

REFERENCES

- [1] Ali, A., Muhammad, I.C., Qamar, S., Akhtar, N., Mahmood, T., Hyder, M. & Jamshed, M.T. (2016), International Journal of Asian Social Science, 6(11): 614-624.
- [2] Allen, E. (2007), Modelling with Ito Stochastic Differential Equations, ISBN-13 978-1-4020-5952-0 (HB), ISBN-13 978-1-4020-5953-7 (e-book).
- [3] Aye, G., Gupta, R., Hammoudeh, S. & Kim, W.J. (2015), Forecasting the Price of Gold Using Dynamic Model Averaging.
- [4] Azzutti, A., (2016), Forecasting Gold Price: A Comparative Study.
- [5] Basaru, C., Toraman, C. & Bayramoglu, M.F. (2011), Determination of Factors Affecting the Price of Gold: A Study of MGARCH Model, Business and Economics Research Journal Volume 2 Number 4 pp. 37-50.
- [6] Dirk, G. B., Joscha B., & Robert C. (2014), Gold Price Forecasts in a Dynamic Model Averaging Framework.
- [7] Davis, R., Dedu, V.K. & Bonye, F. (2014) ,Modeling and Forecasting of Gold Prices on Financial Markets, American International Journal of Contemporary Research Vol. 4 No. 3.
- [8] Guha, B, & Bandyopadhyay, G. (2016), Gold Price Forecasting Using ARIMA Model, Journal of Advanced Management Science Vol. 4, No. 2.
- [9] Guidoum, A.C. & Boukhetala, K. (2016), Estimation of Stochastic Differential Equations with Sim.DiffProc Package Version 3.2.

- [10] Ismail, Z., Yahya, A. & Shabri, A. (2009), Forecasting Gold Prices Using Multiple Linear Regression Method, American Journal of Applied Sciences 6 (8): 1509-1514.
- [11] Khalid, M., Sultana, M, & Zaidi, F. (2014),Forecasting Gold Price: Evidence from Pakistan Market, Research Journal of Finance and Accounting ,Vol.5, No.3.
- [12] Khan, M.M.A. (2013), Forecasting of Gold Prices (Box Jenkins Approach), International Journal of Emerging Technology and Advanced Engineering ,Volume 3, Issue 3.
- [13] Phillips, P.C.B. & Yu, J. (2006), Maximum Likelihood and Gaussian Estimation of Continuous Time Models in Finance, Research Collection School of Economics.
- [14] Pitigalaarachchi, P. A. A. C., Jayasundara D. D. M. & Chandrasekara N.V. (2016), Modeling and forecasting Sri Lankan Gold Prices. International Journal of Sciences: Basic and Applied Research (IJSBAR), Volume 27, No 3, pp. 247-260.
- [15] Sindhu (2013), A study on impact of select factors on the price of Gold, IOSR Journal of Business and Management (IOSR-JBM, Volume 8, Issue 4, pp. 84-93.
- [16] Prices: Evidence from Pakistan, The Lahore Journal of Economics 18: 2 pp.1–35.
- [17] <http://www.investopedia.com/terms/t/troyounce.asp>

[18] <https://bebusinessed.com/history/the-history-of-gold/>

[19] <https://wikipedia.org>

APPENDIX 01

Parameter Estimation of Four SDE Models

```
%This program compute the parameters of four SDE models  
Brownian motion, Geometric Brownian motion, CIR model and  
Vasicek model according to the Sri Lankan gold price using  
maximum likelihood method
```

```
clc;
```

```
format long;
```

```
gold=xlsread('gold rate.xlsx'); %Read the excel file which  
contains gold price data
```

```
N=length(gold)-1;
```

```
dt=1/252; %The length of the time step
```

```
%Parameters of Brownian motion using maximum likelihood  
method
```

```
alpha_bm=(gold(end)-gold(1))/(dt*N);
```

```
SS1=0;
```

```
for i=1:N
```

```
    SS1=SS1+(gold(i+1)-gold(i)-alpha_bm*dt)^2;
```

```
End
```

```
sigma_bm=sqrt(SS1/(N*dt));
```

```
%Parameters of Geometric Brownian motion using maximum  
likelihood method
```

```
SS2=0;
```

```

for j=1:N
    SS2=SS2+(gold(j+1)-gold(j))/gold(j);
End

beta_gbm=SS2/(dt*N);

SS22=0;
for k=1:N
    SS22=SS22+((gold(k+1)-
(1+beta_gbm*dt)*gold(k))/gold(k))^2;
end

sigma_gbm=sqrt(SS22/(N*dt));

%Parameters of CIR model using maximum likelihood method
alpha_cir=(N*(gold(end)-gold(1))-(sum(gold)-
gold(end))*SS2)/(dt*(N^2-(sum(gold)-
gold(end))*(sum(1./gold)-1/gold(end))));

beta_cir=(gold(end)-gold(1)-alpha_cir*N*dt)/(dt*(sum(gold)-
gold(end)));

SS3=0;
for m=1:N
    SS3=SS3+(gold(m+1)-alpha_cir*dt-
(1+beta_cir*dt)*gold(m))^2/gold(m);
End

sigma_cir=sqrt(SS3/(N*dt));

```

```

%Parameters of Vasicek model using maximum likelihood
method
SS41=0;
for b=1:N
    SS41=SS41+(gold(b+1)-gold(b))*gold(b);
end
sum_1=((sum(gold)-gold(end))*SS41)-((gold(end)-
gold(1))*(sum(gold.^2)-gold(end)^2))/(dt*(sum(gold)-
gold(end))^2-N*(sum(gold.^2)-gold(end)^2));

alpha_vas=((sum(gold)-gold(end))*SS41)-((gold(end)-
gold(1))*(sum(gold.^2)-gold(end)^2))/(dt*(sum(gold)-
gold(end))^2-N*(sum(gold.^2)-gold(end)^2));

beta_vas=(gold(end)-gold(1)-sum_1*N*dt)/(dt*(sum(gold)-
gold(end)));

SS4=0;
for p=1:N
    SS4=SS4+(gold(p+1)-alpha_vas*dt-
(1+beta_vas*dt)*gold(p))^2;
End

sigma_vas=sqrt(SS4/(N*dt));

%Create the table of parameters.

```

```

parameter={'alpha (BM) '; 'sigma (BM) '; 'beta (GBM) '; 'sigma (GBM) '
; 'alpha (CIR) '; 'beta (CIR) '; 'sigma (CIR) '; 'alpha (Vasicek) '; 'be
ta (Vasicek) '; 'sigma (Vasicek) '};

MLE=[alpha_bm;sigma_bm;beta_gbm;sigma_gbm;alpha_cir;beta_ci
r;sigma_cir;alpha_vas;beta_vas;sigma_vas];

T1=table(parameter,MLE);

fprintf('Parameters of four SDE models using maximum
likelihood estimation method \n');

disp(T1); %Display the table of parameters

```

Simulation and Forecasting Accuracy Measures

```

%Written by WMHN Weerasinghe
%This program simulate the SDEs using Euler Maruyama
method
%and test the forecasting accuracy using two tests RMSE and
MAPE

%Simulation
parameters; %Run the program parameters

y=xlsread('gold_forecast.xlsx'); %Read the excel file which
contains the data use to forecast
m=length(y);
n=1:10:500000;

```

```

BM=zeros(length(n),m); %Vector of generating values of
Brownian motion

GBM=zeros(length(n),m); %Vector of generating values of
Geometric Brownian motion

CIR=zeros(length(n),m); %Vector of generating values of CIR
model

Vasicek=zeros(length(n),m); %Vector of generating values of
Vasicek model
x0=y(1); %Initial value

BM(:,1)=x0;
GBM(:,1)=x0;
CIR(:,1)=x0;
Vasicek(:,1)=x0;

for p=1:length(n)

A=randn([n(p),m-1]); %A matrix of random numbers

B=zeros(1,m-1);

    for b=1:m-1

        B(b)=mean(A(:,b)); %Calculate the mean of each
column of A

    end

```



```

    for c=2:m

BM(p,c)=BM(p,c-1)+alpha_bm*dt+sigma_bm*sqrt(dt)*B(c-1);

GBM(p,c)=GBM(p,c-1)+beta_gbm*GBM(p,c-1)*dt+
        sigma_gbm*GBM(p,c-1)*sqrt(dt)*B(c-1);

CIR(p,c)=CIR(p,c-1)+((alpha_cir)+beta_cir*CIR(p,c-1))*dt+
        sigma_cir*sqrt(CIR(p,c-1))*sqrt(dt)*B(c-1);
Vasicek(p,c)=Vasicek(p,c-1)+((alpha_vas)+
        beta_vas*Vasicek(p,c-
        1))*dt+sigma_vas*sqrt(dt)*B(c-1);

    end
end

for z=2:m

figure;

plot(n,BM(:,z) ','r-',n,GBM(:,z) ','b-',n,CIR(:,z) ','
        'k-',n,Vasicek(:,z) ','g-',n,y(z)*ones(1,length(n)));

legend('BM','GBM','CIR','Vasicek','Actual');

end
x=1:length(gold)+length(y);
figure;

```

```

plot(x,[gold' y']);

title('Gold price of Sri Lanka from 01st of October 2015 to
28th of October 2016');
xlabel('Date');
ylabel('Gold Price');
figure;

subplot(2,2,1);
plot(1:length(y),BM(length(n),:),1:length(y),y,'*');
title('Plot of past gold prices and forecasted gold prices
using BM model');

subplot(2,2,2);
plot(1:length(y),GBM(length(n),:),1:length(y),y,'*');
title('Plot of past gold prices and forecasted gold prices
using GBM model');

subplot(2,2,3);
plot(1:length(y),CIR(length(n),:),1:length(y),y,'*');
title('Plot of past gold prices and forecasted gold prices
using CIR model');

subplot(2,2,4);
plot(1:length(y),Vasicek(length(n),:),1:length(y),y,'*');
title('Plot of past gold prices and forecasted gold prices
using Vasicek model');
actual_data=y;
modell1=BM(length(n),:);
model2=GBM(length(n),:);

```

```

model3=CIR(length(n),:);
model4=Vasicek(length(n),:);
figure;
t=0:length(y)-1;
plot(t,model1,'k-',t,model2,'g-',t,model3,'b-',
't,model4',
'c-',t,y,'r-');
legend('BM','GBM','CIR','Vasicek','actual');

T1=table(actual_data,model1,model2,model3,model4);
disp(T1);

```

```

A11=(y'-BM(length(n),:));
B11=(y'-GBM(length(n),:));
C11=(y'-CIR(length(n),:));
D11=(y'-Vasicek(length(n),:));

```

```

figure;
subplot(2,2,1);
plot(1:length(y),A11,'*');
subplot(2,2,2);
plot(1:length(y),B11,'*');
subplot(2,2,3);
plot(1:length(y),C11,'*');
subplot(2,2,4);
plot(1:length(y),D11,'*');

```

```

%Forecasting accuracy

RMSE1=sqrt (sum(abs (A11) .^2)/length(y));
RMSE2=sqrt (sum(abs (B11) .^2)/length(y));
RMSE3=sqrt (sum(abs (C11) .^2)/length(y));
RMSE4=sqrt (sum(abs (D11) .^2)/length(y));

MAPE1=(sum(abs (A11) ./BM(length(n),:))/length(y))*100;
MAPE2=(sum(abs (B11) ./GBM(length(n),:))/length(y))*100;
MAPE3=(sum(abs (C11) ./CIR(length(n),:))/length(y))*100;
MAPE4=(sum(abs (D11) ./Vasicek(length(n),:))/length(y))*100;

model={'Brownian Motion'; 'Geometric Brownian Motion';
' CIR'; 'Vasicek'};

RMSE=[RMSE1;RMSE2;RMSE3;RMSE4];

MAPE=[MAPE1;MAPE2;MAPE3;MAPE4];

T2=table(model, RMSE, MAPE);

disp(T2);

```

Sample Paths Generation

```

%This program generates sample paths for the SDE models,
Brownian motion, geometric Brownian motion, CIR model and
Vasicek model.

```

```

parameters;

```

```

y=xlsread('gold_forecast.xlsx'); %Read the excel file which
contains the data use to forecast

m=101;
n=5;
BM=zeros(n,m); %Vector of generating values of Brownian
motion
GBM=zeros(n,m); %Vector of generating values of Geometric
Brownian motion
CIR=zeros(n,m); %Vector of generating values of CIR model
Vasicek=zeros(n,m); %Vector of generating values of Vasicek
model

x0=y(1); %Initial value

BM(:,1)=x0;
GBM(:,1)=x0;
CIR(:,1)=x0;
Vasicek(:,1)=x0;

for p=1:n
    A=randn([n,m-1]); %A matrix of random numbers

    for c=2:m

BM(p,c)=BM(p,c-1)+alpha_bm*dt+sigma_bm*sqrt(dt)*A(p,c-1);

GBM(p,c)=GBM(p,c-1)+beta_gbm*GBM(p,c-1)*dt+
sigma_gbm*GBM(p,c-1)*sqrt(dt)*A(p,c-1);

```

```

CIR(p,c)=CIR(p,c-1)+((alpha_cir)+beta_cir*CIR(p,c-1))*dt+
    sigma_cir*sqrt(CIR(p,c-1))*sqrt(dt)*A(p,c-1);

Vasicek(p,c)=Vasicek(p,c-1)+
    ((alpha_vas)+beta_vas*Vasicek(p,c-1))*dt+
    sigma_vas*sqrt(dt)*A(p,c-1);

    end

end

figure

for i_1=1:n
    hold on;
    plot(0:m-1,BM(i_1,:));
end

figure;

for i_2=1:n
    hold on;
    plot(0:m-1,GBM(i_2,:));
end

figure;

for i_3=1:n
    hold on;
    plot(0:m-1,CIR(i_3,:));
end

```

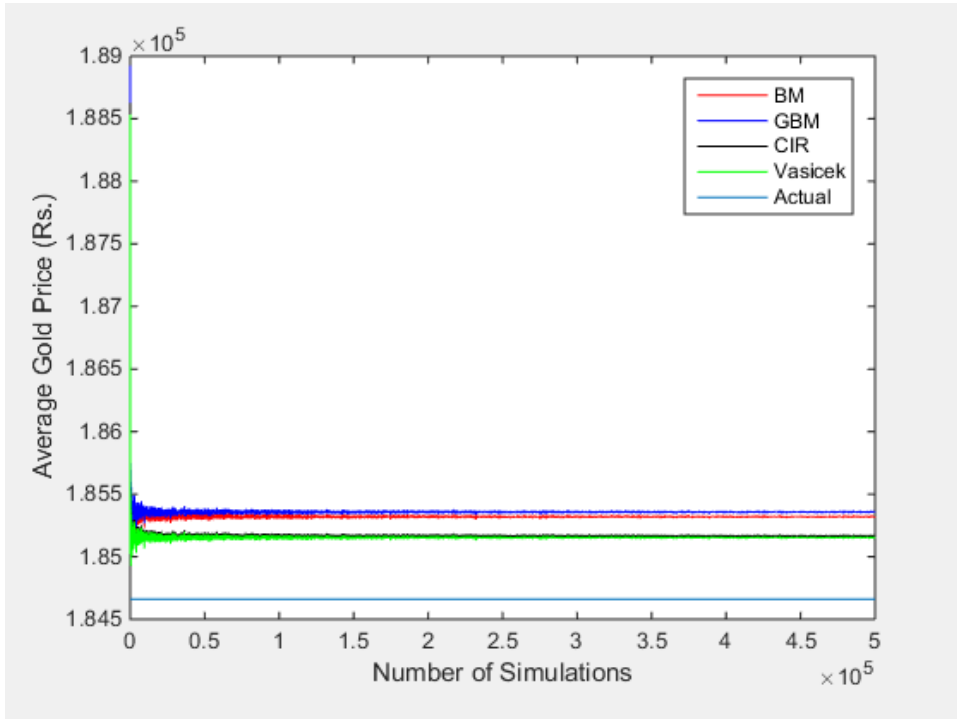
```
end
figure;

for i_4=1:n
    hold on;
    plot(0:m-1,Vasicek(i_4,:));
end
```

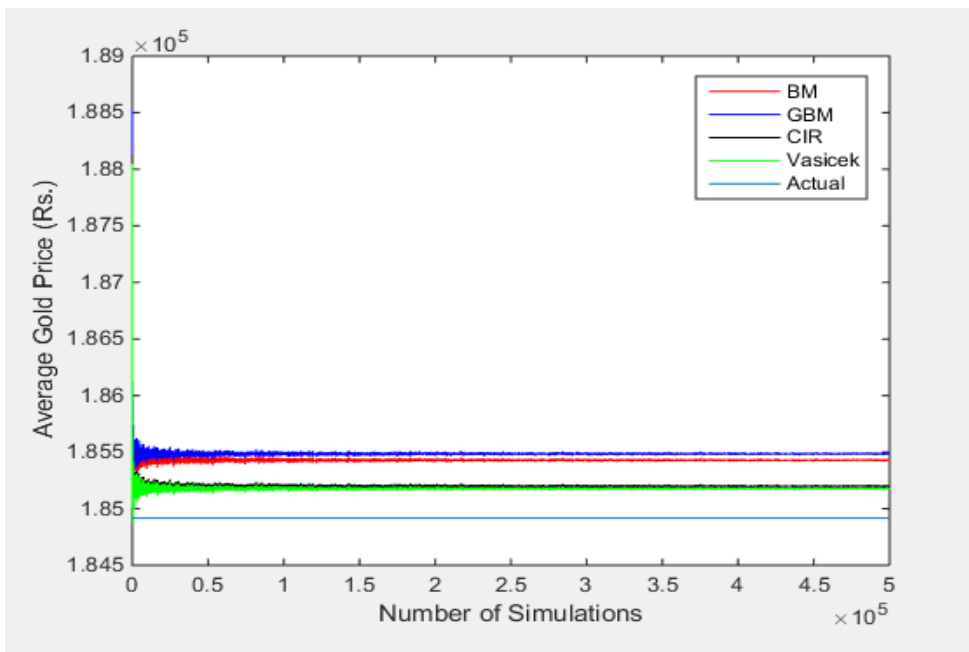
APPENDIX 02

Monte Carlo simulations of the forecasted gold prices from 12th of October 2016 to 14th of October 2016.

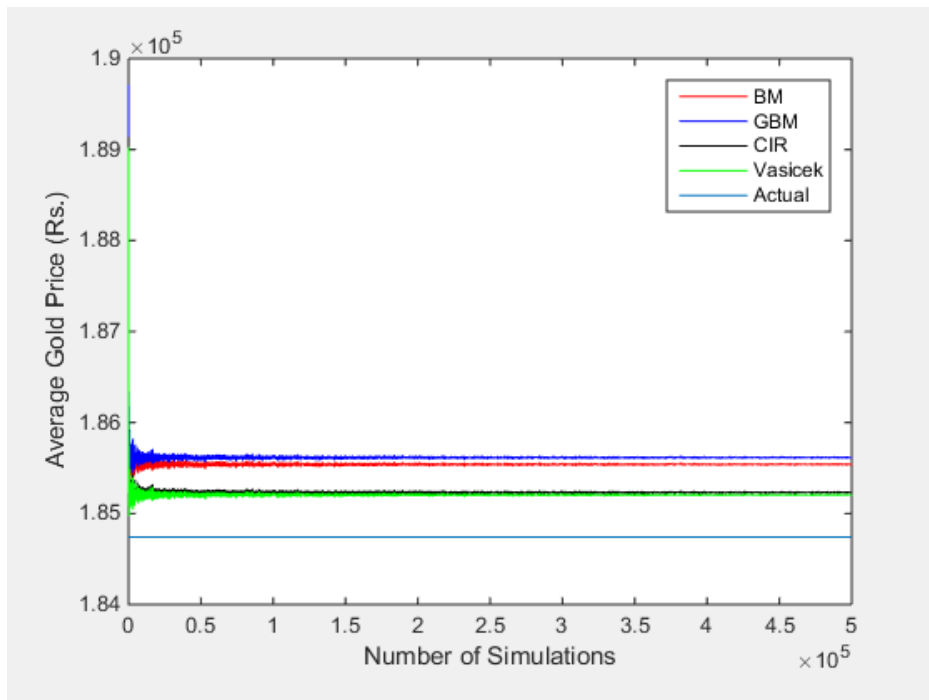
12/10/2016



13/10/2016



14/10/2016



APPENDIX 03

Gold Price of Sri Lanka in Rupees from 01/10/2015 to 14/10/2016

Date	Gold Price (Rs.)
01.10.2015	157574.104
02.10.2015	157134.843
05.10.2015	160768.1198
06.10.2015	160487.2945
07.10.2015	161959.6559
08.10.2015	160774.8253
09.10.2015	160728.0625
12.10.2015	162490.3533
13.10.2015	162442.4899
14.10.2015	164685.7591
15.10.2015	166316.0396
16.10.2015	166228.3504
19.10.2015	165650.7861
20.10.2015	164663.7863
21.10.2015	166008.0883
22.10.2015	164343.1347
23.10.2015	164931.795
26.10.2015	164243.6864
28.10.2015	164680.2028
29.10.2015	163635.9117
30.10.2015	161538.0497
02.11.2015	160814.9254
03.11.2015	160128.1341

04.11.2015	158333.5129
05.11.2015	156819.7196
06.11.2015	156934.9254
09.11.2015	154711.1945
11.11.2015	154970.0821
12.11.2015	154546.4881
13.11.2015	153732.0576
16.11.2015	155136.5138
17.11.2015	154112.8495
18.11.2015	151885.0426
19.11.2015	153455.7704
20.11.2015	154174.6454
23.11.2015	152459.4916
24.11.2015	152738.933
26.11.2015	153252.5517
27.11.2015	153094.9603
30.11.2015	150926.2789
01.12.2015	153616.6656
02.12.2015	153187.3727
03.12.2015	150522.2986
04.12.2015	152087.5964
07.12.2015	155407.1923
08.12.2015	153197.9607
09.12.2015	154163.515

10.12.2015	153780.3309
11.12.2015	152829.6352
14.12.2015	154150.6484
15.12.2015	152803.6777
16.12.2015	152638.9139
17.12.2015	153312.7431
18.12.2015	151484.4273
21.12.2015	153315.7149
22.12.2015	154716.2058
23.12.2015	154189.7187
28.12.2015	154134.3139
29.12.2015	154247.0284
30.12.2015	153982.5198
31.12.2015	153015.7719
01.01.2016	152822.509
04.01.2016	153507.5012
05.01.2016	155184.4858
06.01.2016	155207.84
07.01.2016	158331.7341
08.01.2016	158796.2628
11.01.2016	158874.4732
12.01.2016	157582.4629
13.01.2016	155826.0485
14.01.2016	157105.9157
18.01.2016	156989.6548
19.01.2016	156956.5374
20.01.2016	157114.0797
21.01.2016	158324.0206
22.01.2016	158188.5505
25.01.2016	158333.17
26.01.2016	159846.0911

27.01.2016	161285.5816
28.01.2016	161164.864
29.01.2016	160529.2603
01.02.2016	161311.9
02.02.2016	162226.4738
03.02.2016	162419.2105
05.02.2016	166259.5578
08.02.2016	167758.2265
09.02.2016	171661.2504
10.02.2016	171579.165
11.02.2016	173622.545
12.02.2016	178058.1478
15.02.2016	176002.7446
16.02.2016	172935.1131
17.02.2016	173040.231
18.02.2016	173903.15
19.02.2016	176602.11
23.02.2016	174999.9904
24.02.2016	176730.9793
25.02.2016	177616.3693
26.02.2016	178082.7255
29.02.2016	176876.9562
01.03.2016	179291.175
02.03.2016	176636.1159
03.03.2016	178804.8162
04.03.2016	181787.1656
08.03.2016	183199.09
09.03.2016	180597.7545
10.03.2016	180130.7807
11.03.2016	184523.7413
14.03.2016	180600.9755

15.03.2016	176673.225
16.03.2016	177317.591
17.03.2016	180702.425
18.03.2016	181760.09
21.03.2016	180321.09
23.03.2016	179084.1829
24.03.2016	175202.5113
28.03.2016	174234.5413
29.03.2016	175485.3305
30.03.2016	178063.875
31.03.2016	176679.7005
01.04.2016	176953.1105
04.04.2016	175334.955
05.04.2016	176270.305
06.04.2016	176787.6255
07.04.2016	176392.62
08.04.2016	178018.69
11.04.2016	179975.73
12.04.2016	180600.9755
15.04.2016	176709.2
18.04.2016	177846.01
19.04.2016	177140.9
20.04.2016	180378.65
22.04.2016	179910.2555
25.04.2016	177546.7811
26.04.2016	178406.5005
27.04.2016	179169.89
28.04.2016	178709.41
29.04.2016	183342.99
03.05.2016	186285.745
04.05.2016	186575.2044

05.05.2016	186595.6066
06.05.2016	186511.8118
09.05.2016	187537.0032
10.05.2016	184255.8889
11.05.2016	184993.0894
12.05.2016	185651.9775
13.05.2016	184737.3963
16.05.2016	186248.433
17.05.2016	186488.904
18.05.2016	186112.6838
19.05.2016	183309.0463
20.05.2016	183083.8625
24.05.2016	181939.725
25.05.2016	178937.275
26.05.2016	179549.425
27.05.2016	177261.15
30.05.2016	175220.65
31.05.2016	176874.9125
01.06.2016	177780.4877
02.06.2016	177328.5583
03.06.2016	176673.9345
06.06.2016	181326.405
07.06.2016	181560.878
08.06.2016	181823.125
09.06.2016	183973.4659
10.06.2016	184399.1276
13.06.2016	184745.9643
14.06.2016	185493.7931
15.06.2016	185884.79
16.06.2016	187842.075
17.06.2016	185016.4683

20.06.2016	185573.4025
21.06.2016	186180.0418
22.06.2016	184273.7825
23.06.2016	183850.1875
24.06.2016	185933.7988
27.06.2016	192731.4988
28.06.2016	191889.775
29.06.2016	191809.8875
30.06.2016	191170.7875
01.07.2016	192876.7488
04.07.2016	196820.2863
05.07.2016	195225.1486
07.07.2016	198798.2002
08.07.2016	196973.525
11.07.2016	198984.5113
12.07.2016	197169.6125
13.07.2016	193876.63
14.07.2016	194670.5863
15.07.2016	193065.5738
18.07.2016	193022.725
20.07.2016	193507.86
21.07.2016	190912.2425
22.07.2016	193789.2
25.07.2016	191945.4625
26.07.2016	192345.5463
27.07.2016	192163.3588
28.07.2016	194877.7789
29.07.2016	195048.3024
01.08.2016	196728.9775
02.08.2016	196529.3
03.08.2016	198660.6372

04.08.2016	197765.6975
05.08.2016	198085.3093
08.08.2016	194674.48
09.08.2016	194271.168
10.08.2016	196370.72
11.08.2016	195700.96
12.08.2016	194986.0123
15.08.2016	194729.1975
16.08.2016	195495.9825
18.08.2016	197093.5725
19.08.2016	196010.325
22.08.2016	194094.09
23.08.2016	194542.23
24.08.2016	194651.355
25.08.2016	192829.8546
26.08.2016	193043.0764
29.08.2016	191658.3833
30.08.2016	192720.5204
31.08.2016	191475.738
01.09.2016	190839.0033
02.09.2016	191121.7462
05.09.2016	192579.2945
06.09.2016	192866.5032
07.09.2016	196240.1892
08.09.2016	195801.9492
09.09.2016	194602.9175
13.09.2016	193267.6899
14.09.2016	191694.3008
15.09.2016	192861.6922
19.09.2016	191707.1159
20.09.2016	191849.9963

21.09.2016	191775.8014
22.09.2016	194711.5757
23.09.2016	194834.86
26.09.2016	195314.8651
27.09.2016	195402.5499
28.09.2016	193956.3162
29.09.2016	194065.7428
30.09.2016	194305.1365
03.10.2016	193448.7159
04.10.2016	192048.5351
05.10.2016	186601.3864
06.10.2016	185938.9861
07.10.2016	184526.5768
10.10.2016	185099.7832
11.10.2016	184942.1631
12.10.2016	184661.3795
13.10.2016	184916.9855
14.10.2016	184741.44

