0.6 \mathrm{~m})$

VARIATION OF MINOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" (FOR LINER THICKNESS $t=0.6 \mathrm{~m}$ )

| ELEMENT NUMBER | MINOR PRINCIPAL STRESS $\times\left(-1 \times 10^{3}\right)\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |
| :---: | :---: | :---: | :---: |
|  | RATIO OF $\mathrm{a} / \mathrm{b}$ |  |  |
|  | $\mathrm{a} / \mathrm{b}=1.156$ | $\mathrm{a} / \mathrm{b}=1.358$ | $\mathrm{a} / \mathrm{b}=1.500$ |
|  | 0.9362 | 0.6632 | 0.8159 |
|  | 0.8078 | 0.5000 | 0.7441 |
|  | 0.5255 | 0.4246 | 0.6354 |
|  | 0.4731 | 0.3479 | 0.4845 |
| 46 | 0.4286 | 0.2667 | 0.4533 |
| 56 | 0.3748 | 0.2024 | 0.4002 |
| 66 | 0.2949 | 0.1548 | 0.3217 |
| 76 | 0.2191 | 0.1172 | 0.2526 |
| 86 | 0.1657 | 0.0715 | 0.1938 |
| 96 | 0.1290 | 0.0645 | 0.1538 |
| 106 | 0.1041 | 0.0495 | 0.1257 |
| 116 | 0.0784 | 0.0420 | 0.0993 |
| 126 | 0.0656 | 0.0355 | 0.0749 |
| 136 | 0.0456 | 0.0298 | 0.0560 |
| 146 | 0.0341 | 0.0259 | 0.0419 |
| 156 | 0.0256 | 0.0220 | 0.0306 |
| 166 | 0.0197 | 0.0193 | 0.0223 |
| 176 | 0.0158 | 0.0161 | 0.0171 |
| 186 | 0.0133 | 0.0134 | 0.0140 |

Table 7.10


Figure 7.11 Variation of minor principal stress along radial line "CD" (Liner thickness $(\mathrm{t})=0.8 \mathrm{~m})$

VARIATION OF MINOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" (FOR LINER THICKNESS $\mathrm{t}=0.8 \mathrm{~m}$ )

| ELEMENT NUMBER | MINOR PRINCIPAL STRESS $\times\left(-1 \times 10^{3}\right)\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |
| :---: | :---: | :---: | :---: |
|  | RATIO OF $\mathrm{a} / \mathrm{b}$ |  |  |
|  | $\mathrm{a} / \mathrm{b}=1.156$ | $\mathrm{a} / \mathrm{b}=1.358$ | $\mathrm{a} / \mathrm{b}=1.500$ |
| 6 | 0.9583 | 0.6885 | 0.8749 |
| 16 | 0.8300 | 0.4903 | 0.8044 |
|  | 0.5930 | 0.3872 | 0.7079 |
| 36 | 0.5859 | 0.3230 | 0.3844 |
| 46 | 0.3897 | 0.2448 | 0.4216 |
| 56 | 0.3426 | 0.1845 | 0.3732 |
| 66 | 0.2715 | 0.1403 | 0.2974 |
| 76 | 0.2024 | 0.1059 | 0.2334 |
| 86 | 0.1531 | 0.0786 | 0.1775 |
| 96 | 0.1192 | 0.0579 | 0.1405 |
| 106 | 0.0962 | 0.0443 | 0.1144 |
| 116 | 0.0723 | 0.0375 | 0.0900 |
| 126 | 0.0601 | 0.0317 | 0.0679 |
| 136 | 0.0421 | 0.0265 | 0.0503 |
| 146 | 0.0316 | 0.0231 | 0.0377 |
| 156 | 0.0237 | 0.0196 | 0.0273 |
| 166 | 0.0183 | 0.0172 | 0.0198 |
| 176 | 0.0146 | 0.0142 | 0.0152 |
| 186 | 0.0123 | 0.0005 | 0.0123 |

Table 7.11


Figure 7.12 Variation of minor principal stress along radial line "CD" $($ Liner thickness $(t)=1.0 \mathrm{~m})$

VARIATION OF MINOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" (FOR LINER THICKNESS $\mathrm{t}=1.0 \mathrm{~m}$ )

| ELEMENT NUMBER | MINOR PRINCIPAL STRESS $\times\left(-1 \times 10^{3}\right)\left(\mathrm{kN} / \mathrm{m}^{2}\right)$ |  |  |
| :---: | :---: | :---: | :---: |
|  | RATIO OF $\mathrm{a} / \mathrm{b}$ |  |  |
|  | $\mathrm{a} / \mathrm{b}=1.156$ | $\mathrm{a} / \mathrm{b}=1.358$ | $\mathrm{a} / \mathrm{b}=1.500$ |
| 6 | 0.9813 | 0.7096 | 0.8976 |
| 16 | 0.8445 | 0.4717 | 0.8139 |
| 26 | 0.6218 | 0.3651 | 0.7237 |
| 36 | 0.5866 | 0.3107 | 0.4132 |
| 46 | 0.3768 | 0.2308 | 0.3934 |
| 56 | 0.3126 | 0.1719 | 0.3538 |
| 66 | 0.2461 | 0.1297 | 0.2824 |
| 76 | 0.1836 | 0.0975 | 0.2221 |
| 86 | 0.1388 | 0.0721 | 0.1638 |
| 96 | 0.1081 | 0.0529 | 0.1329 |
| 106 | 0.0872 | 0.0404 | 0.1079 |
| 116 | 0.0653 | 0.0341 | 0.0847 |
| 126 | 0.0545 | 0.0288 | 0.0638 |
| 136 | 0.0381 | 0.0241 | 0.0471 |
| 146 | 0.0386 | 0.0209 | 0.0352 |
| 156 | 0.0214 | 0.0177 | 0.0255 |
| 166 | 0.0165 | 0.0156 | 0.0184 |
| 176 | 0.0132 | 0.0128 | 0.0140 |
| 186 | 0.0112 | 0.0106 | 0.0114 |

Table 7.12

## CHAPTER 8.0

## INFLUENCE OF STIFFNESS OF ROCK ON STRESS AND DEFORMATION IN ROCK SURROUNDING ELLIPTICAL TUNNELS

Figures 8.1 and 8.2 show that stronger rock carries a larger stress than a weaker rock. This implies that for weaker rock, the concrete lining will take most of the imposed load, and will experience higher stress magnitudes than in the case of stronger rock.

Figures 8.5 and 8.6 show that the displacements in rock reduce as the stiffness of rock increases. The numerical results show that this amount of reduction depends on the location of the point, the $E_{c} / E_{\mathrm{r}}$ ratio, and the tunnel thickness.

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Number nodes $=253$
Number of elements $=230$
$(\mathrm{a} / \mathrm{b}=1.500)$

| RATIO OF | A/B |
| :---: | :---: |
| $\mathrm{Ec} / \mathrm{Er}=100$ | $\cdots$ |
| $\mathrm{Ec} / \mathrm{Er}=50$ |  |
| $\mathrm{Ec} / \mathrm{Er}=20$ |  |
| $\mathrm{Ec} / \mathrm{Er}=10$ |  |
| $\mathrm{Ec} / \mathrm{Er}=5$ |  |
| SCALE $1 \mathrm{~cm}=168$ | $\mathrm{kN} / \mathrm{m} 2$ |

Figure 8.1 Variation of major principal stress along radial line "CD"
$($ Liner thickness $(t)=0.2 \mathrm{~m})$

VARIATION OF MAJOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" (FOR FOR ELLIPTICAL TUNNEL $-3, a / b=1.500$ )
(LINER THICKNESS $=0.2 \mathrm{~m}$ )

| ELEMENT NUMBER | MAJOR PRINCIPAL STRESS $\times 10^{3} \mathrm{kN} / \mathrm{m}^{2}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | RATIO OF $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}$ |  |  |  |  |
|  | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=5$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=10$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=20$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=50$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=100$ |
| 6 | 5.4360 | 9.9410 | 15.6800 | 23.1300 | 27.2800 |
| 16 | 0.8044 | 0.7144 | 0.5642 | 0.3555 | 0.2473 |
| 26 | 0.7036 | 0.6181 | 0.4916 | 0.3243 | 0.2402 |
| 36 | 0.6491 | 0.5635 | 0.4465 | 0.2971 | 0.2227 |
| 46 | 0.5919 | 0.5134 | 0.4099 | 0.2808 | 0.2180 |
| 56 | 0.5317 | 0.4586 | 0.3664 | 0.2543 | 0.2003 |
| 66 | 0.4335 | 0.3737 | 0.3011 | 0.2159 | 0.1759 |
| 76 | 0.3500 | 0.3012 | 0.2439 | 0.1782 | 0.1476 |
| 86 | 0.2727 | 0.2353 | 0.1920 | 0.1434 | 0.1214 |
| 96 | 0.2207 | 0.1902 | 0.1554 | 0.1168 | 0.0994 |
| 106 | 0.1799 | 0.1550 | 0.1267 | 0.0959 | 0.0824 |
| 116 | 0.1441 | 0.1241 | 0.1015 | 0.0770 | 0.0664 |
| 126 | 0.1059 | 0.0912 | 0.0747 | 0.0570 | 0.0495 |
| 136 | 0.0744 | 0.0640 | 0.0522 | 0.0395 | 0.0343 |
| 146 | 0.0516 | 0.0443 | 0.0361 | 0.0272 | 0.0235 |
| 156 | 0.0329 | 0.0282 | 0.0228 | 0.1710 | 0.0149 |
| 166 | 0.0189 | 0.0162 | 0.0129 | 0.0094 | 0.0082 |
| 176 | 0.0101 | 0.0085 | 0.0067 | 0.0048 | 0.0041 |
| 186 | 0.0047 | 0.0039 | 0.0030 | 0.0021 | 0.0081 |
| 196 | 0.0009 | 0.0008 | 0.0005 | 0.0003 | 0.0004 |
| 206 | -0.0132 | -0.0001 | -0.0009 | -0.0004 | -0.0001 |
| 216 | -0.0227 | -0.0018 | -0.0013 | -0.0005 | -0.0008 |

Table 8.1


Figure 8.2 Variation of minor principal stress along radial line "CD" (Liner thickness $(\mathrm{t})=0.2 \mathrm{~m})$

VARIATION OF MINOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" (FOR FOR ELLIPTICAL TUNNEL $-3, a / b=1.500$ )
(LINER THICKNESS $=0.2 \mathrm{~m}$ )

| ELEMENT NUMBER | MINOR PRINCIPAL STRESS $\times\left(-1 \times 10^{3}\right) \mathrm{kN} / \mathrm{m}^{2}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | RATIO OF $E_{C} / E_{R}$ |  |  |  |  |
|  | $E_{C} / E_{R}=5$ | $E_{C} / E_{R}=10$ | $E_{C} / E_{R}=20$ | $E_{C} / E_{R}=50$ | $E_{C} / E_{R}=100$ |
| 6 | 0.8205 | 0.6004 | 0.3280 | 0.5300 | 0.3899 |
| 16 | 0.8380 | 0.7335 | 0.6099 | 0.4554 | 0.3698 |
| 26 | 0.7893 | 0.6893 | 0.5705 | 0.4204 | 0.3362 |
| 36 | 0.6869 | 0.6005 | 0.4997 | 0.3767 | 0.3106 |
| 46 | 0.6604 | 0.5749 | 0.4753 | 0.3532 | 0.2872 |
| 56 | 0.5775 | 0.5036 | 0.4176 | 0.3138 | 0.2588 |
| 66 | 0.4757 | 0.4129 | 0.3399 | 0.2528 | 0.2078 |
| 76 | 0.3743 | 0.3250 | 0.2679 | 0.0228 | 0.1668 |
| 86 | 0.2943 | 0.2542 | 0.2075 | 0.1534 | 0.1266 |
| 96 | 0.2354 | 0.2029 | 0.1652 | 0.1218 | 0.1007 |
| 106 | 0.1950 | 0.1675 | 0.1355 | 0.0991 | 0.0817 |
| 116 | 0.1564 | 0.1338 | 0.1075 | 0.0776 | 0.0635 |
| 126 | 0.1183 | 0.1011 | 0.0812 | 0.0585 | 0.0481 |
| 136 | 0.0907 | 0.0770 | 0.0610 | 0.0427 | 0.0342 |
| 146 | 0.0678 | 0.0576 | 0.0457 | 0.0319 | 0.0255 |
| 156 | 0.0505 | 0.0427 | 0.0335 | 0.0228 | 0.0177 |
| 166 | 0.0375 | 0.0316 | 0.0245 | 0.0162 | 0.0122 |
| 176 | 0.0291 | 0.0245 | 0.0189 | 0.0122 | 0.0088 |
| 186 | 0.0240 | 0.0201 | 0.0155 | 0.0097 | 0.0068 |
| 196 | 0.0201 | 0.0107 | 0.0128 | 0.0080 | 0.0054 |
| 206 | 0.0173 | 0.0145 | 0.0110 | 0.0067 | 0.0045 |
| 216 | 0.0154 | 0.0129 | 0.0098 | 0.0060 | 0.0039 |

Table 8.2


Figure 8.3 Variation of major principal stress along circumferential line "CD" (Liner thickness $(\mathrm{t})=0.2 \mathrm{~m}$ )

VARIATION OF MAJOR PRINCIPAL STRESS ALONG CIRCUMFERENTIAL LINE "GH" (FOR FOR ELLIPTICAL TUNNEL - 3, $\mathrm{a} / \mathrm{b}=1.500$ )
(LINER THICKNESS $=0.2 \mathrm{~m}$ )

| NODE NUMBER | MAJOR PRINCIPAL STRESS $\times 10^{3} \mathrm{kN} / \mathrm{m}^{2}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | RATIO OF $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}$ |  |  |  |  |
|  | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=5$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=10$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=20$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=50$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=100$ |
| 51 | 0.3319 | 0.2930 | 0.2253 | 0.1200 | 0.0565 |
| 52 | 0.3518 | 0.3110 | 0.2414 | 0.1340 | 0.0698 |
| 53 | 0.3764 | 0.3317 | 0.2594 | 0.1519 | 0.0894 |
| 54 | 0.4232 | 0.3711 | 0.2930 | 0.1830 | 0.1220 |
| 55 | 0.4744 | 0.4133 | 0.3285 | 0.2170 | 0.1589 |
| 56 | 0.5317 | 0.4580 | 0.3664 | 0.2543 | 0.2003 |
| 57 | 0.5699 | 0.4881 | 0.3952 | 0.2922 | 0.2474 |
| 58 | 0.5921 | 0.4978 | 0.4021 | 0.3102 | 0.2788 |
| 59 | 0.6045 | 0.4972 | 0.3933 | 0.3098 | 0.3019 |
| 60 | 0.6094 | 0.4883 | 0.3660 | 0.2565 | 0.2793 |

Table 8.3


Figure 8.4 Variation of minor principal stress along circumferential line "CD" (Liner thickness $(t)=0.2 \mathrm{~m})$

VARIATION OF MINOR PRINCIPAL STRESS ALONG CIRCUMFERENTIAL LINE "GH" (FOR FOR ELLIPTICAL TUNNEL - $3, \mathrm{a} / \mathrm{b}=1.500$ )
(LINER THICKNESS $=0.2 \mathrm{~m}$ )

| NODE NUMBER | MINOR PRINCIPAL STRESS $\times 10^{3} \mathrm{kN} / \mathrm{m}^{2}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | RATIO OF $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}$ |  |  |  |  |
|  | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=5$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=10$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=20$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=50$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=100$ |
| 51 | 0.7619 | 0.7187 | 0.6586 | 0.5822 | 0.5356 |
| 52 | 0.7584 | 0.7080 | 0.6463 | 0.5663 | 0.5176 |
| 53 | 0.7379 | 0.6844 | 0.6174 | 0.5308 | 0.4794 |
| 54 | 0.6843 | 0.6247 | 0.5527 | 0.4642 | 0.4143 |
| 55 | 0.6311 | 0.5611 | 0.4820 | 0.3892 | 0.3390 |
| 56 | 0.5775 | 0.5036 | 0.4176 | 0.3138 | 0.2588 |
| 57 | 0.5278 | 0.4492 | 0.3515 | 0.2303 | 0.1689 |
| 58 | 0.4247 | 0.3395 | 0.2349 | 0.1139 | 0.0636 |
| 59 | 0.3270 | 0.2184 | 0.0943 | 0.1070 | 0.0512 |
| 60 | 0.2634 | 0.1374 | 0.0614 | 0.1496 | 0.0136 |

Table 8.4

Number nodes $=253$
Number of elements $=230$
$(\mathrm{a} / \mathrm{b}=1.500)$

| RATIO OF A/B |
| :---: |
| $\mathrm{Ec} / \mathrm{Er}=100$ |
| $\mathrm{Ec} / \mathrm{Er}=50$ |
| $\mathrm{Ec} / \mathrm{Er}=20$ |
| $\mathrm{Ec} / \mathrm{Er}=10$ |
| $\mathrm{Ec} / \mathrm{Er}=5$ |

SCALE $1 \mathrm{~cm}=0.43 \times 10^{-}-3 \mathrm{~m}$

Figure 8.5 Variation of " $x$ " displacement along circumferential line " GH " $($ Liner thickness $(t)=0.2 \mathrm{~m})$

VARIATION OF "X" DISPLACEMENTS ALONG CIRCUMFERENTIAL LINE "GH" (FOR FOR ELLIPTICAL TUNNEL - $3, \mathrm{a} / \mathrm{b}=1.500$ )
(LINER THICKNESS $=0.2 \mathrm{~m}$ )

| NODE NUMBER | " X ' DISPLACEMENTS $\times 10^{-3}(\mathrm{~m})$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | RATIO OF $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}$ |  |  |  |  |
|  | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=5$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=10$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=20$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=50$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=100$ |
| 67 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 68 | 0.1038 | 0.1862 | 0.3063 | 0.5211 | 0.7491 |
| 69 | 0.1947 | 0.3476 | 0.5659 | 0.9366 | 1.3010 |
| 70 | 0.2851 | 0.5027 | 0.8013 | 1.2610 | 1.6430 |
| 71 | 0.3670 | 0.6352 | 0.9793 | 1.4080 | 1.5980 |
| 72 | 0.4350 | 0.7326 | 1.0730 | 1.3070 | 1.0200 |
| 73 | 0.4815 | 0.7872 | 1.0790 | 0.9677 | -0.0462 |
| 74 | 0.4945 | 0.7694 | 0.9298 | 0.2388 | -1.8520 |
| 75 | 0.4799 | 0.6995 | 0.6961 | -0.6068 | -3.7480 |
| 76 | 0.4487 | 0.6084 | 0.4561 | -1.1337 | -5.2640 |
| 77 | 0.4323 | 0.5635 | 0.3439 | -1.6630 | -5.9210 |

Table 8.5


Figure 8.6 Variation of " $y$ " displacement along circumferential line "GH"
(Liner thickness $(\mathrm{t})=0.2 \mathrm{~m})$

VARIATION OF "Y" DISPLACEMENTS ALONG CIRCUMFERENTIAL LINE "GH" (FOR FOR ELLIPTICAL TUNNEL - $3, \mathrm{a} / \mathrm{b}=1.500$ )
(LINER THICKNESS $=0.2 \mathrm{~m}$ )

| NODE NUMBER | $" Y$ ' DISPLACEMENTS $\times 10^{-3}(\mathrm{~m})$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | RATIO OF $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}$ |  |  |  |  |
|  | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=5$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=10$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=20$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=50$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=100$ |
| 67 | 1.4140 | 2.5640 | 4.5590 | 9.7440 | 17.5500 |
| 68 | 1.3950 | 2.5260 | 4.4840 | 9.5510 | 17.1600 |
| 69 | 1.3530 | 2.4410 | 4.3100 | 9.1020 | 16.2500 |
| 70 | 1.2460 | 2.2310 | 3.9000 | 8.1120 | 14.3200 |
| 71 | 1.1180 | 1.9790 | 3.4090 | 6.9300 | 12.0200 |
| 72 | 0.9353 | 1.6300 | 2.7490 | 5.3810 | 9.0480 |
| 73 | 0.7676 | 1.3160 | 2.1590 | 4.0130 | 6.4510 |
| 74 | 0.5409 | 0.9020 | 1.4140 | 2.4000 | 3.5500 |
| 75 | 0.3506 | 0.5657 | 0.8397 | 1.2670 | 1.6570 |
| 76 | 0.1709 | 0.2672 | 0.3752 | 0.4925 | 0.5353 |
| 77 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |

Table 8.6

## CHAPTER 9.0

## CONCLUSION

The analyses show that introduction of liners contribute in general to reduction of stress levels and deformations in the rock mass surrounding tunnels, and that an optimum liner thickness could be arrived at in practical situations. The reduction in stress magnitudes and displacements at points inside the rock mass depends on the tunnel shape, location of the point, and the stress or displacement quantity being considered.

Stiffer rock experience larger stresses but smaller displacements than weaker rock. Thus for weaker rock, the magnitudes of stress gradients through the concrete liner thickness will be greater (the strains in the concrete liner will be greater than for stronger rock), and points in the rock mass will experience greater deformations. In weaker rock, a thicker concrete liner will be advantageous for stress and deformation reduction in the rock mass.

The effect of elliptical tunnel geometry on stress in the rock mass is not definitive, but there appears to be a certain $a / b$ ratio at which the stresses are highest. Results in chapter 7 constitute only a limited parametric analysis, which indicate that the stresses, in general, increase first and then start to decrease after a certain $a / b$ value, as the $a / b$ ratio of the ellipse is increased.

This type of finite element analysis offers the tunnel engineers the tools to arrive at an optimum linear thickness and tumnel geometry, by striking a balance between cost and efficiency.

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## APPENDIX A

## ANALYSIS OF CIRCULAR TUNNEL, $\mathbf{a} / \mathrm{b}=1$

A circular tunnel geometry was considered to asses the accuracy of numerical results predicted by FEAP, by comparing the numerical results with the analytical solution for a circular lined tunnel given by Jaeger(1979). Material properties, loading and boundary conditions used are identical to those used for elliptical tunnels considered in chapters $4,5 \& 6$ for a liner thickness of 0.2 m . Finite element mesh used for this analysis is shown in figure A1.

Analytical results and the FEM results were plotted in one graph for comparison purpose (see figures A2 and A3). According to the above results, the deviation of FEM results form analytical results is small. This deviation is close enough for engineer applications. Therefore the results obtained for elliptical tunnels which do not have any analytical solution can be considered as acceptable.


Figure A1 Finite element mesh for circular tunnel with $\mathrm{a} / \mathrm{b}=1$ CIRCULAR TUNNEL, $a / b=1$

| ELEMENT | MAJOR PRINCIPAL STRESS $\times 10^{3} \mathrm{kNm}^{-2}$ |  |
| :---: | :---: | :---: |
|  | FEAP | ANALITICAL |
| 16 | 0.5404 | 0.5622 |
| 26 | 0.4878 | 0.5134 |
| 36 | 0.4439 | 0.4707 |
| 46 | 0.4067 | 0.4330 |
| 56 | 0.3533 | 0.3772 |
| 66 | 0.2930 | 0.3144 |
| 76 | 0.2293 | 0.2461 |
| 86 | 0.1606 | 0.1731 |
| 96 | 0.1109 | 0.1215 |
| 106 | 0.0771 | 0.0859 |
| 116 | 0.0535 | 0.0615 |
| 126 | 0.0388 | 0.0462 |
| 136 | 0.0289 | 0.0360 |
| 146 | 0.0213 | 0.0281 |
| 156 | 0.0155 | 0.0220 |
| 166 | 0.0110 | 0.0173 |
| 176 | 0.0071 | 0.0133 |
| 186 | 0.0038 | 0.0098 |
| 196 | 0.0013 | 0.0072 |
| 206 | 0.0005 | 0.0054 |
| 216 | -0.0178 | 0.0041 |

Table A1

VARIATION OF MAJOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" FOR CIRCULAR TUNNEL , $\mathrm{a} / \mathrm{b}=1$
(LINER THICKNESS $t=0.2 \mathrm{~m}$ )


Figure A2 Variation of major principal stress along radial line "CD" (Liner thickness $(t)=0.2 \mathrm{~m})$

## VARIATION OF MINOR PRINCIPAL STRESS ALONG RADIAL LINE "CD" FOR CIRCULAR TUNNEL, $a / b=1$

| ELEMENT | MINOR PRINCIPAL STRESS $\times\left(-1 \times 10^{3}\right) \mathrm{kNm}^{-2}$ |  |
| :---: | :---: | :---: |
| NUMBER | FEAP | ANALITICAL |
| 16 | 0.4615 | 0.5622 |
| 26 | 0.4301 | 0.5134 |
| 36 | 0.4016 | 0.4707 |
| 46 | 0.3750 | 0.4330 |
| 56 | 0.3337 | 0.3772 |
| 66 | 0.2848 | 0.3144 |
| 76 | 0.2286 | 0.2461 |
| 86 | 0.1657 | 0.1731 |
| 96 | 0.1195 | 0.1215 |
| 106 | 0.0869 | 0.0859 |
| 116 | 0.0642 | 0.0615 |
| 126 | 0.0498 | 0.0462 |
| 136 | 0.0401 | 0.0360 |
| 146 | 0.0326 | 0.0281 |
| 156 | 0.0268 | 0.0220 |
| 166 | 0.0224 | 0.0173 |
| 176 | 0.0185 | 0.0133 |
| 186 | 0.0152 | 0.0098 |
| 196 | 0.0127 | 0.0072 |
| 206 | 0.0109 | 0.0054 |
| 216 | 0.0097 | 0.0041 |

Table A2

## VARIATION OF MINOR PRINCIPAL STRESS ALONG RADIAL LINE "CD"

FOR CIRCULAR TUNNEL , $\mathrm{a} / \mathrm{b}=1$
(LINER THICKNESS $\mathbf{t}=\mathbf{0 . 2 m}$ )


Figure A3 Variation of major principal stress along radial line "CD"
(Liner thickness $(\mathrm{t})=0.2 \mathrm{~m})$

## APPENDIX B

## CHECK FOR STRAIN IN CONCRETE LINER UNDER INTERNAL FLUID PRESSURE



NOTE 1.0 .67 takes account of the relation between the cube strength and the bending strengit in a flexural member. It is simply a coefficient and not a partial safety factor. NOTE 2. $f_{\mathrm{cu}}$ is in $\mathrm{N} / \mathrm{mm}^{2}$.

Figure Bla shows short term design stress-strain curve for normal weight concrete (BS 8110)

$$
2.4 \times 10^{-4}\left(\mathrm{f}_{\mathrm{cu}} / \gamma_{\mathrm{m}}\right)^{0.5}=2.4(25 / 1.5)^{0.5}=0.00098 \mathrm{kN} / \mathrm{mm}^{2}
$$

$$
\begin{aligned}
5.5\left(f_{\mathrm{cu}} / \gamma_{\mathrm{m}}\right)^{0.5}=5.5(25 / 1.5)^{0.5} & =22.45 \mathrm{kN} / \mathrm{mm}^{2} \\
& =22450 \mathrm{MPa} \\
& =2.245 \times 10^{7} \mathrm{kPa}
\end{aligned}
$$

$0.67\left(f_{m} / \gamma_{m}\right)=(0.67 \times 25) / 1.5=11.17 \mathrm{~N} / \mathrm{mm}^{2}$

$$
\begin{aligned}
\varepsilon & =1 /\left(2.2485 \times 10^{7} / 11.1710^{3}\right) \\
& =0.000497 \\
& =0.0005
\end{aligned}
$$

From he above calculation it can be seen that the strain in concrete is 0.0005 at failure for grade 25 concrete, if the initial tangent modulus is excepted to prevail.

| ELEMENT NUMBER | MAJOR PRINCIPAL STRAIN $\times 10^{-3}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=5$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}} 10$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=20$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=50$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=100$ |
| 1 | 0.1291 | 0.2369 | 0.3861 | 0.5974 | 0.7325 |
| 6 | 0.2508 | 0.4419 | 0.6857 | 0.1001 | 0.1175 |
| 10 | 0.2904 | 0.4435 | 0.6089 | 0.7894 | 0.8674 |

Table A 3

VARIATION OF MINOR PRINCIPAL STRAIN
(FOR ELLIPTICAL TUNNEL $3, a / b=1.500$ )
(LINER THICKNESS $\mathrm{t}=0.2 \mathrm{~m}$ )

| ELEMENT NUMBER | MINOR PRINCIPAL STRAIN $\times(-1) \times 10^{-3}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=5$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}} 10$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=20$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=50$ | $\mathrm{E}_{\mathrm{C}} / \mathrm{E}_{\mathrm{R}}=100$ |
| 1 | 0.9211 | 0.1401 | 0.2081 | 0.3132 | 0.3967 |
| 6 | 0.1365 | 0.2106 | 0.3055 | 0.4273 | 0.4897 |
| 10 | 0.1482 | 0.2056 | 0.2647 | 0.3181 | 0.3228 |

Table A 4



[^0]:    Table 6.4

