

computational resources are limited, and mesh refinement is feasible. When higher accuracy is required for uniform regular mesh problems, PS elements are recommended. They combine superior accuracy with minimal computational overhead. For distorted mesh problems requiring high accuracy, Q8 elements are the preferred choice. With moderate accuracy and memory capability, Allman elements are the preferred choice.

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