



Title	Tangent modulus method : An original method to measure in-situ rock stress
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Citation	Tunnelling and Underground Space Technology, 82, 148-155 <a href="https://doi.org/10.1016/j.tust.2018.08.005">https://doi.org/10.1016/j.tust.2018.08.005</a>
Issue Date	2018-12
Doc URL	<a href="http://hdl.handle.net/2115/79823">http://hdl.handle.net/2115/79823</a>
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Type	article (author version)
File Information	FujiiEtAl2018-AuthorVersion.pdf



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1 Tangent Modulus Method - An Original Method to Measure In-Situ Rock Stress

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14  
15 Abbreviated title: Tangent Modulus Method to Measure Rock Stress

1 **ABSTRACT**

2 This paper proposed Tangent Modulus Method (TMM) which is an improved oriented core method to determine  
3 in-situ rock stresses. In this approach, the cylindrical specimens prepared along different directions from thick core  
4 samples were uniaxially compressed twice to a given stress level. The stress value of the bending point in the first  
5 loading cycle of the stress-tangent modulus curve is considered as the normal component of the in-situ rock stress  
6 along the drilled direction of the specimen. Four types of rocks from soft porous tuff and sandstone to hard  
7 crystalline granite was investigated to evaluate the potential of this method. The effects of changes in strain rate,  
8 temperature, water content, confining and pore pressure, and stresses larger than the preload on the stress value of  
9 the bending point were experimentally investigated on preload specimens to investigate their influence on TMM.  
10 Comparison of the stress measurement results by TMM and an overcoring method at AK tunnel in Hokkaido, Japan  
11 was also performed to validate the TMM.

12  
13 Keywords: Tangent Modulus Method; in-situ rock stress; strain rate; temperature; confining pressure  
14

1 **1. INTRODUCTION**

2 As shown in extant studies including Fairhurst (2003) and Ljunggren et al. (2003), numerous methods for in-situ  
3 rock stress measurement have been developed to date. They are divided into in-situ methods, oriented core  
4 methods, and other methods. Oriented core methods can be applied to rock cores from great underground depth and  
5 are cheaper and less time consuming than other methods. However, various factors affect the results from oriented  
6 core methods, and they are recognized as less reliable than in-situ methods (Ljunggren et al., 2003).

7  
8 In order to increase the reliability of oriented core methods, previous studies, such as Lavrov (2003), examined the  
9 impact of various conditions in the Kaiser effect, and this utilizes acoustic emission (AE) due to the initiation and  
10 propagation of microcracks. Experiments indicate that the stress level at the beginning of AE occurrence during  
11 uniaxial compression on a triaxially preloaded specimen is equal to the preloaded differential stress value minus  
12 0.5–0.7 times the preloaded confining pressure value. This does not entirely preclude any estimation of in-situ  
13 stress, and instead presented a serious problem because the lateral stress is not known in advance. Results also  
14 indicate that heating of a saturated diorite or liporite specimen up to 80–100 °C completely eliminates the Kaiser  
15 effect. It should also be noted that the Kaiser effect requires a significantly expensive AE measurement system and  
16 excellent experimental skills.

17  
18 Specifically, in the present study, the tangent modulus method (TMM) is presented as a potentially better original  
19 oriented core method for stress measurement. The TMM does not require either an AE measurement system or  
20 excellent experimental skills. The effect of lateral stress on the result was 1/5th of that from the Kaiser effect (see  
21 Section 3.5). The reason is potentially because TMM utilizes the irrecoverable closure of voids as opposed to the  
22 initiation and propagation of microcracks (see Chapter 2). The effect of a change in the surrounding water  
23 temperature is not significant (see Section 3.2) although it is not possible to perform a quantitative comparison with  
24 the aforementioned results for the Kaiser effect because there are differences in the tested rock types.

25  
26 The procedure for stress measurement using TMM is described first. Subsequently, the effects of changes in strain  
27 rate, temperature, water content, confining and pore pressures, and short duration loading of higher stresses

1 (simulating the stress concentration at rock sampling) on the TMM are investigated using laboratory tests. Finally, a  
2 comparison between results using the TMM and a stress relief method in the AK tunnel, Japan, is discussed.

## 4 **2. Tangent modulus method**

5 The following procedure was used to determine in-situ rock stress in the study:

- 7 (1) Oriented thick rock cores were sampled from a drilling hole.
- 8 (2) Cylindrical rock specimens in various directions were prepared by re-drilling the thick rock core from a  
9 drilling hole.
- 10 (3) The specimens were uniaxially or triaxially compressed twice to a certain stress level.
- 11 (4) The stress value of the bending point in the stress-tangent modulus curve in the first loading cycle or the  
12 point where the first and the second stress-tangent modulus curves begin to separate (the point is also  
13 subsequently termed as the bending point for the purpose of convenience) was considered as the normal  
14 component of the in-situ rock stress in the direction of the specimen.
- 15 (5) The three-dimensional stress state was calculated from the normal stress components in more than six  
16 independent directions.

17  
18 In order to demonstrate the potential of the tangent modulus method, the following experiments were performed  
19 (Fig. 1):

- 21 (1) 30 mm $\phi$   $\times$  60 mm long cylindrical rock specimens were compressed to a given preloading stress level, and  
22 the stress was maintained for a set time to simulate in-situ rock stress.
- 23 (2) The specimens were unloaded and subsequently cyclically compressed to a higher stress level twice after a  
24 delay time.
- 25 (3) The stress value at the bending point was compared to the preloading stress value.

26  
27 As an outline, uniaxial preloading at approximately 30% uniaxial compressive strength (UCS) was applied for 1 h

1 at 295 K, and cyclic loading was performed to approximately 50% UCS at a strain rate of  $10^{-4} \text{ s}^{-1}$  at 295 K unless  
2 other conditions were specified. A time delay was not incorporated although removal and re-installment of  
3 end-pieces and clip gages from the specimen were undertaken over one to several minutes. This was performed to  
4 ensure that stress memory did not arise due to deformation of the boundary between end-pieces and the specimen or  
5 from the clip gage and that measured stresses arose solely from the rock specimen itself. It was assumed that rock  
6 specimens did not retain any memory of in-situ rock stress because they were sampled several years prior to  
7 performing the experiments and experienced changes in water contents during storage, cutting and grinding using  
8 water, and oven-drying for 24 h at 353 K. As shown later in Section 3.3, rock specimens lost their stress memory  
9 quickly due to changes in the water content.

10  
11 The results confirmed that the bending point appeared at the preloading stress level in porous rocks, such as  
12 Shirahama sandstone (Fig. 2a) and Kimachi sandstone that both date to the Miocene age, and in a Pleistocene  
13 Shikotsu welded tuff under dry conditions (Fujii et al., 2003; Fujii et al., 2008). The bending point was discernible  
14 although not quite distinctive in a hard and crystalline Inada granite (Fig. 2b; Fujii et al., 2008). The strengths of  
15 these rocks are shown in Table 1. Bending points became more indistinct with increases in the delay time due to  
16 relaxation. However, bending points were observed at the preloading stress level even after a delay time of 6 weeks  
17 when samples were preloaded for 17 h (Fig. 3). A significantly longer delay time was expected for rocks that were  
18 subjected to in-situ stress for geologically long periods.

19  
20 The mechanism of TMM was explained by nearly irrecoverable closures of rock voids such as microcracks and  
21 pores. We assume that A in Fig. 4a denotes the in-situ stress condition under which a rock exhibits a few voids that  
22 are tabular and sufficiently large such that they are partly closed, and the rock is stiff during the first cyclic loading  
23 up to the in-situ stress level (B to C) because practically none of the voids closed. However, the stiffness decreased  
24 under further compression (C to D) due to the closure of the partly closed voids and closure of other open voids.  
25 Hence, a bending point appeared at C (Fig. 4b). Further closures did not occur in the second loading cycle, thereby  
26 resulting in high stiffness throughout the second loading cycle (E to F). The aforementioned mechanism also  
27 correlated well with the principle of Deformation Rate Analysis (DRA), (Yamamoto, 2009), which corresponds to

1 another in-situ rock stress measurement method using oriented cores. In the study, TMM was performed by plotting  
2 the tangent modulus (Fig. 4b) since DRA was conducted by plotting the strain difference ( $\Delta\varepsilon$  in Fig. 4a) relative to  
3 the axial stress under cyclic loading because nonlinearity was not very evident for most real rocks.

### 5 **3. INFLUENCES OF VARIOUS FACTORS**

6 The above results suggest that TMM could be used as an oriented core method in the future. However, as stated by  
7 Lavrov (2003), Ljunggren et al. (2003), and Hsieh et al. (2015), there are several factors that can affect the results  
8 of stress measurements by oriented core methods. It was necessary to investigate the effects prior to any practical  
9 use of TMM or any other oriented core method. Therefore, effects of changes in the strain rate, temperature, water  
10 content, confining and pore pressures, and stress concentration at sampling were investigated.

#### 12 **3.1 Strain rates for cyclic loading**

13 A clear effect of the strain rate for cyclic loading between  $10^{-6.5} \text{ s}^{-1}$  and  $10^{-2.5} \text{ s}^{-1}$  (Fig. 5) was not observed. The  
14 specimen lost any stress memory over the long experimental time corresponding to several days for the slowest  
15 strain rate of  $10^{-7} \text{ s}^{-1}$ . Hence, the cyclic loading strain rate did not significantly affect the results provided that it was  
16 not excessively slow.

#### 18 **3.2 Temperature of water**

19 Rock mass temperature may not be identical to laboratory room temperature. In order to investigate the effect of the  
20 difference in temperature, Kimachi sandstone specimens were preloaded in pure water, unloaded, and cooled in  
21 pure water at 295 K for 1 h. Cyclic loading was subsequently promptly applied in air at 295 K. Water temperature  
22 between 295 K and 353 K for preloading was not significant (Fig. 6) (Makasi and Fujii, 2008).

#### 24 **3.3 Change in water content**

25 Stress memory was lost very easily with changes in the water content of the specimens. For example, specimens  
26 that were preloaded in water lost stress memory quickly after they were dried. Similarly, preloaded dry specimens  
27 lost stress memory after they were immersed into water. The results suggested that it was necessary to maintain the

1 water content of rock samples to the maximum possible extent until after cyclic loading stress measurements were  
2 completed.

3

#### 4 **3.4 Triaxial cyclic loading for triaxially preloaded specimens**

5 Triaxial cyclic loading for triaxially preloaded specimens was undertaken because it was not possible to apply  
6 uniaxial cyclic loading when in-situ rock stress approaches or exceeds the uniaxial compressive strength of the  
7 rock. The apparatus for triaxial compression tests was described in Alam et al. (2014). A loading frame was used to  
8 apply the axial load. Axial strain was measured by using strain gages. A double ball plunger pump with a relief  
9 valve connected to the ultra-compact triaxial cell (Alam et al., 2014) was used to maintain the confining pressure.

10

11 The bending point was observed at smaller stress than the triaxial preloading stress when cyclic loading was  
12 undertaken under a smaller confining pressure for dry Shirahama Sandstone (Fig. 7). However, a clear bending  
13 point was not observed when cyclic loading was undertaken under a larger confining pressure.

14

15 Conversely, the preloading stress was precisely estimated for a smaller confining pressure, and the bending point  
16 was observed at a smaller stress level when the confining pressure exceeded the preloaded value (Fig. 8) for dry  
17 Kimachi Sandstone. The results appear to contradict each other. However, for example, the set including the highest  
18 bending point stress under triaxial cyclic loading and the confining pressure value that exhibited the highest  
19 bending point stress may be considered as an in-situ rock stress state although the minimum and intermediate  
20 stresses were restricted such that they were identical.

21

22 Subsequently, a pair of stainless steel attachments was connected to the saturated and jacketed Kimachi sandstone  
23 sample to apply pore pressure. Each attachment included a hole for water flow and a pore pressure sensor. A  
24 syringe pump was connected to both attachments and used to produce a constant pore pressure, and the specimens  
25 were triaxially preloaded under a pore pressure. Cyclic loading was undertaken under various confining and pore  
26 pressures.

27



1 Under a constant confining pressure, total and differential stress values at the bending point were obtained by  
2 triaxial cyclic loading of a triaxial preloaded saturated Kimachi sandstone sample with a pore pressure between  
3 60% and 140% for preloading (Fig. 9a). In contrast, smaller total and differential stress values at the bending point  
4 were obtained under a pore pressure of  $\leq 20\%$  or  $\geq 180\%$  for preloading. Terzaghi's effective stress was precisely  
5 evaluated only for the case in which the same pore pressure was used.

6

7 Based on the data shown in Dassanayake et al. (2015), Biot's effective stress coefficient for Kimachi sandstone is  
8 given as follows:

$$9 \quad \alpha = A - BP'_C \quad (1)$$

10 where  $P'_C$  denotes the effective confining pressure, and  $A$  and  $B$  are constants. We rearrange Eq. (1), and Biot's  
11 coefficient is calculated from the total confining pressure  $P_C$  and pore pressure  $P_p$  as follows:

$$12 \quad \alpha = \frac{A - BP_C}{1 - BP_p} \quad (2)$$

13 We substitute the values of  $A$  and  $B$  for Kimachi sandstone corresponding to  $0.984$  and  $0.014 \text{ MPa}^{-1}$ , respectively,  
14 into Eq. (2), and the Biot coefficient is calculated as  $0.908$ . This implies that the effective Terzaghi stress was  
15 almost identical to the effective Biot stress in this case. Therefore, only the effective Terzaghi stress is shown here.

16

17 A smaller total preloading stress was investigated under pore pressure and under a constant effective confining  
18 pressure for a cyclic loading smaller than that of the preload (Fig. 9b). The effective and differential preloading  
19 stress was measured as lower when pore pressure exceeding that of the preloading was used.

20

### 21 **3.5 Uniaxial cyclic loading for triaxially preloaded specimens**

22 Uniaxial cyclic loading was performed for triaxially preloaded saturated Kimachi sandstone under a range of  
23 confining and pore pressures. The preloaded differential axial stress corresponded to  $12 \text{ MPa}$  for all the specimens.  
24 The effect of pore pressure was obtained as negligible (Fig. 10). The bending point stress decreased with respect to  
25 the confining pressure at preloading. We approximated the results with a linear superposition of axial stress,

1 confining pressure, and pore pressure in preloading to obtain the following expression:

$$2 \quad \sigma_B = (0.93 \pm 0.07)\sigma - (1.05 \pm 0.11)P_C - (0.002 \pm 0.15)P_p \quad (3)$$

3 or

$$4 \quad \sigma_B = (0.93 \pm 0.07)\Delta\sigma - (0.11 \pm 0.11)P_C - (0.002 \pm 0.15)P_p \quad (4)$$

5 where  $\sigma_B$ ,  $\sigma$ ,  $P_C$ ,  $P_p$ , and  $\Delta\sigma$  denote the bending point stress, preloaded axial total stress, preloaded confining  
6 pressure, preloaded pore pressure, and preloaded axial differential stress, respectively. The negligible effect of pore  
7 pressure in the test series was obtained by chance. The sensitivity of the bending stress value (0.11 in Eq. (4)) to the  
8 preloading confining pressure was approximately 1/5 of that obtained in the Kaiser effect. This demonstrated an  
9 advantage of the TMM when compared to the Kaiser effect.

### 11 **3.6 Effect of stress exceeding preload albeit applied for a shorter duration**

12 The dry Kimachi sandstone specimens were subject to the following:

- 13 (1) compression at 30% UCS for 24 h as a preload to simulate in-situ rock stress;
- 14 (2) compression up to 40% UCS by a triangular loading pattern for approximately 1 min to simulate the stress  
15 concentration at rock sampling (Fig. 11);
- 16 (3) unloading and maintaining for specified delay times; and subsequently,
- 17 (4) cyclic loading twice up to 50% of UCS to obtain the stress-tangent modulus curves.

18 All loading and unloading operations were undertaken at a strain rate of  $10^{-4} \text{ s}^{-1}$ . Seven specimens were tested with  
19 delay times corresponding to a maximum of 1 week.

20 Bending points were observed at 40% UCS (16 MPa) for delay times between 0 and 1 hour (Fig. 12a–c). This  
21 indicated that the memory of the long term-preload was erased under higher short term stress. Bending points were  
22 observed at 30% UCS (12 MPa) and 40% UCS for a delay time of 3 h (Fig. 12d). This indicates that memories of  
23 both the long-term preload and the higher short-term load were detected. Bending points were observed only at  
24 30% UCS after delay times of 1 d and 3 d (Fig. 12e and f). The memory of the larger short-term stress was lost and  
25

1 only the memory of the long-term preload was detected. A bending point was not observed for a delay time of 1  
2 week (Fig. 12g), and thus the memories of both loads were lost.

3

#### 4 **4. DISCUSSION**

5 The experimental results are summarized as follows:

6

7 (1) The bending point appears at the preloading stress level in the axial stress-tangent modulus diagram during  
8 cyclic loading for four dry rocks. Bending points are observed under the preloading stress level even after a  
9 delay time of 6 weeks after 17 h of preloading.

10 (2) A clear effect of strain rates for cyclic loading is not observed with the exception of the slowest strain rate at  
11 which the specimen lost stress memory during the long experimental duration.

12 (3) A clear effect of preloading water temperature is not observed between 295 K and 353 K.

13 (4) Stress memory is lost very easily when the water content of the specimens change. The water content of rock  
14 cores should be maintained unchanged to the maximum possible extent until stress measurements by cyclic  
15 loading are completed.

16 (5) Confining pressure during triaxial cyclic loading affects the bending point stress value.

17 (6) Pore pressure during triaxial cyclic loading affects the bending point stress value.

18 (7) In uniaxial cyclic loading for triaxially preloaded rocks, confining pressure for preloading affects the  
19 bending point stress value although the effects of the pore pressure are negligible.

20 (8) It is estimated that the memory of a larger stress over a short time at rock sampling is lost, and it is  
21 potentially possible to evaluate a precise value of the normal component of in-situ rock stress (which acted  
22 over geological time in the direction of the specimen) if an appropriate delay time is set.

23

24 Results (1)–(3) and (8) prompt further investigation and improvement of the tangent modulus method. Result (4)  
25 may be considered as a practical albeit difficult guideline. Results (5) and (6) are academically interesting although  
26 they do not warrant further investigation because it is significantly easier to perform uniaxial cyclic loading than  
27 triaxial cyclic loading. Result (7) leads to the conclusion that it is necessary to consider lateral stress components

1 other than axial stress, and the result appears natural because rock deformation is strongly affected by confining  
2 pressure. An estimation of the three-dimensional stress state is potentially possible by combining Eq. (3) or Eq. (4)  
3 for more than seven directions (or six directions if pore pressure is ignored). It should be noted that this does not  
4 mean that more than six holes are required. Specimens in various directions are prepared from a thick rock core  
5 from a drill hole. For example, 30-mm thick and 60-mm long specimens in any direction are prepared by re-drilling  
6 from a rock core with a diameter exceeding 67.1 mm. However, further investigations should be performed for the  
7 cases in which the directions of specimen do not coincide with the principal stress directions. The negligible effect  
8 of pore pressure is useful to estimate the normal stress value. Conversely, this limits the estimation of pore pressure  
9 by TMM. This does not lead to significant disadvantages because in-situ pore pressure can be measured by other  
10 means. However, the negligible effect is potentially obtained by chance and should be investigated further with  
11 respect to other rock types.

## 13 **5. Case study at AK tunnel in Hokkaido, Japan**

14 Stress measurements were performed at AK tunnel in Hokkaido, Japan (Goto et al., 2007 in Japanese and  
15 Kawamura et al., 2006 in Japanese) in 2005 by using TMM and the pilot hole wall deformation method. The latter  
16 method is a stress relief method utilizing changes in diameter in three directions and axial displacements along four  
17 directions during overcoring (Lee et al., 2009). The method does not require a strain gage attachment to the  
18 borehole wall and instead measures displacement using mechanical transducers. Therefore, it is expected as suitable  
19 for severe conditions such as muddy sludges and rough borehole walls. The Cretaceous and highly fractured rock  
20 mass consisted of hard sandstone with a UCS of 237 MPa and a 50% tangent modulus of 55 GPa.

21  
22 The N62°W horizontal borehole was drilled from the sidewall of the tunnel. The overburden was 98 m and  
23 overcoring was attempted at depths corresponding to 1.0, 5.4, 7.4, and 8.4 m. Displacement during overcoring was  
24 only recorded at the depth of 8.4 m due to the highly fractured nature of the rock mass. The calculated maximum,  
25 intermediate, and minimum principal stresses were 43, 6, and -13 MPa, respectively (Fig. 13). The displacement  
26 behavior due to stress relief was considerably unstable, and the calculated stresses could potentially contain errors.  
27 However, it is noted that the rock stress significantly exceeded the overburden pressure and was nearly uniaxial.

1

2 Stress measurement using TMM was performed on the rock core from the aforementioned drill hole. The 150-mm  
3 thick core was highly fractured, and samples at approximately 1 m from the sidewall with relatively fewer fractures  
4 were used for the tests. Ideally, specimens in six independent directions are required to obtain the stress tensor.  
5 However, 30-mm thick and 60-mm long specimens in the axial direction (V) and the two perpendicular directions  
6 (P1 and P2) were prepared by re-drilling the thick rock core because the length of the thick core was insufficient  
7 and the thick core was not orientated due to fractures. The rock core was maintained as immersed in tap water, and  
8 the test was performed as soon as possible (10 d after the sampling) to minimize the loss of stress memory.

9

10 The wet specimens were quickly cyclic loaded in air at  $10^{-4} \text{ s}^{-1}$  after 10 days of in-situ sampling. Bending points  
11 were detected for five out of six V specimens (Fig. 14) and in all three P1 specimens. A bending point was not  
12 detected in the four P2 specimens. Average bending point stress corresponded to  $30.8 \pm 6.0 \text{ MPa}$  in V and  $25.4 \pm 7.7$   
13  $\text{MPa}$  in P1. It was not possible to directly compare the results with the results discussed above as obtained from the  
14 overcoring method. However, bending points were detected for the hard sandstone specimens from in-situ rock  
15 mass, and the stress level at the bending point was similar to the maximum principal stress from an overcoring  
16 method.

17

## 18 **6. CONCLUDING REMARKS**

19 In the study, TMM for measurement of in-situ rock stress was proposed as an improved oriented core method. The  
20 procedure to determine in-situ rock stress by TMM was as follows: Oriented rock cores were sampled from the site  
21 and cylindrical rock specimens were constructed, and the specimens were uniaxially or triaxially compressed twice  
22 to a given stress level. The stress value of the bending point in the stress-tangent modulus curve in the first loading  
23 cycle or the point where the first and the second stress-tangent modulus curves begin to separate (the point was also  
24 termed as the bending point for convenience) was considered as the normal component of in-situ rock stress in the  
25 direction of the specimen.

26

27 In order to evaluate the potential of the method, the existence of a bending point for four uniaxially preloaded dry

1 specimens of rock from soft porous tuff and sandstones to a hard crystalline granite was investigated. The effects of  
2 the strain rate, changes in temperature or water content, confining and pore pressures, and stresses exceeding the  
3 preload on the bending point stress value were also experimentally investigated on the preloaded specimens. The  
4 main results were as follows: (1) The bending point appeared at the preloading stress level in the axial  
5 stress-tangent modulus diagram during the cyclic loading for four dry rocks, and the points were observed at the  
6 preloading stress level even after a time delay of 6 weeks for 17 h of preloading; (2) a clear effect of the strain rate  
7 for the cyclic loading was not observed with the exception of the slowest strain rate at which the specimen lost any  
8 stress memory given the long experimental duration; (3) a clear effect of preloading water temperature between 295  
9 K and 353 K was not observed; (4) stress memory was very easily lost when the water content of specimens  
10 changed, and thus it was necessary to maintain the water content of rock cores to the maximum possible extent until  
11 stress measurement by cyclic loading was completed; (5) the confining pressure during triaxial cyclic loading  
12 affected the bending point stress value; (6) the pore pressure during triaxial cyclic loading affected the bending  
13 point stress value; (7) in uniaxial cyclic loading for triaxially preloaded rocks, the confining pressure for preloading  
14 affected the bending point stress value while the effects of pore pressure were negligible; and (8) the memory of  
15 higher stresses over a short time at rock sampling was lost, and it was potentially possible to evaluate the precise  
16 value of the normal component of in-situ rock stress (which acts over geologically-long times in the specimen  
17 direction) if an appropriate delay time was set.

18

19 In the case study at AK tunnel in Hokkaido, Japan, it was confirmed that bending points were detected for rock  
20 specimens from in-situ rock mass, and that the stress level at the bending point was similar to the maximum  
21 principal stress by using an overcoring method.

22

23 It is expected that future studies will focus on investigating the tangent modulus method in detail, improve on the  
24 same, and widely used it to measure in-situ rock stress.

25

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## Captions of figures

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Fig. 1 Preloading and cyclic loading. 1 and 2 mean the first and the second loading cycle, respectively.

Fig. 2 Examples of stress-tangent modulus curve in cyclic loading. 1 and 2 mean the first and the second loading cycle, respectively. Strain rate and preloading duration were  $10^{-5} \text{ s}^{-1}$  and 60 min. for Shirahama sandstone. They were  $10^{-4} \text{ s}^{-1}$  and 100 min. for Inada granite.

Fig. 3 Maximum delay time for stress memory with duration of preload application  $t_L$  for dry Shirahama Sandstone. Strain was measured by a clip gage.

Fig. 4 Schematic figures showing deformation of a very nonlinear rock.

Fig. 5 Influence of strain rates for the cyclic loading of dry Kimachi sandstone. Strain was either measured by a clip gage or evaluated from stroke.

Fig. 6 Influence of water temperature for preloading of Kimachi sandstone

Fig. 7 Influence of confining pressure change at cyclic loading for dry Shirahama sandstone. Confining pressure and axial stress for preloading was 5 MPa and 15.8 MPa, respectively.

Fig. 8 Influence of confining pressure change at cyclic loading for dry Kimachi sandstone. Confining pressure and axial stress for preloading is 10 MPa and 29 MPa, respectively.

Fig. 9 Influence of pore pressure on bending point stress for saturated Kimachi sandstone. Total confining pressure, pore pressure and total axial stress for preload were 10 MPa, 5 MPa and 22 MPa, respectively.



1 Fig. 10 Bending point stress by uniaxial cyclic loading for triaxially preloaded saturated Kimachi Sandstone.  
2 Preloaded differential axial stress was 12 MPa for all specimens. Preloaded pore pressure was 5 MPa except for 0.9  
3 MPa and 4.9 MPa for confining pressure of 1 MPa and 5 MPa, respectively in (b). Strain was based on a clip gage.

4  
5 Fig. 11 Preloading, larger stress application for short period and cyclic loading.

6  
7 Fig. 12 Stress-tangent modulus curves. Pre-stress and short time-larger stress are 12 MPa and 16 MPa,  
8 respectively. Strain was measured by the clip gage. Red and blue curves show the first and the second loading,  
9 respectively.

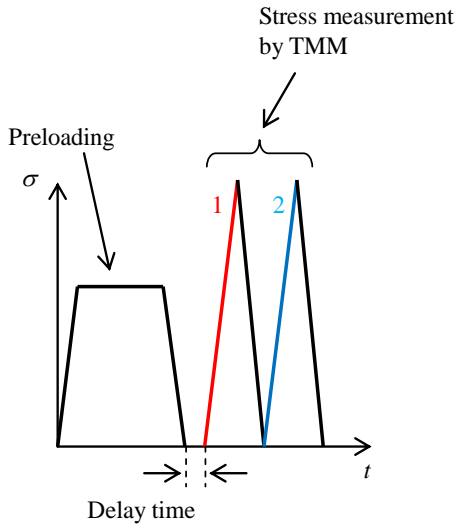
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11 Fig. 13 Stereo projection of the stress state (MPa) measured using the pilot hole wall displacement method at AK  
12 tunnel onto the lower hemisphere.

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14 Fig. 14 An example of stress-tangent modulus curve pairs for specimen V-1.

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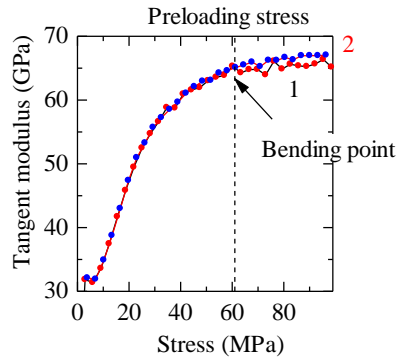
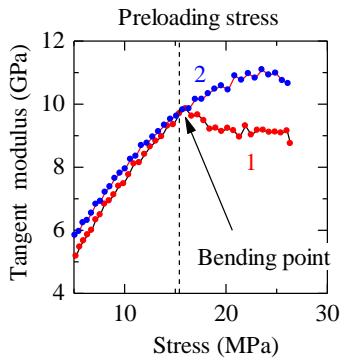
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### Figures



2

3 Fig. 1 Preloading and cyclic loading. 1 and 2 mean the first and the second loading cycle, respectively.



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5 (a) Dry Shirahama sandstone

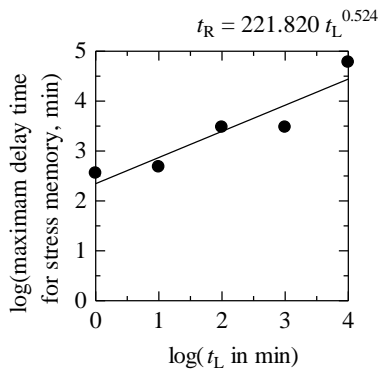
(b) Dry Inada granite

6 Fig. 2 Examples of stress-tangent modulus curve in cyclic loading. 1 and 2 mean the first and the second

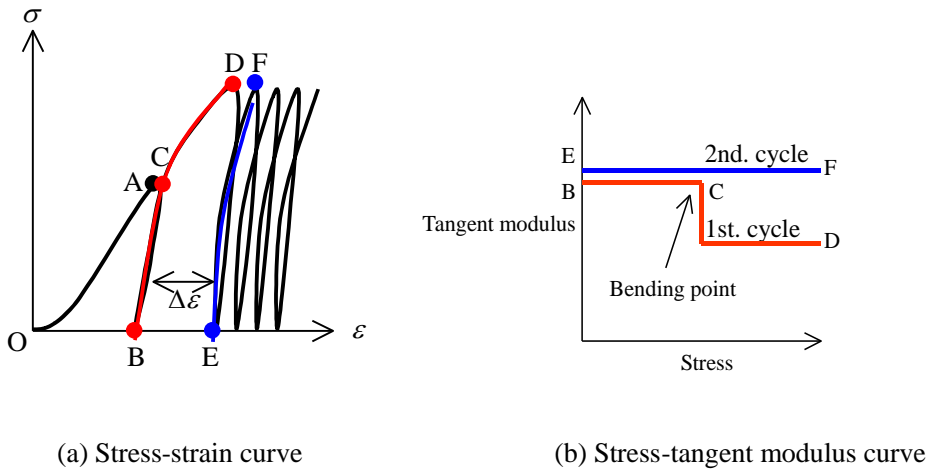
7 loading cycle, respectively. Strain rate and preloading duration were  $10^{-5} \text{ s}^{-1}$  and 60 min. for Shirahama sandstone.

8 They were  $10^{-4} \text{ s}^{-1}$  and 100 min. for Inada granite.

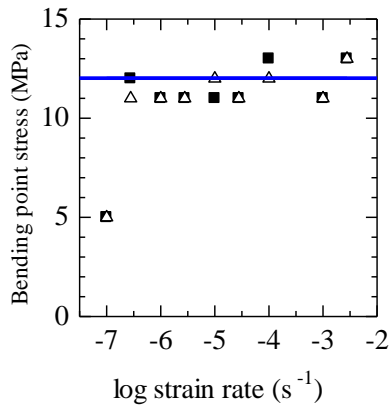
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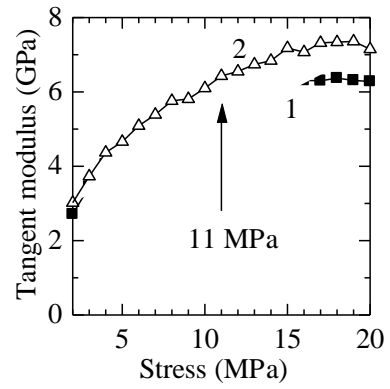
1  
 2 Fig. 3 Maximum delay time for stress memory with duration of preload application  $t_L$  for dry Shirahama  
 3 Sandstone. Strain was measured by a clip gage.



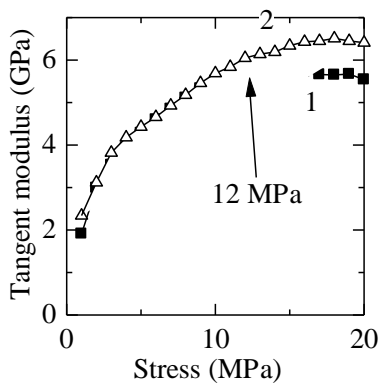
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 5 (a) Stress-strain curve (b) Stress-tangent modulus curve  
 6 Fig. 4 Schematic figures showing deformation of a very nonlinear rock.  
 7



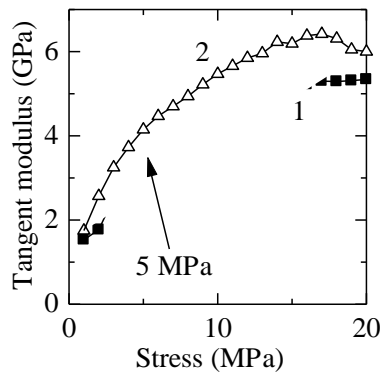
(a) Influence of strain rate



(b)  $10^{-3} \text{ s}^{-1}$  (stroke base)

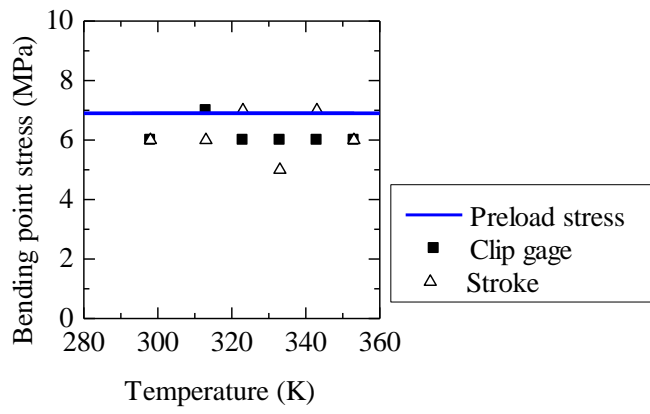


(c)  $10^{-6} \text{ s}^{-1}$  (stroke base)

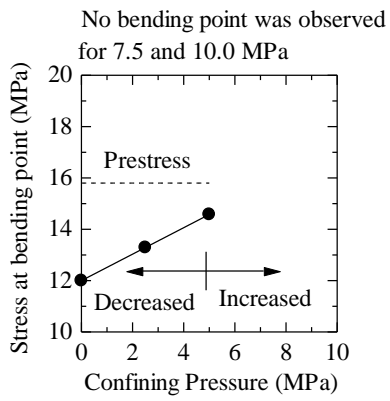


(d)  $10^{-7} \text{ s}^{-1}$  (stroke base)

Fig. 5 Influence of strain rates for the cyclic loading of dry Kimachi sandstone and examples of stress-tangent modulus curves. Strain was either measured by a clip gage or evaluated from stroke.

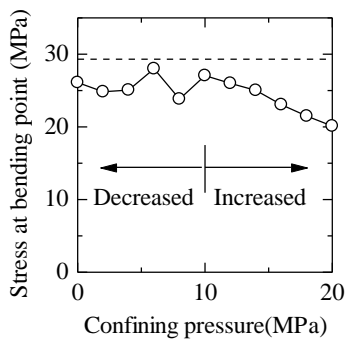


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 2 Fig. 6 Influence of water temperature for preloading of Kimachi sandstone  
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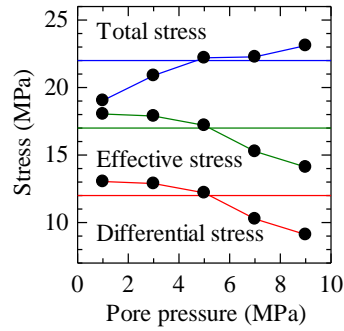
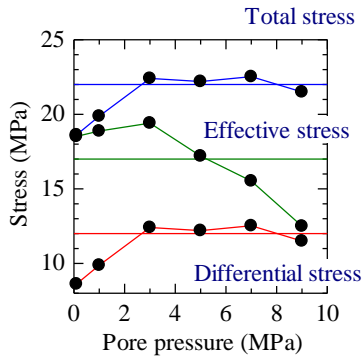
2 Fig. 7 Influence of confining pressure change at cyclic loading for dry Shirahama sandstone. Confining pressure  
3 and axial stress for preloading was 5 MPa and 15.8 MPa, respectively.



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5 Fig. 8 Influence of confining pressure change at cyclic loading for dry Kimachi sandstone. Confining pressure  
6 and axial stress for preloading is 10 MPa and 29 MPa, respectively.

7

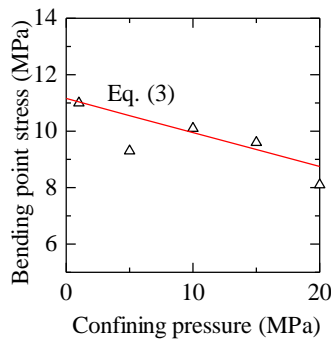
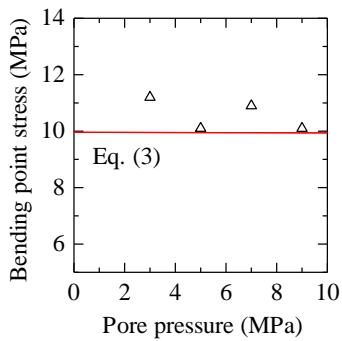


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2 (a) Constant total confining pressure of 10 MPa (b) Constant effective confining pressure of 5 MPa

3 Fig. 9 Influence of pore pressure on bending point stress for saturated Kimachi sandstone. Total confining

4 pressure, pore pressure and total axial stress for preload were 10 MPa, 5 MPa and 22 MPa, respectively.



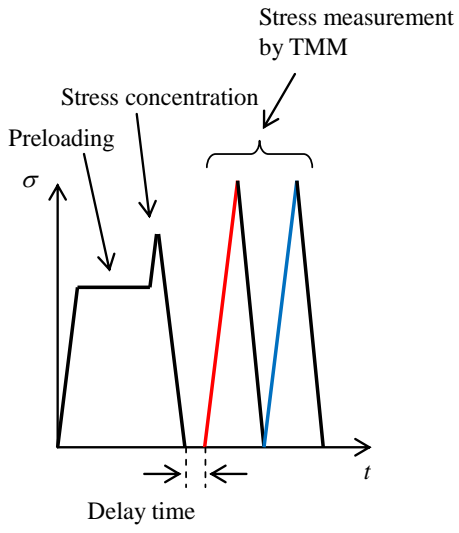
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6 (a) Constant confining pressure of 10 MPa (b) Nearly constant pore pressure of 5 MPa

7 Fig. 10 Bending point stress by uniaxial cyclic loading for triaxially preloaded saturated Kimachi Sandstone.

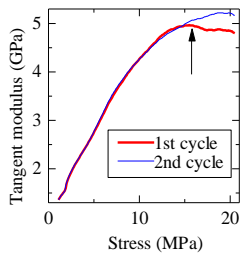
8 Preloaded differential axial stress was 12 MPa for all specimens. Preloaded pore pressure was 5 MPa except for 0.9

9 MPa and 4.9 MPa for confining pressure of 1 MPa and 5 MPa, respectively in (b). Strain was based on a clip gage.

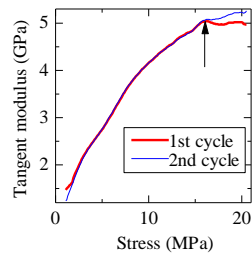


1  
2 Fig. 11 Preloading, larger stress application for short period and cyclic loading.  
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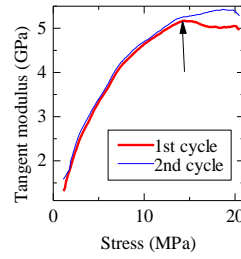




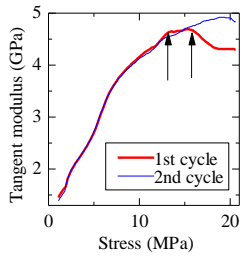
(a) No delay time



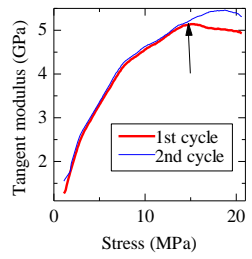
(c) 30 min. delay



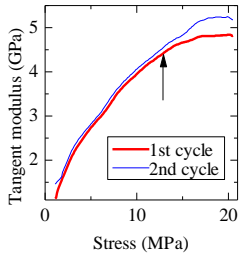
(d) 1 hour delay



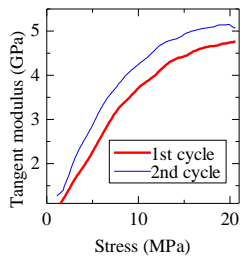
(e) 3 hour delay



(f) 1 day delay

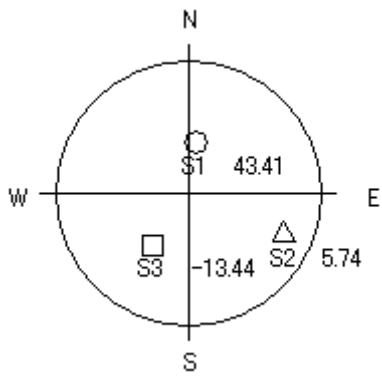


(g) 3 day delay

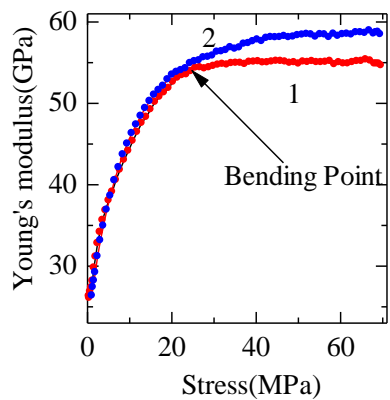


(h) 1 week delay

Fig. 12 Stress-tangent modulus curves. Pre-stress and short time-larger stress are 12 MPa and 16 MPa, respectively. Strain was measured by the clip gage. Red and blue curves show the first and the second loading, respectively.



1  
 2 Fig. 13 Stereo projection of the stress state (MPa) measured using the pilot hole wall displacement method at AK  
 3 tunnel onto the lower hemisphere.



4 ]  
 5 Fig. 14 An example of stress-tangent modulus curve pairs for specimen V-1.  
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